WORKSHOP CALCULATION & SCIENCE

(NSQF)

1st YEAR

(As per Revised Syllabus July 2022)

Mechanic Agricultural Machinery

Directorate General of Training

DIRECTORATE GENERAL OF TRAINING
MINISTRY OF SKILL DEVELOPMENT & ENTREPRENEURSHIP
GOVERNMENTOF INDIA

NATIONAL INSTRUCTIONAL MEDIA INSTITUTE, CHENNAI

Nimi

Post Box No. 3142, CTI Campus, Guindy, Chennai - 600 032

Workshop Calculation & Science

Mechanic Agricultural Machinery - 1ˢᵗ Year NSQF

As per Revised Syllabus July 2022

Developed & Published by

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FOREWORD

The Government of India has set an ambitious target of imparting skills to 30 crores people, one out of every four Indians, by 2020 to help them secure jobs as part of the National Skills Development Policy. Industrial Training Institutes (ITIs) play a vital role in this process especially in terms of providing skilled manpower. Keeping this in mind, and for providing the current industry relevant skill training to Trainees, ITI syllabus has been recently updated with the help of comprising various stakeholder's viz. Industries, Entrepreneurs, Academicians and representatives from ITIs.

The National Instructional Media Institute (NIMI), Chennai, has now come up with instructional material to suit the revised curriculum for **Workshop Calculation & Science - Mechanic Agricultural Machinery 1st Year** NSQF (Revised 2022) under CTS will help the trainees to get an international equivalency standard where their skill proficiency and competency will be duly recognized across the globe and this will also increase the scope of recognition of prior learning. NSQF trainees will also get the opportunities to promote life long learning and skill development. I have no doubt that with NSQF the trainers and trainees of ITIs, and all stakeholders will derive maximum benefits from these IMPs and that NIMI's effort will go a long way in improving the quality of Vocational training in the country.

The Executive Director & Staff of NIMI and members of Media Development Committee deserve appreciation for their contribution in bringing out this publication.

Jai Hind

Ms. TRISHALJIT SETHI,
Additional Secretary / Director General (Training),
Ministry of Skill Development & Entrepreneurship,
Government of India.

New Delhi - 110 001

PREFACE

The National Instructional Media Institute(NIMI) was set up at Chennai, by the Directorate General of Training, Ministry of skill Development and Entrepreneurship, Government of India, with the technical assistance from the Govt of the Federal Republic of Germany with the prime objective of developing and disseminating instructional Material for various trades as per prescribed syllabus and Craftsman Training Programme(CTS) under NSQF levels.

The Instructional materials are developed and produced in the form of Instructional Media Packages (IMPs), consisting of Trade Theory, Trade Practical, Test and Assignment Book, Instructor Guide, Wall charts, Transparencies and other supportive materials. The above material will enable to achieve overall improvement in the standard of training in ITIs.

A national multi-skill programme called SKILL INDIA, was launched by the Government of India, through a Gazette Notification from the Ministry of Finance (Dept of Economic Affairs), Govt of India, dated 27th December 2013, with a view to create opportunities, space and scope for the development of talents of Indian Youth, and to develop those sectors under Skill Development.

The emphasis is to skill the Youth in such a manner to enable them to get employment and also improve Entrepreneurship by providing training, support and guidance for all occupation that were of traditional types. The training programme would be in the lines of International level, so that youths of our Country can get employed within the Country or Overseas employment. The **National Skill Qualification Framework (NSQF)**, anchored at the National Skill Development Agency(NSDA), is a Nationally Integrated Education and competency-based framework, to organize all qualifications according to a series of **levels of Knowledge, Skill and Aptitude.** Under NSQF the learner can acquire the Certification for Competency needed at any level through formal, non-formal or informal learning.

The **Workshop Calculation & Science -** Mechanic Agricultural Machinery 1st Year NSQF (Revised 2022) under CTS is one of the book developed by the core group members as per the NSQF syllabus.

The **Workshop Calculation & Science -** Mechanic Agricultural Machinery 1st Year NSQF (Revised 2022) under CTS as per NSQF is the outcome of the collective efforts of experts from Field Institutes of DGT, Champion ITI's for each of the Sectors, and also Media Development Committee **(MDC)** members and Staff of **NIMI.** NIMI wishes that the above material will fulfill to satisfy the long needs of the trainees and instructors and shall help the trainees for their Employability in Vocational Training.

NIMI would like to take this opportunity to convey sincere thanks to all the Members and Media Development Committee (MDC) members.

Chennai - 600 032   **EXECUTIVE DIRECTOR**

ACKNOWLEDGEMENT

INTRODUCTION

The material has been divided into independent learning units, each consisting of a summary of the topic and an assignment part. The summary explains in a clear and easily understandable fashion the essence of the mathematical and scientific principles. This must not be treated as a replacment for the instructor's explanatory information to be imparted to the trainees in the classroom, which certainly will be more elaborate. The book should enable the trainees in grasping the essentials from the elaboration made by the instructor and will help them to solve independently the assignments of the respective chapters. It will also help them to solve the various problems, they may come across on the shop floor while doing their practical exercises.

The assignments are presented through 'Graphics' to ensure communications amongst the trainees. It also assists the trainees to determine the right approach to solve the problems. The required relevent data to solve the problems are provided adjacent to the graphics either by means of symbols or by means of words. The description of the symbols indicated in the problems has its reference in the relevant summaries.

At the end of the exercise wherever necessary assignments, problems are included for further practice.

Time allotment:

Duration of 1st Year : 34 Hrs

Time allotment for each title of exercises has been given below. **Workshop Calculation & Science - Mechanic Agricultural Machinery** 1st Year NSQF Revised Syllabus 2022.

S.No	Title	Exercise No.	Time in Hrs
1	Unit, Fractions	1.1.01 - 1.1.07	4
2	Square root, Ratio and Proportions, Percentage	1.2.08 - 1.2.14	6
3	Material Science	1.3.15 & 1.3.16	3
4	Mass, Weight, Volume and Density	1.4.17 & 1.4.18	3
5	Speed and Velocity, Work, Power and Energy	1.5.19 - 1.5.21	4
6	Heat & Temperature and Pressure	1.6.22 & 1.6.23	4
7	Basic Electricity	1.7.24	2
8	Mensuration	1.8.25 - 1.8.27	4
9	Levers and Simple machines	1.9.28 & 1.9.29	2
10	Trigonometry	1.10.30 - 1.10.32	2
		Total	**34 Hrs**

LEARNING / ASSESSABLE OUTCOME

On completion of this book you shall be able to

- **Demonstrate basic mathematical concept and principles to perform practical operations.**

- **Understand and explain basic science in the field of study.**

CONTENTS

SYLLABUS

1st Year

Workshop Calculation & Science - Mechanic Agricultural Machinery
Revised syllabus July 2022 under CTS

S.No.	Title	Time in Hrs
I	**Unit, Fractions**	4
	1 Classification of Unit System	
	2 Fundamental and Derived Units F.P.S, C.G.S, M.K.S and SI Units	
	3 Measurement Units and Conversion	
	4 Factors, HCF, LCM and Problems	
	5 Fractions – Addition, Subtraction, Multiplication & Division	
	6 Decimal Fractions – Addition, Subtraction, Multiplication & Division	
	7 Solving Problems by using calculator	
II	**Square root, Ratio and Proportions, Percentage**	6
	1 Square and Square root	
	2 Simple problems using calculator	
	3 Applications of Pythagoras theorem and related problems	
	4 Ratio and Proportion	
	5 Ratio and Proportion - Direct and Indirect proportions	
	6 Percentage	
	7 Percentage - Changing percentage to decimal and fraction	
III	**Material Science**	3
	1 Types of metal, types of ferrous and non ferrous metals	
	2 Physical and Mechanical Properties of metals	
IV	**Mass, Weight, Volume, and Density**	3
	1 Mass, volume, density, weight and specific gravity	
	2 Related problems for mass, volume, density, weight and specific gravity	
V	**Speed and Velocity, Work, Power and Energy**	4
	1 Speed and velocity - Rest, motion, speed, velocity, difference between speed and velocity, acceleration and retardation	
	2 Speed and velocity - Related problems on speed & velocity	
	3 Work, power, energy, HP, IHP, BHP and efficiency	

S.No.	Title	Time in Hrs
VI	**Heat & Temperature and Pressure**	**4**
	1 Concept of heat and temperature, effects of heat, difference between heat and temperature, boiling point & melting point of different metals and non-metals	
	2 Concept of pressure - Units of pressure, atmospheric pressure, absolute pressure, gauge pressure and gauges used for measuring pressure	
VII	**Basic Electricity**	**2**
	1 Introduction and uses of electricity, electric current AC, DC their comparison, voltage, resistance and their units	
VIII	**Mensuration**	**4**
	1 Area and perimeter of square, rectangle and parallelogram	
	2 Surface area and Volume of solids - cube, cuboid, cylinder, sphere and hollow cylinder	
	3 Finding the lateral surface area , total surface area and capacity in litres of hexagonal, conical and cylindrical shaped vessels	
IX	**Levers and Simple Machines**	**2**
	1 Simple machines - Effort and load, mechanical advantage, velocity ratio, efficiency of machine, relation between efficiency, velocity ratio and mechanical advantage	
	2 Lever & Simple machines - Lever and its types	
X	**Trigonometry**	**2**
	1 Measurement of angles	
	2 Trigonometrical ratios	
	3 Trigonometrical tables	
	Total	**36**

Unit, Fractions - Classification of unit system

Necessity

All physical quantities are to be measured in terms of standard quantities.

Unit

A unit is defined as a standard or fixed quantity of one kind used to measure other quantities of the same kind.

Classification

Fundamental units and derived units are the two classifications.

Fundamental units

Units of basic quantities of length, mass and time.

Derived units

Units which are derived from basic units and bear a constant relationship with the fundamental units.E.g. area, volume, pressure, force etc.

Systems of units

– F.P.S system is the British system in which the basic units of length, mass and time are foot, pound and second respectively.

– C.G.S system is the metric system in which the basic units of length, mass and time are centimeter, gram and seconds respectively.

– M.K.S system is another metric system in which the basic units of length, mass and time are metre, kilogram and second respectively.

– S.I. units are referred to as Systems International units which is again of metric and the basic units, their names and symbols are as follows.

Fundamental units and derived units are the two classifications of units.

Length, mass and time are the fundamental units in all the systems (i.e) F.P.S, C.G.S, M.K.S and S.I. systems.

Example

Length: What is the length of copper wire in the roll , if the roll of copper wire weighs 8kg, the dia of wire is 0.9cm and the density is 8.9 gm/cm^3?

Solution

mass of copper wire in the roll = 8kg (or)8000grams
Dia of copper wire in the roll = 0.9cm
Density of copper wire = 8.9 gm/cm^3

Area of cross section of copper wire

$$= \frac{\pi\, d^2}{4} = \frac{\pi \times (0.9^2)}{4} = 0.636 cm^2$$

Volume of copper wire

$$= \frac{\text{Mass of copper wire}}{\text{Density of copper wire}} = \frac{8000 grams}{8.9 \text{ gm/cm}^3} = 898.88 cm^3$$

Length of copper wire

$$= \frac{\text{Volume of copper wire}}{\text{Area of cross section of copper wire}} = \frac{898.88 cm^3}{0.636 cm^2}$$

$$= 1413.33 \text{ cm}$$

Length of copper wire =1413cm.

Time: The S.I. unit of time, the second, is another base units of S.I., it is defined as the time interval occupied by a number of cycles of radiation from the calcium atom. The second is the same quantity in the S.I. in the British and in the U.S. systems of units.

Fundamental units of F.P.S, C.G.S, M.K.S and S.I

S.No.	Basic quantity	British units		Metric units				International units	
		F.P.S	Symbol	**C.G.S**	Symbol	**M.K.S**	Symbol	**S.I Units**	Symbol
1	Length	Foot	ft	Centimetre	cm	Metre	m	Metre	m
2	Mass	Pound	lb	Gram	g	Kilogram	kg	Kilogram	Kg
3	Time	Second	s	Second	s	Second	s	Second	s
4	Current	Ampere	A	Ampere	A	Ampere	A	Ampere	A
5	Temperature	Fahrenheit	°F	Centigrade	℃	Centigrade	℃	Kelvin	K
6	Light intensity	Candela	Cd	Candela	Cd	Candela	Cd	Candela	Cd

Workshop Calculation & Science - MAM

Unit, Fractions - Fundamental and Derived units F.P.S, C.G.S, M.K.S and SI units

Derived units of F.P.S, C.G.S, M.K.S and SI system

S.No	Physical quantity	British units		Metric units		MKS		International units	
		FPS	Symbol	CGS	Symbol	MKS	Symbol	SI Units	Symbol
1	Area	Square foot	ft^2	Square centimetre	cm^2	Square metre	m^2	Square metre	m^2
2	Volume	Cubic foot	ft^3	Cubic centimetre	cm^3	Cubic metre	m^3	Cubic metre	m^3
3	Density	Pound per cubic foot	lb/ft^3	Gram per cubic centimetre	g/cm^3	Kilogram per cubic metre	kg/m^3	Kilogram per cubic metre	Kg/m^3
4	Speed	Foot per second	ft/s	Centimetre per second	cm/sec	Metre per second	m/sec	Metre per second	m/sec
5	Velocity (linear)	Foot per second	ft/s	Centimetre per second	cm/sec	Metre per second	m/sec	Metre per second	m/sec
6	Acceleration	Foot per square second	ft/s^2	Centimetre per square second	cm/sec^2	Metre per square second	m/sec^2	Metre per square second	m/sec^2
7	Retardation	Foot per square Second	ft/s^2	Centimetre per square second	cm/sec^2	Metre per square second	m/sec^2	Metre square second	m/sec^2
8	Angular velocity	Degree per second	Deg/sec	Radian per second	rad/sec	Radian per second	rad/sec	Radian per second	rad/sec
9	Mass	Pound (slug)	lb	Gram	g	Kilogram	kg	Kilogram	kg
10	Weight	Pound	lb	Gram	g	Kilogram weight	kg	Newton	N
11	Force	Pounds	lbf	dyne	dyn	Kilogram force	kgf	Newton	N(kgm/sec^2)
12	Power	Foot pound per second	ft.lb/sec	Gram.centimetre/sec	g.cm/sec	kilogram metre per second	kg.m/sec		-
		Horse power	hp	Erg per second		watt	W	watt	W(J/sec)
13	Pressure, Stress	Pound per square inch	lb/in^2	Gram per square centimetre	g/cm^2	Kilogram per square metre	kg/m^2	Newton per square metre	N/m^2
14	Energy, Work	Foot.pound	ft.lb	Gram centimetre	g.cm	Kilogram metre	kg.m	joule	J(Nm)
15	Heat	British thermal unit	BTU	calorie	Cal	joule	J	joule	J(Nm)
16	Torque	Pound force foot	lbf.ft	Newton millimetre	N mm	Kilogram metre	kg.m	Newton metre	Nm
17	Temperature	Degree Fahrenheit	°F	Degree Centigrade	°C	Kelvin	K	Kelvin	K

Unit, Fractions - Measurement units and conversion

Units and abbreviations

Quantity	Units	Abbreviation of unit
Calorific value	kilojoules per kilogram	kJ/kg
Specific fuel consumption	kilogram per hour per newton	kg/hr/N
Length	millimetre, metre, kilometre	mm, m, km
Mass	kilogram, gram	kg, g
Time	seconds, minutes, hours	s, min, h
Speed	centimetre per second, metre per second kilometre per hour, miles per hour	cm/s, m/s km/h, mph
Acceleration	metre-per-square second	m/s^2
Force	newtons, kilonewtons	N,kN
Moment	newton-metres	Nm
Work	joules	J
Power	horsepower, watts, kilowatts	Hp, W, kW
Pressure	newton per square metre kilonewton per square metre	N/m^2 kN/m^2
Angle	radian	rad
Angular speed	radians per second radians-per-square second revolutions per minute revolutions per second	rad/s rad/s^2 Rpm rev/s

Decimal multiples and parts of unit

Decimal power	Value	Prefixes	Symbol	Stands for
10^{12}	1000000000000	tera	T	billion times
10^9	1000000000	giga	G	thousand millintimes
10^6	1000000	mega	M	million times
10^3	1000	kilo	K	thousand times
10^2	100	hecto	h	hundred times
10^1	10	deca	da	ten times
10^{-1}	0.1	deci	d	tenth
10^{-2}	0.01	centi	c	hundredth
10^{-3}	0.001	milli	m	thousandth
10^{-6}	0.000001	micro	µ	millionth
10^{-9}	0.000000001	nano	n	thousand millionth
10^{-12}	0.000000000001	pico	p	billionth

SI units and the British units:

| Quantity	SI unit → British unit	British unit → SI unit
Length	1 m = 3.281 ft 1 km = 0.621 mile	1 ft = 0.3048 m 1 mile = 1.609 km
Speed	1 m/s = 3.281 ft/s 1 km/h = 0.621 mph	1 ft/s = 0.305 m/s 1 mph = 1.61 km/h
Acceleration	$1 \text{ m/s}^2 = 3.281 \text{ ft/s}^2$	$1 \text{ ft/s}^2 = 0.305 \text{ m/s}^2$
Mass	1 kg = 2.205 lb	1 lb = 0.454 kg
Force	1 N = 0.225 lbf 1 MN	1 lbf = 4.448 N 1 million newtons
Torque	1 Nm = 0.738 lbf ft	1 lbf ft = 1.355 Nm
Pressure	$1 \text{ N/m}^2 = 0.000145 \text{ lbf/in}^2$ $1 \text{ Pa} = 1 \text{ N/m}^2$ $1 \text{ bar} = 14.5038 \text{ lbf/in}^2$	$1 \text{ lbf/in}^2 = 6.896 \text{ kN/m}^2$ $1 \text{ lbf/in}^2 = 6.895 \text{ kN/m}^2$
Energy, work	1 J = 0.738 ft lbf 1 J = 0.239 calorie 1 kJ = 0.948 BTU (1 therm = 100 000 BTU) 1 kJ = 0.526 CHU	1 ft lbf = 1.355 J 1 calorie = 4.186 J 1 BTU = 1.055 kJ 1 CHU = 1.9 kJ
Power	1 kW = 1.34 hp	1 hp = 0.7457 kW
Fuel consumption	1km/L = 2.82 mile/gallon	1 mpg = 0.354 km/L
Specific fuel consumption	1 kg/kWh = 1.65 lb/bhp h 1 litre/kWh=1.575 pt/bhp h	1 lb/bhp h = 0.606 kg/kWh 1 pt/bhp h = 0.631 litre/kWh
Calorific value	1 kJ/kg = 0.43 BTU/lb 1 kJ/kg = 0.239 CHU/lb	1 BTU/lb = 2.326 kJ/kg 1 CHU/lb = 4.188 kJ/kg

Prefixes for decimal multiples and submultiples

Use		
1 Megapascal	= 1 MPa	= 1000000 Pa
1 Kilowatt	= 1 kW	= 1000 W
1 Hectolitre	= 1 hL	= 100 L
Decanewton	= 1 daN	= 10 N
Decimetre	= 1 dm	= 0.1 m
1 Centimetre	= 1 cm	= 0.01 m
1 Millimetre	= 1 mm	= 0.001 m
1 Micrometre	= 1 um	= 0.000001 m

Conversion factors

1 inch	=	25.4 mm
1 mm	=	0.03937 inch
1 metre	=	39.37 inch
1 micron	=	0.00003937"
1 kilometre	=	0.621 miles
1 pound	=	453.6 g
1 kg	=	2.205 lbs
1 metric ton	=	0.98 ton

Units of physical quantities
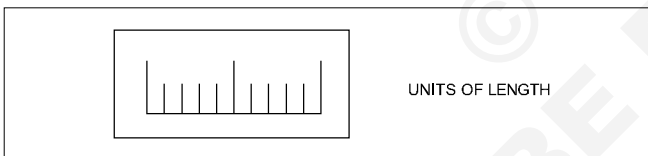
UNITS OF LENGTH

Units of length

Micron	1 μ	=	0.001 mm
Millimetre	1 mm	=	1000 μ
Centimetre	1 cm	=	10 mm
Decimetre	1 dm	=	10 cm
Metre	1 m	=	10 dm
Kilometre	1 km	=	1000 m
Inch	1"	=	25.4 mm
Foot	1'	=	0.305 m
Yard	1 Yd	=	0.914 m
Nautical mile	1 NM	=	1852 m
Geographical mile	1	=	1855.4 m

Units of area

UNITS OF AREA
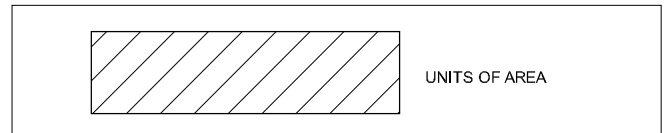
Square millimetre	1 mm^2	
Square centimetre	1 cm^2	= 100 mm^2
Square decimetre	1 dm^2	= 100 cm^2
Square metre	1 m^2	= 100 dm^2
Are	1 a	= 100 m^2
Hectare	1 ha	= 100 a
Square kilometre	1 km^2	= 100 ha
Square inch	1 sq.in	= 6.45 cm^2
Square foot	1 sq.ft	= 0.093 m^2
Square yard	1 sq.yd	= 0.84 m^2
Square metre	1 m^2	= 10.76 ft^2
Acre	1	= 40.5 a

1 Acre = 100 cent	1 Hectare = 2.47 acres
1 Cent = 436 Sq. ft. 1 Ground = 2400 Sq.ft.	1 acre = 0.4047 Hectare
	1 Hectare = 10000 sq. metre

Units of weight

UNITS OF WEIGHT
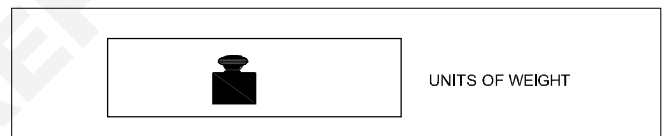
Milligram - force	1 mgf	
Gram-force	1 gf	1000 mgf
Kilogram-force	1 kgf	= 1000 gf
Tonne	1 t	= 1000 kgf
Ounce	1	= 28.35 gf
Pound	1 lbs	= 0.454 kgf
Long ton	1	= 1016 kgf
Short ton	1	= 907 kgf
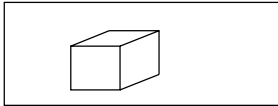
Units of volume and capacity

UNITS OF VOLUME AND CAPACITY

Cubic millimetre	1 mm^3	
Cubic centimetre	1 cm^3	= 1000 mm^3
Cubic decimetre	1 dm^3	= 1000 cm^3
Cubic metre	1 m^3	= 1000 dm^3
Litre	1 l	= 1 dm^3
Hectolitre	1 hl	= 100 l
Cubic inch	1 cu. in	= 16.387 cm^3
Cubic foot	1 cu. ft	= 28317 cm^3
Gallon (British)	1 gal	= 4.54 l
1cubic metre	1 m^3	= 1000 litres
1000 Cu.cm	1000 cm^3	= 1 litre
1 cubic foot	1 ft^3	= 6.25 Gallon
1 litre	1lt	= 0.22 Gallon

Circular unit
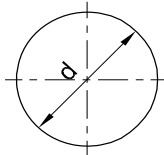
CIRCULAR OF UNIT

Radian

Relationship between Radian and Degree

$$1 \text{ Radian} = \frac{180°}{\pi}$$

$$180^0 = \pi \text{ Radian};$$

$$1 \text{ Degree} = \frac{\pi}{180} \text{ Radian}$$

Work

WORK

Kilogram-force	1 kgfm	= 9.80665 J
Metre	1 kgfm	= 9.80665 Ws
Joule	1 J	= 1 Nm
Watt-second	1 Ws	= 0.102 kgfm
Kilowatt hour	1 kWh	= 3.6 x 10^6 J
		= 859.8456 kcal$_{IT}$
I.T.Kilocalorie	1 kcal$_{IT}$	= 426.kgfm

Power

POWER

Kilogram-force metre/second	
1 kgfm/s	= 9.80665 W
Kilowatt	1 kW = 1000 W = 1000 J/s
	= 102 kgfm/s (approx.)
Metric horse power	1 HP = 75 kgfm/s
	= 0.736 kW
1 Calorie	= 4.187J
I.T.Kilocalorie/hour = 1 kcal$_{IT/h}$ = 1.163 W	

Pressure

Pascal	1 Pa	= 1 N/m^2	1 atm	= 101325 Pa
Bar	1 bar = 10N/cm^2	= 100000 Pa–Torr	1 torr	= $\frac{101325}{760}$ ≈ 133.32 pa
Atmosphere	1 atm	= 1 kgf/cm^2	1 kgf/cm^2 = 735.6 mm of mercury	

TEMPERATURE

Scale	Freezing point	Boiling point
Centigrade (˚C)	0°C	100°C
Fahrenheit (°F)	32°F	212°F
Kelvin (K)	273K	373K
Reaumur (°R)	0°R	80°R

TEMPERATURE

$$\frac{°R}{80} = \frac{°C}{100} = \frac{K-273}{100} = \frac{°F-32}{180}$$

FORCE

Force	In C.G.S. System : Force (Dyne)	= Mass (gm)XAcceleration (cm/sec^2)
	In F.P.S. System : Force (Poundal)	= Mass (Ib) X Acceleration (ft./sec^2)
	In M.K.S System : Force (Newton)	= Mass (Kg) x Acceleration (mtr./sec^2)
	1 Dyne	= 1 gm x1 cm/sec^2
	1 Poundal	= 1 lb x 1 ft/sec^2
	1 Newton	= 1 kg x 1 mtr/sec^2 = 10^5 dynes
	1gm weight	= 981 Dynes
	1 lb weight	= 32 Poundals
	1 kg weight	= 9.81 Newtons

ELECTRICAL QUANTITIES

V	Electric potential	V	Volt	V(W/A)
E	Electromotive force	V	Volt	V(W/A)
I	Electric current	A	Ampere	A
R	Electric resistance	Ω	Ohm	Ω (V/A)
e	Specific resistance	Ω m	Ohm metre	Vm/A
G	Conductance	Ω^{-1}	Siemens	S

ELECTRICAL QUANTITIES
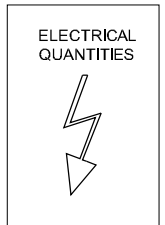
Assignment - Answer the following question.

1 Convert 320 kilometres into miles _____

2 Convert 16 tons into kilograms _____

3 Convert 40 inches into centimetres _____

4 Convert 8 metres into feet _____

5 Convert 2.5 gallons into litres _____

6 Convert 5 litres into gallons _____

7 120°C = _____ °F.

8 Expand the abbreviations of the following

   a N/m^2

   b RPM

9 Convert the following S.I. units as required.

   a Length

   i 3.4 m = _____mm

   ii 10.2 km = _____mile

   b Mass

   i 650 g = _____kg

   ii 120 mg = _____g

   c Force

   i 1.2 N = _____kg

   ii 25 kg = _____N

   d Work, energy, amount of heat

   i 120 KJ = _____J

   ii 300 wh = _____kwh

   e Power

   i 0.2 kW = _____W

   ii 350 W = _____kW

   f Convert as required.

   i 5 N = _____KN

Unit, Fractions - Factors, HCF, LCM and problems

Prime Numbers and whole Numbers

Factor

A factor is a small number which divides exactly into a bigger number.e.g.

To find the factors of 24, 72, 100 numbers

24 = 2 x 2 x 2 x 3

72 = 2 x 2 x 2 x 3 x 3

100 = 2 x 2 x 5 x 5

The numbers 2,3,5 are called factors.

Definition of a prime factor

Prime factor is a number which divides a prime number into factors.e.g.

57 = 3 x 19

The numbers 3 and 19 are prime factors.

They are called as such, since 3 & 19 also belong to prime number category.

Definition of H.C.F

The Highest Common Factor

The H.C.F of a given group of numbers is the highest number which will exactly divide all the numbers of that group.e.g.

To find the H.C.F of the numbers 24, 72, 100

24 = 2 x 2 x 2 x 3

72 = 2 x 2 x 2 x 3 x 3

100 = 2 x 2 x 5 x 5

The factors common to all the three numbers are

2 x 2 = 4. So HCF = 4.

Definition of L.C.M

Lowest common multiple

The lowest common multiple of a group of numbers is the smallest number that will contain each number of the given group without a remainder.e.g.

- Factorise the following numbers

7,17,20,66,128

7,17 - These two belong to Prime numbers. Hence no factor except unity and itself.

2	20
2	10
	5

Factors of 20 = 2 x 2 x 5

2	66
3	33
	11

Factors of 66 = 2 x 3 x 11

2	128
2	64
2	32
2	16
2	8
2	4
	2

Factors of 128 = 2 x 2 x 2 x 2 x 2 x 2 x 2

- Select prime numbers from 3 to 29

3,5,7,11,13,17,19,23,29

- Find the HCF of the following group of numbers HCF of 78, 128, 196

2	78
3	39
	13

78 = 2 x 3 x 13

2	128
2	64
2	32
2	16
2	8
2	4
	2

128 = 2 x 2 x 2 x 2 x 2 x 2 x 2

2	196
2	98
	49

196 = 2 x 2 x 49

HCF = 2

- Find LCM of 84,92,76

LCM =	2	84, 92, 76
	2	42, 46, 38
	3	21, 23, 19
		7, 23, 19

LCM = 2 x 2 x 3 x 7 x 23 x 19 = 36708

- To find out the LCM of 36, 108, 60

2	36, 108, 60
2	18, 54, 30
3	9, 27, 15
3	3, 9, 5
	1, 3, 5

LCM of the number

36, 108, 60 = 2 x 2 x 3 x 3 x 3 x 5 = 540

The necessity of finding LCM and HCF arises in subtraction and addition of fractions.

Unit, Fractions - Fractions - Addition, subtraction, multiplication & division

Description

A minimal quantity that is not a whole number. For e.g. .

$\dfrac{1}{5}$ a vulgur fraction consists of a numerator and denominator.
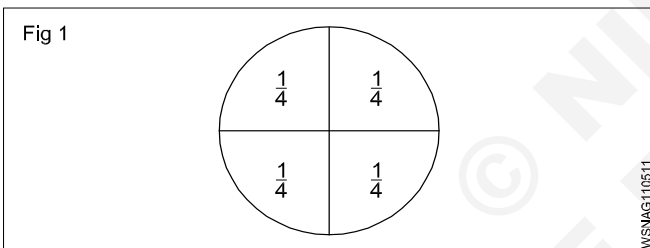
Numerator/Denominator

The number above the line in a vulgar fraction showing how many of the parts indicated by the denominator are taken is the numerator. The total number of parts into which the whole quantity is divided and written below the line in a vulgar fraction is the denominator. e.g.

$$\dfrac{1}{4}, \dfrac{3}{4}, \dfrac{7}{12}$$

1,3,7 - numerators   4,12 - denominators
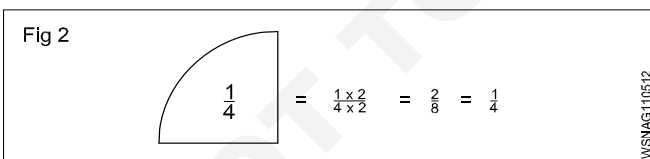
Fraction: Concept

Every number can be represented as a fraction.e.g.

$1\dfrac{1}{4} = \dfrac{5}{4}$, A full number can be represented as an apparent

fraction.e.g. (Fig 1)

Fig 1

Fraction: Value

The value of a fraction remains the same if the numerator and denominator of the fraction are multiplied or divided by the same number.(Fig 2)


Fig 2

$$\dfrac{1}{4} = \dfrac{1 \times 2}{4 \times 2} = \dfrac{2}{8} = \dfrac{1}{4}$$

Multiplication

When fractions are to be multiplied, multiply all the numerators to get the numerator of the product and multiply all the denominators to form the denominator of the product. (Fig 3)


Fig 3

$$\dfrac{1}{4} \times \dfrac{3}{1} = \dfrac{1 \times 3}{4 \times 1} = \dfrac{3}{4}$$
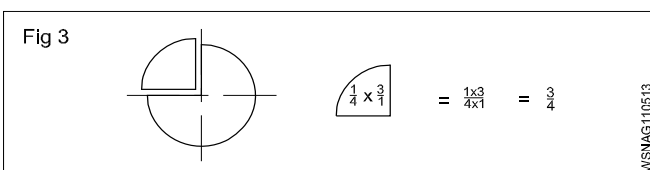
Division

When a fraction is divided by another fraction the dividend is multiplied by the reciprocal of the divisor. (Fig 4)

Fig 4

$$\dfrac{1}{2} \div \dfrac{3}{1} = \dfrac{1}{2} \times \dfrac{1}{3} = \dfrac{1}{6}$$
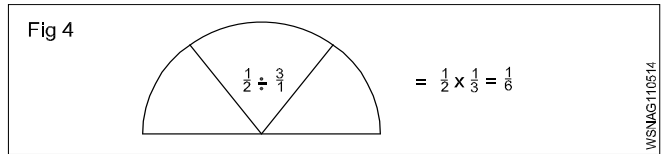
Addition and Subtraction

The denominators of the fractions should be the same when adding or subtracting the fractions. Unequal denominators must first be formed into a common denominator. It is the lowest common denominator and it is equal to the product of the most common prime numbers of the denominators of the fractions in question.(Fig 5)

Fig 5

$$\dfrac{1}{4} + \dfrac{1}{4} = \dfrac{2}{4} = \dfrac{1}{2}$$

$$\dfrac{1}{4} + \dfrac{1}{2} = \dfrac{1+2}{4} = \dfrac{3}{4}$$
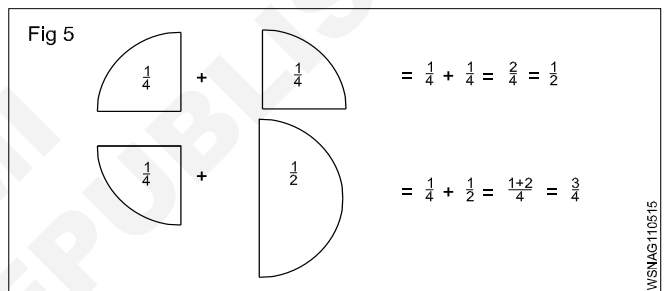
Examples

- Multiply $\dfrac{3}{4}$ by $\dfrac{2}{3}$,

$$\dfrac{3}{4} \times \dfrac{2}{3} = \dfrac{6}{12} = \dfrac{1}{2}$$

- Divide $\dfrac{3}{8}$ by $\dfrac{3}{4}$,

$$\dfrac{3}{8} \div \dfrac{3}{4} = \dfrac{3}{8} \times \dfrac{4}{3} = \dfrac{1}{2}$$

- Add $\dfrac{3}{4}$ and $\dfrac{2}{3}$,

$$\dfrac{3}{4} + \dfrac{2}{3} = \dfrac{9}{12} + \dfrac{8}{12} = \dfrac{17}{12} = 1\dfrac{5}{12}$$

- sub $\dfrac{7}{16}$ from $\dfrac{17}{32}$

$$\dfrac{17}{32} - \dfrac{7}{16} = \dfrac{17}{32} - \dfrac{14}{32} = \dfrac{(17-14)}{32} = \dfrac{3}{32}$$

Types of fractions

- Proper fractions are less than unity. Improper fractions have their numerators greater than the denominators.

- A mixed number has a full number and a fraction.

Addition of fraction

Add $\dfrac{1}{2} + \dfrac{1}{8} + \dfrac{5}{12}$

To add these fractions we have to find out L.C.M of denominators 2,8,12.

Find L.C.M of 2,8,12

Step 1 L.C.M

$$
\begin{array}{c|c}
2 & 2,8,12 \\
\hline
2 & 1,4,6 \\
\hline
 & 1,2,3
\end{array}
$$

Factors are 2,2,2,3

Hence L.C.M = 2 x 2 x 2 x 3 = 24

Step 2

$\dfrac{1}{2} + \dfrac{1}{8} + \dfrac{5}{12} = \dfrac{12}{24} + \dfrac{3}{24} + \dfrac{10}{24}$

$= \dfrac{12 + 3 + 10}{24} = \dfrac{25}{24} = 1\dfrac{1}{24}.$

Subtraction of fraction

subtract $9\dfrac{15}{32}$ from $17\dfrac{9}{16}$ or $(17\dfrac{9}{16} - 9\dfrac{15}{32})$

Step 1: Subtract whole number first 17 - 9 = 8

Step 2: L.C.M of 16,32 = 32

Since number 16 divides the number 32

Subtracting fractions = $\dfrac{3}{32}$

Adding with whole number from Step 1

we get $8 + \dfrac{3}{32} = 8\dfrac{3}{32}$

Common fractions

Problems with plus and minus sign

Example

solve $3\dfrac{3}{4} + 6\dfrac{7}{8} - 4\dfrac{5}{16} - \dfrac{9}{32}$

Rule to be followed

1 Add all whole numbers

2 add all + Numbers

3 Add all - Numbers

4 Find L.C.M of all denominators

Solution

Step 1: Add whole numbers = 3 + 6 - 4 = 5

Step 2: Add fractions = $\dfrac{3}{4} + \dfrac{7}{8} - \dfrac{5}{16} - \dfrac{9}{32}$

L.C.M of 4,8,16,32 is 32

$\dfrac{24 + 28 - 10 - 9}{32}$

$= \dfrac{52 - 19}{32}$

$= \dfrac{33}{32} = 1\dfrac{1}{32}$

Step 3: Adding again with the whole number

we get $5 + 1\dfrac{3}{32} = 6\dfrac{3}{32}$

Examples

Common fractions

- Multiply

a $\dfrac{3}{8}$ by $\dfrac{4}{7} = \dfrac{3}{8}$ x $\dfrac{4}{7} = \dfrac{3}{14}$ b $\dfrac{2}{3}$ x $\dfrac{3}{4}$ x $\dfrac{5}{8} = \dfrac{5}{16}$

- Division

a $\dfrac{5}{16} \div \dfrac{5}{32} = \dfrac{5}{16}$ x $\dfrac{32}{5} = 2$

b $4\dfrac{2}{3} \div 3\dfrac{1}{7} = \dfrac{14}{3} \div \dfrac{22}{7} = \dfrac{14}{3}$ x $\dfrac{7}{22} = \dfrac{49}{33} = 1\dfrac{16}{33}$

- Addition

$\dfrac{1}{2} + \dfrac{1}{4} + \dfrac{1}{8}$

L..C.M = 2,4,8 = 8

$\dfrac{1}{2} + \dfrac{1}{4} + \dfrac{1}{8} = \dfrac{4 + 2 + 1}{8} = \dfrac{7}{8}$

- Subtraction

$5\dfrac{1}{4} - 3\dfrac{3}{4} = 5 - 3 + \dfrac{1}{4} - \dfrac{3}{4}$

$= 2 + \dfrac{1}{4} - \dfrac{3}{4} = 2\dfrac{1}{4} - \dfrac{3}{4}$

$= \dfrac{9}{4} - \dfrac{3}{4} = \dfrac{9 - 3}{4}$

$= \dfrac{6}{4} = \dfrac{3}{2} = 1\dfrac{1}{2}$

Assignment

1 Convert the following into improper fractions.

a $1\dfrac{2}{7} = $ _____

b $4\dfrac{3}{5} = $ _____

c $3\dfrac{3}{5} = $ _____

2 Convert the following into mixed numbers.

a $\dfrac{12}{11} = $ _____

b $\dfrac{36}{14} = $ _____

c $\dfrac{18}{10} = $ _____

3 Place the missing numbers.

a $\dfrac{11}{13} = \dfrac{x}{91}$ _____

b $\dfrac{3}{5} = \dfrac{42}{x}$ _____

c $\dfrac{9}{14} = \dfrac{x}{98}$ _____

4 Simplify.

a $\dfrac{45}{60} = $ _____

b $\dfrac{8}{12} = $ _____

5 Multiply.

a $5 \times \dfrac{2}{3} = $ _____

b $\dfrac{3}{4} \times 2 = $ _____

c $\dfrac{3}{4} \times \dfrac{5}{6} = $ _____

6 Divide

a $\dfrac{1}{4} \div \dfrac{3}{4} = $ _____

b $6 \div \dfrac{3}{4} = $ _____

c $\dfrac{3}{4} \div \dfrac{2}{7} = $ _____

7 Place the missing numbers.

a $\dfrac{2}{3} = \dfrac{1}{12} \times$ _____

b $\dfrac{14}{24} = \dfrac{1}{12} \times$ _____

c $\dfrac{7}{8} = \dfrac{1}{12} \times$ _____

8 Add the followings:

a $\dfrac{3}{4} + \dfrac{7}{12} = $ _____

b $\dfrac{7}{8} + \dfrac{3}{4} = $ _____

9 Subtract

a $\dfrac{4}{5} - \dfrac{2}{5} = $ _____

b $\dfrac{5}{6} - \dfrac{3}{4} = $ _____

10 Simplify

a $2\dfrac{6}{7} - \dfrac{3}{8} - \dfrac{1}{3} - 1\dfrac{1}{16} = $ _____

b $2\dfrac{2}{7} - \dfrac{5}{6} + 8 = $ _____

11 Express as improper fractions

a $5\dfrac{3}{4}$

b $3\dfrac{5}{64}$

c $1\dfrac{5}{12}$

Unit, Fractions - Decimal fractions - Addition, subtraction, multiplication & division

Description

Decimal fraction is a fraction whose denominator is 10 or powers of 10 or multiples of 10 (i.e.) 10, 100, 1000, 10000 etc. Meaning of a decimal number:-

12.3256 means

$$(1 \times 10) + (2 \times 1) + \frac{3}{10} + \frac{2}{100} + \frac{5}{1000} + \frac{6}{10000}$$

Representation

The denominator is omitted. A decimal point is placed at different positions of the number corresponding to the magnitude of the denominator

$Ex. \dfrac{5}{10} = 0.5, \dfrac{35}{100} = 0.35 \ \dfrac{127}{10000} = 0.0127, \dfrac{3648}{1000} = 3.648$

Addition and subtraction

Arrange the decimal fractions in a vertical order, placing the decimal point of each fraction to be added or subtracted, in succession one below the other, so that all the decimal points are arranged in a straight line. Add or subtract as you would do for a whole number and place the decimal point in the answer below the column of decimal points.

Decimal fractions less than 1 are written with a zero before the decimal point. Example: 45/100 = 0.45 (and not simply .45)

Add 0.375 + 3.686

```
  0.375
  3.686
 ------
  4.061
```

Subtract 18.72 from 22.61

```
 22.61
 18.72
 -----
  3.89
```

Multiplication

Ignore the decimal points and multiply as whole numbers. Find the total number of digits to the right of the decimal point. Insert the decimal point in the answer such that the number of digits to the right of the decimal point equals to the sum of the digits found to the right of the decimal points in the problem.

Multiply 2.5 by 1.25

= 25 x 125 = 3125. The sum of the figures to the right of decimal point is 3. Hence the answer is 3.125.

Division

Move the decimal point of the divisor to the right to make it a full number. Move the decimal point in the dividend to

the same number of places, adding zeroes if necessary. Then divide.

Divide 0.75 by 0.25

$$0.25\overline{)0.75}$$

$$\frac{0.75}{0.25} \times \frac{100}{100} = \frac{75}{25}$$

$$25\overline{)75} = 3$$

> **Move the decimal point in the multiplicand to the right to one place if the multiplier is 10, and to two places if the multiplier is 100 and so on. When dividing by 10 move the decimal point one place to the left, and, if it is by 100, move them point by two places and so on.**

Example

Allowance allowing 3 mm for cutting off each pin, how many pins can be made from a 900 mm long bar and how much material will be left out?

Fig 1
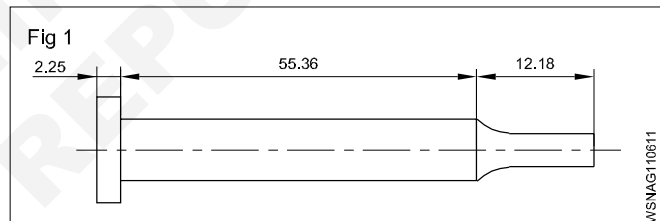
Total Length of pin	= 2.25 + 55.36 + 12.18
	= 69.79 mm
Cutting allowance	= 3 mm
Total Length	= length of pin + cutting allowance
	= 69.79 mm + 3 mm
	= 72.79 mm
Length of the bar	= 900 mm
No.of pins to be cut	$= \dfrac{900}{72.79} = 12.394$
	= 12 pins
Left out material	= Total length - length of pin + cutting allowance
	= 900 - 12 x 69.79 + 12 x 3
	= 900 - 837.48 + 36
	= 900 - 873.48
Left out length	= 26.52 mm

Conversion of Decimals into fractions and vice-versa

- Convert decimal into fractions

Example

Convert 0.375 to a fraction

Now place 1 under the decimal point followed by as many zeros as there are numbers

$$0.375 = \frac{375}{1000} = \frac{15}{40} = \frac{3}{8}$$

$$0.375 = \frac{3}{8}$$

- Convert fraction into decimal

Example

- Convert $\frac{9}{16}$ to a decimal

Proceed to divide $\frac{9}{16}$ in the normal way of division but put zeros (as required) after the number 9 (Numerator)

```
        0.5625
16 ) 90000
        80
        100
         96
         40
         32
         80
         80
          0
```

$$\frac{9}{16} = 0.5625$$

Recurring decimals

While converting from fraction to decimals, some fractions can be divided exactly into a decimal. In some fractions the quotient will not stop. It will continue and keep recurring. These are called recurring decimals.

Examples

- convert $\frac{1}{3}, \frac{2}{3}, \frac{1}{7}$

  a $\quad \frac{1}{3} = \frac{10000}{3} = 0.3333 - \text{Recurring}$

  b $\quad \frac{2}{3} = \frac{20000}{3} = 0.666 - \text{Recurring}$

  c $\quad \left(\frac{1}{7} = \frac{10000}{7} = 0.142857142 - \text{Recurring} \right)$

Method of writing approximations in decimals

1.73556	= 1.7356	Correct to 4 decimal places
5.7343	= 5.734	Correct to 3 decimal places
0.9345	= 0.94	Correct to 2 decimal places

Multiplication and division by 10,100,1000

Multiplying decimals by 10

A decimal fraction can be multiplied by 10,100,1000 and so on by moving the decimal point to the right by as many places as there are zeros in the multiplier.

- 4.645 x 10 = 46.45 (one place)
- 4.645 x 100 = 464.5 (two places)
- 4.645 x 1000 = 4645 (three places)

Dividing decimals by 10

A decimal fraction can be divided by 10,100,1000 and so on, by moving the decimal point to the left by as many places as required in the divisor by putting zeros

Examples

- 3.732 ÷ 10 = 0.3732 (one place)
- 3.732 ÷ 100 = 0.03732 (two places)
- 3.732 ÷ 1000 = 0.003732 (three places)

Examples

- Rewrite the following number as a fraction

  453.273

  453.273

  $$= (4 \times 100) + (5 \times 10) + (3 \times 1) + \frac{2}{10} + \frac{7}{100} + \frac{3}{100}$$

  $$= 453 \frac{273}{1000}$$

- Write the representation of decimal places in the given number 0.386

  3 - Ist decimal place
  8 - IInd decimal place
  6 - IIIrd decimal place

- Write approximations in the following decimals to 3 places.

  a 6.9453 ——> 6.945
  b 8.7456 ——> 8.746

- Convert fraction to decimal

  $$\frac{21}{24} = \frac{7}{8} = 0.875$$

- Convert decimal to fraction

  $$0.0625 = \frac{625}{10000} = \frac{5}{80} = \frac{1}{16}$$

Assignment

1 Write down the following decimal numbers in the expanded form.

   a 514.726

   b 902.524

2 Write the following decimal numbers from the expansion.

   a $500 + 70 + 5 + \dfrac{3}{10} + \dfrac{2}{100} + \dfrac{9}{1000}$

   b $200 + 9 + \dfrac{1}{10} + \dfrac{3}{100} + \dfrac{5}{1000}$

3 Convert the following decimals into fractions in the simplest form.

   a 0.72

   b 5.45

   c 3.64

   d 2.05

4 Convert the following fraction into decimals

   a $\dfrac{3}{5}$

   b $\dfrac{10}{4}$

   c $24\dfrac{54}{1000}$

   d $\dfrac{12}{25}$

   e $\dfrac{8}{25}$

   f $1\dfrac{3}{25}$

5 Addition of decimals

   a 4.56 + 32.075 + 256.6245 + 15.0358

   b 462.492 + 725.526 + 309.345 + 626.602

6 Subtract the following decimals

   a 612.5200 − 9.6479

   b 573.9246 − 215.6000

7 Add and subtract the following

   a 56.725 + 48.258 − 32.564

   b 16.45 + 124.56 + 62.7 - 3.243

8 Multiply the following

   a By 10,100,1000

      i   3.754 x 10

      ii 8.964 x 100

      iii 2.3786 x 1000

      iv 0.005 x 1000

   b By whole numbers

      i   8.4 x 7

      ii 56.72 x 8

   c By another decimal figure (use calculator)

      i   15.64 x 7.68

      ii 2.642 x 1.562

9 Divide the following

   a $\dfrac{62.5}{25}$

   b $\dfrac{64.56}{10}$

   c $\dfrac{0.42}{100}$

   d $\dfrac{48.356}{1000}$

10 Division

   a $\dfrac{16.8}{1.2}$

   b $\dfrac{1.54}{1.1}$

11 Change the fraction into a decimal

   i $1\dfrac{5}{8}$

   ii $\dfrac{12}{25}$

12 Find the value

   20.5 x 40 ÷ 10.25 + 18.50

Unit, Fractions - Solving problems by using calculator

A pocket calculator allows to spend less time in doing tedious calculations. A simple pocket calculator enables to do the arithmetical calculations of addition, subtraction, multiplication and division, while a scientific type of calculator can be used for scientific and technical calculations also.

No special training is required to use a calculator. But it is suggested that a careful study of the operation manual of the type of the calculator is essential to become familiar with its capabilities. A calculator does not think and do. It is left to the operator to understand the problem, interpret the information and key it into the calculator correctly.

Constructional Details (Fig 1)

Fig 1
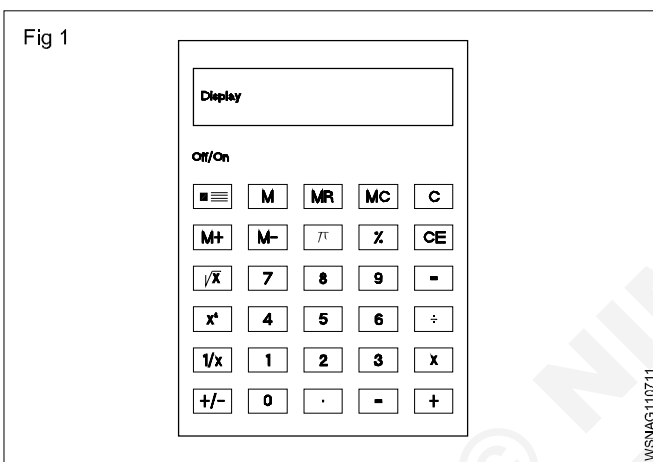
The keyboard is divided into five clear and easily recognizable areas and the display.

- **Data entry keys**

The entry keys are from $\boxed{0}$ ....to $\boxed{9}$

and a key for the decimal point $\boxed{.}$.

- **Clearing keys**

These keys have the letter 'C'

$\boxed{C}$ $\boxed{CLR}$ Clear totally

$\boxed{CE}$ Clear entry only

$\boxed{CM}$, $\boxed{MC}$ Clear memory

| Key	Description
$\boxed{+}$	Addition key
$\boxed{-}$	Subtraction key
$\boxed{x}$	Multiplication key
$\boxed{\div}$	Division key
$\boxed{=}$	Equals key to display the result

- **Function keys**

Key	Description
$\boxed{\pi}$	Pi key
$\boxed{\sqrt{x}}$	Square root key
$\boxed{\%}$	Percentage key
$\boxed{+/-}$	Sign change key
$\boxed{x^2}$	Square key
$\boxed{\frac{1}{X}}$	Reciprocal key

- **Memory keys**

Key	Description
$\boxed{M}$	Store the display number
$\boxed{M+}$	The displayed value is added to the memory
$\boxed{M-}$	The displayed value is subtracted from the memory
$\boxed{MR}\boxed{RCL}$	The stored value is recalled on to the display

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15

Further functional keys included in Scientific calculators are as shown in Fig 2.

Fig 2

DISPLAY

FUNCTION KEYS

MEMORY/ STORE KEYS

SCIENTIFIC CALCULATOR
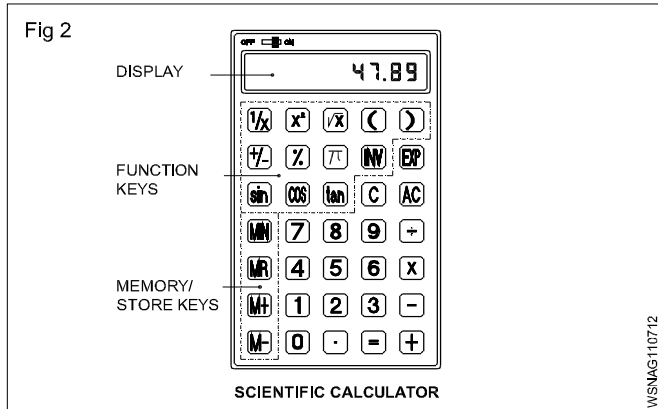
Sin Cos Tan ( ) For trigonometric functions and for brackets

Exp Exponent key

INV Some of the keys have coloured lettering above or below them. To use a function in coloured lettering, press INV key. INV will appear on the display. Then press the key that the coloured lettering identifies. INV will disappear from the display.

log , INV 10^x to obtain the logarithm of the displayed number and the antilogarithm of the displayed value.

INV R–P to convert displayed rectangular coordinates into polar coordinates.

INV P–R to convert displayed polar coordinates into rectangular coordinates.

- **The display**

The display shows the input data, interim results and answers to the calculations.

The arrangement of the areas can differ from one make to another. Keying in of the numbers is done via. an internationally agreed upon set of ten keys in the order that the numbers are written.

Rules and Examples:

- **Addition:** Example 18.2 + 5.7

Sequence	Input	Display
Input of the 1st term of the sum	1 8 . 2	18.2
Press + key	+	18.2
Input 2nd term of the sum. the first term goes into the register	5 . 7	5.7
Press the = key	=	23.9

- **Subtraction:** Example 128.8 - 92.9

Sequence	Input	Display
Enter the subtrahend	1 2 8 . 8	128.8
Press - key	-	128.8
Enter the minuend. The subtrahend goes into the register	9 2 . 9	92.9
Press the = key	=	35.9

- **Multiplication:** Example 0.47 x 2.47

Sequence	Input	Display
Enter multiplicand	. 4 7	0.47
Press x key	x	0.47
Enter multiplier, multiplicand goes to register	2 . 4 7	2.47
Press = key	=	1.1609

- **Division:** Example 18.5/2.5

Sequence	Input	Display
Enter the dividend	1 8 . 5	18.5
Press ÷ Key	÷	18.5
Enter the divisor goes to the register	2 . 5	2.5
Press = key	=	7.4

- **Multiplication & Division:**
  Example : 2.5 x 7.2 / 4.8 x 1.25

Sequence	Input	Display
Enter 2.5	2 . 5	2.5
Press x key	x	2.5
Enter 7.2	7 . 2	7.2
Press ÷ key	÷	18
Enter Open bracket	(	
Enter 4.8	4 . 8	4.8
Press x key	x	4.8
Enter 1.25	1 . 2 5	1.25
Enter Close bracket	)	6
Press = key	=	3.0

- Store in memory Example (2+6) (4+3)

Sequence	Input	Display
Workout for the first bracket	2	2
	+	2
	6	6
	=	8
Store the first result in	STO , M	8
x	or M+	
Workout for the 2nd bracket	4	4
	+	4
	3	3
	=	7
Press x key	x	7
Recall memory	RCL or MR	8
Press = key	=	56

- **Percentage:** Example 12% of 1500

Sequence	Input	Display
Enter 1500	1 5 0 0	1500
Press x key	x	1500
Enter 12	1 2	12
Press INV %	INV %	12
Press = key	=	180

- **Square root:** Example $\sqrt{2}+\sqrt{3\times5}$

Sequence	Input	Display
Enter 2	2	2
Press $\sqrt{a}$ key	$\sqrt{a}$	1.414
Press + key	+	1.414
Press bracket key	(	1.414
Enter 3	3	3
Press $\sqrt{a}$ key	$\sqrt{a}$	1.732
Press x key	x	1.732
Enter 5	5	5
Press $\sqrt{a}$ key	$\sqrt{a}$	2.236
Press bracket close key	)	3.873
Press = key	=	5.2871969
2 √ + (3 √ x 5 √) =		5.2871969

$\sqrt{2}+\sqrt{3\times5}$ = 5.287

- **Common logarithm:** Example log 1.23

Sequence	Input	Display
1 . 2 3 log	=	0.0899051

- **Power:** Example $123 + 30^2$

Sequence	Input	Display
1 2 3 + 3 0 INV X²	=	1023

Assignment

1 Using calculator solve the following

a 625 + 3467 + 20 + 341 + 6278 = _____

b 367.4 + 805 + 0.7 + 7.86 + 13.49 = _____

c 0.043 + 1.065 + 13.0 + 34.76 + 42.1 = _____

d 47160 + 1368.4 + 0.1 + 1.6901 + 134.267 = _____

2 Using calculator simplify the following

a 24367 - 4385 = _____

b 9.643 - 0.7983 = _____

c 4382.01 - 381.3401 = _____

d 693.42 - 0.0254 = _____

3 Using calculator find the values of the following

a 23 x 87 = _____

b 1376 x 0.81 = _____

c 678 x 243 = _____

d 0.75 x 0.24 = _____

4 Using calculator solve the following

a 22434 ÷ 3 = _____

b 4131 ÷ 243 = _____

c 469890 ÷ 230 = _____

d 3.026 ÷ 0.89 = _____

5 Solve the following
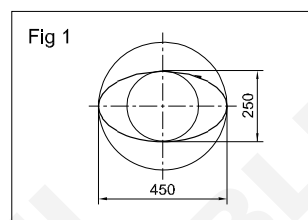
a $\dfrac{1170 \times 537.5}{13 \times 215}$ = _____

b $\dfrac{28.2 \times 18 \times 3500}{1000 \times 3 \times 0.8}$ = _____

6 Solve the following

a $\dfrac{(634 + 128) \times (384 - 0.52)}{8 \times 0.3}$ = _____

b $\dfrac{(389 - 12.2) \times (842 - 0.05 - 2.6)}{(3.89 - 0.021) \times (28.1 + 17.04)}$ = _____
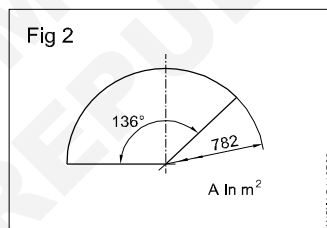
7

Fig 1

2a = 450 mm (major axis)

2b = 250 mm (minor axis)

Perimeter of the ellipse

A = _____ metre^2

Hint A = π x a x b unit^2

8

Fig 2

ø = 782 mm

α = 136°

Area of the sector

A = _____

Hint $A = \dfrac{\pi \times d^2}{4} \times \dfrac{\alpha}{360°}$

9

Fig 3   d = 1.25m
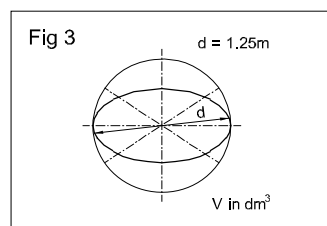
d = 1.25 metre

V = _____ dm^3

Volume of sphere

Hint $V = \dfrac{4}{3}\pi r^3$

10

Fig 4
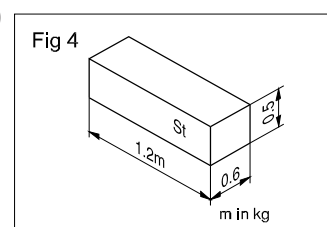
L = 1.2 metres

B = 0.6 metre

H = 0.5 metre

'ρ' (rho) density of steel = 7.85 kg/dm^3

m = _____ kg

(mass 'm = V x ρ)

Square root, Ratio and Proportions, Percentage - Square and square root

a   basic number

2   exponent

$\sqrt{}$ radial sign indicating the square root.

$\sqrt{a^2}$ square root of 'a' square
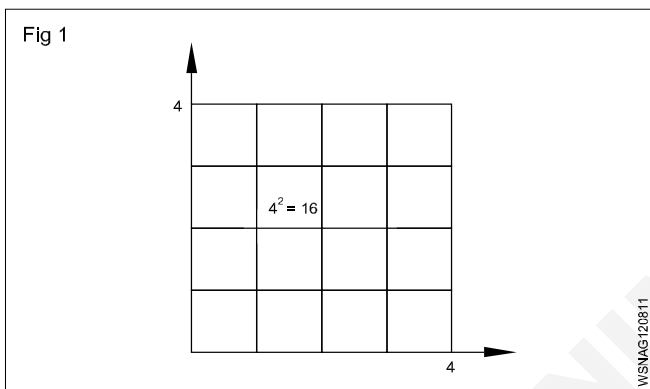
a^2 radicand

Square number

The square of a number is the number multiplied by itself.

Basic number x basic number = Square number

$a \times a = a^2$

$4 \times 4 = 4^2 = 16$

Fig 1

Splitting up

A square area can be split up into sub-areas. The largest square of 36 is made up of a large square 16, a small square 4 and two rectangles 8 each.
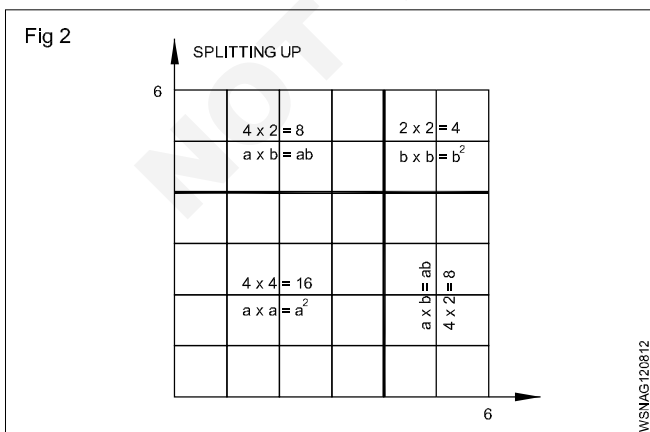
Large square 4 x 4 = 16 a^2

Two rectangles 2 x 4 x 2 = 16   2ab

Small square 2 x 2 = 4 b^2

Sum of sub-areas = 36 = $a^2 + 2ab + b^2$

$\sqrt{36} = \sqrt{a^2 + 2ab + b^2}$

Fig 2

Result: In order to find the square root, we split up the square numbers.

Extracting the square root procedure

- Starting from the decimal point form groups of two figures towards right and left. Indicate by a prime symbol. $\sqrt{4624.00}$

- Find the root of the first group, calculate the difference, bring down the next group.

- Multiply the root by 2 and divide the partial radicand.

- Enter the number thus calculated in the divisor for the multiplication.

Fig 3
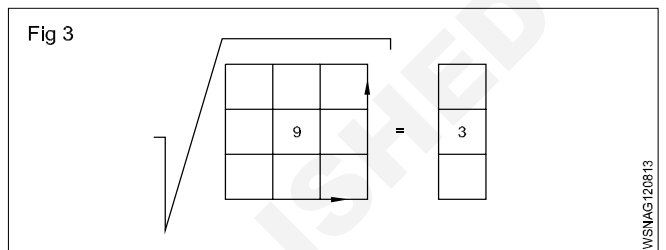
If there is a remainder, repeat the procedure.

```
              68
   6  │  46,24
      │    36
  128 │  1024
      │  1024
      │     0
```

$\sqrt{4624} = 68$

Basic number x basic number = Square

$\sqrt{\text{Square number}}$ = **basic number**

Example

The cross-section of a rivet is 3.46 cm^2. Calculate the diameter of the hole.

Fig 4
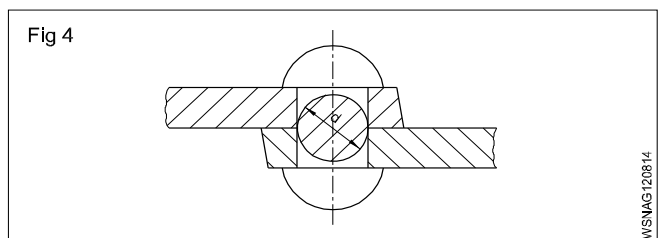
Rivet cross-section is the hole cross-section.

To find 'd',

Given that Area = 3.46 cm^2

Area = 0.785 x d^2 (formula)

3.46 cm^2 = d^2 x 0.785

$d^2 = \dfrac{3.46 \text{ cm}^2}{0.785}$

$d = \sqrt{\dfrac{3.46}{0.785}}$ cm

$d = 2.1 \text{ cm (or) } 21 \text{ mm}$

Square root, Ratio and Proportions, Percentage - Simple problems using calculator
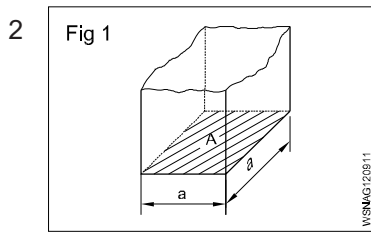
1 a $\sqrt{2916}$ = ——————.
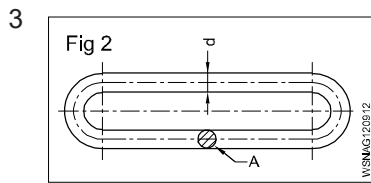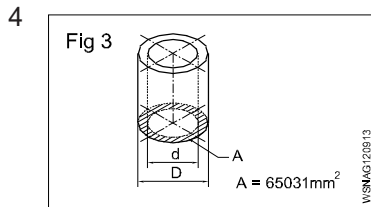
   b $\sqrt{45796}$ = ——————.

   c $\sqrt{8.2944}$ = ——————.

   d $\sqrt{63.845}$ = ——————.

2 Fig 1

A = 2025 mm²
a = ——————mm

3 Fig 2

A = 176.715 mm²
d = ——————mm

4 Fig 3

A = 65031 mm²
d = 140 mm
D = ——————mm
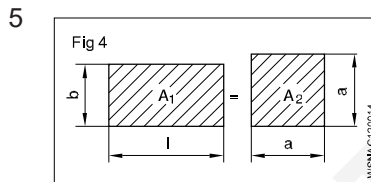
A = 65031mm²

5 Fig 4

l = 58 cm
b = 45 cm
A₁ = A₂
a = ——————cm

6 Fig 5

d=140mm A=807,77 sq.cm

A = 807.77 cm²
d = 140 mm
D = ——————mm

7 Fig 6

a x a = 543169 mm²
a = ——————mm

8 Fig 7

d : l = 1:1.5
A = 73.5 mm²
d = ——————mm

9 Fig 8

A₂-A₁ - ΔA = 12.7% OF A₁
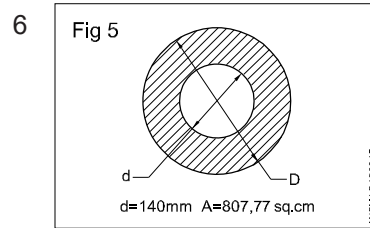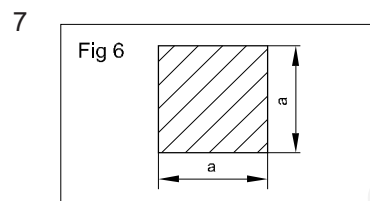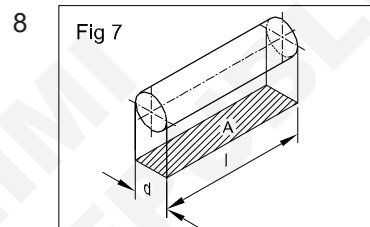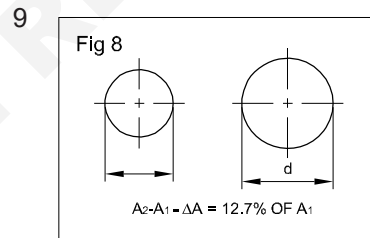
increase in area
A = 12.7%
A = 360 mm²
d = ——————mm
(d = diameter after the increase in area)

Square root, Ratio and Proportions, Percentage - Applications of pythagoras theorem and related problems

Applications of Pythagoras Theorem

Some of the applications of the Pythagoras theorem are; (Fig 1)

Fig 1
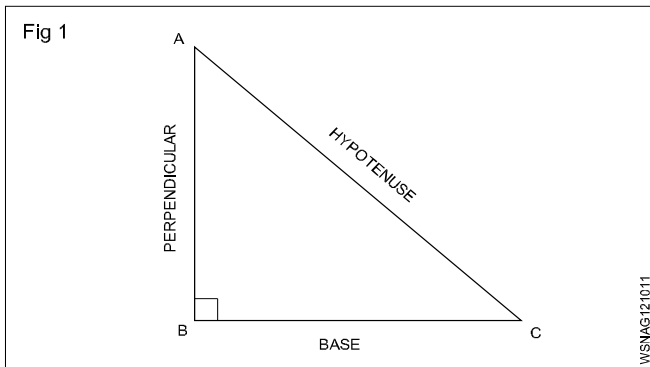
1 The Pythagoras theorem is commonly used to find the lengths of sides of a right-angled triangle.

2 It is used to find the length of the diagonal of a square.

3 Pythagoras theorem is used in trigonometry to find the trigonometric ratios like sin, cos, tan, cosec, sec and cot.

4 Pythagoras theorem is used in security cameras for face recognition.

5 Architects use the technique of the Pythagoras theorem for engineering and construction fields.

6 The Pythagoras theorem is applied in surveying the mountains.

7 It is also used in navigation to find the shortest route.

8 By using the Pythagoras theorem, we can derive the formula for base, perpendicular and hypotenuse.

9 Painters use ladders to paint on high buildings with the help of the Pythagoras theorem.

10 Pythagoras theorem is used to calculate the steepness of slopes of hills or mountains.

11 The converse of the Pythagoras theorem is used to check whether a triangle is a right triangle or not.

Application of pythagoras theorem in real life

Pythagoras theorem states that

"In a right-angled triangle, the square of the hypotenuse side is equal to the sum of squares of the other two sides".

1 The sides of this triangle have been named Perpendicular, Base and Hypotenuse.

2 The hypotenuse is the longest side, as it is opposite to the angle 90°.

3 The sides of a right triangle (say AB, BC and CA) which have positive integer values, when squared, are put into an equation, also called a Pythagorean triplet.

4 To calculate the length of staircase required to reach a window

5 To find the length of the longest item can be kept in your room.

6 To find the steepness of the hills or mountains.

7 To find the original height of a tree broken due to heavy rain and lying on itself

8 To determine heights and measurements in the construction sites.

Examples

1 What is the side AC if AB = 15 cm, BC = 25 cm.

$$AC^2 = AB^2 + BC^2$$
$$= 15^2 + 25^2$$
$$= 225 + 625 = 850$$
$$AC = \sqrt{850} = 29.155 \text{ cm}$$
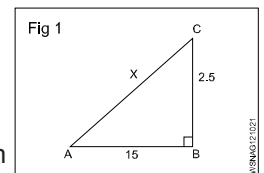
2 What is the side BC if AB = 10 cm, AC = 30 cm.

$$AC^2 = AB^2 + BC^2$$
$$30^2 = 10^2 + BC^2$$
$$900 = 100 + BC^2$$
$$BC^2 = 900 - 100 = 800$$
$$BC = 28.284 \text{ cm}$$
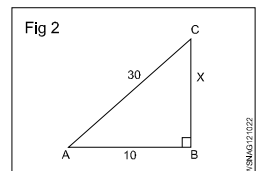
3 What is the side AB if BC = 20 cm, AC = 35 cm.

$$AC^2 = AB^2 + BC^2$$
$$35^2 = AB^2 + 20^2$$
$$1225 = AB + 400$$
$$AB^2 = 1225 - 400 = 825$$
$$AB = 28.72 \text{ cm}$$
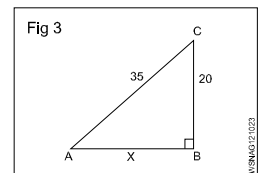
4 What is the value of side BC if AB = 8 cm, AC = 24 cm.

$$AC^2 = AB^2 + BC^2$$
$$24^2 = 8^2 + BC^2$$
$$576 = 64 + BC^2$$
$$BC^2 = 576 - 64 = 512$$
$$BC = \sqrt{572} = 22.63 \text{ cm}$$
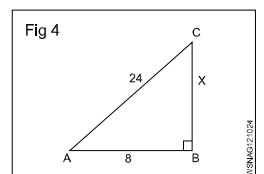
5   What is the value side AC if AB = 6.45 cm, BC = 8.52 cm.

$AC^2 = AB^2 + BC^2$

$AC^2 = 6.45^2 + 8.52^2$

$AC^2 = 41.60 + 72.59$

$\quad\;\; = 114.19$

$AC = \sqrt{114.19}$ = 10.69 cm

Fig 5
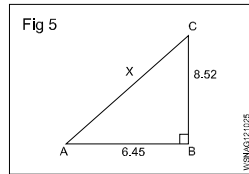
6   What is the value of side AB if BC = 3.26 cm, AC = 8.24 cm.

$AC^2 = AB^2 + BC^2$

$8.24^2 = AB^2 + 3.26^2$

$67.9 = AB + 10.63$

$AB^2 = 67.9 - 10.63$

$\quad\;\; = 57.27$

$AB = \sqrt{57.27}$ = 7.57 cm

Fig 6
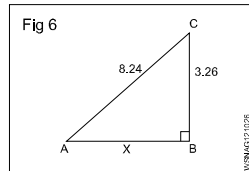
7   What is the value of side AB if AC = 12.5 cm, BC = 8.5 cm.

$AC^2 \quad = AB^2 + BC^2$

$12.5^2 \quad = AB^2 + 8.5^2$

$156.25 = AB + 72.25$

$AB^2 \quad = 156.25 - 72.25$

$\quad\quad\;\; = 84$

$AB \quad = \sqrt{84}$ = 9.17 cm

Fig 7
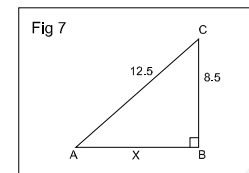
8   A ladder of 12.5 metre long is placed with upper end against a wall. The lower end being 7.5 metres from the wall. What height is the upper end above the ground.

$AC^2 \quad = AB^2 + BC^2$

$BC^2 \quad = AC^2 - AB^2$

$BC^2 \quad = x^2$

$AC^2 \quad = AB^2 + BC^2$

$12.5^2 \quad = x^2 + 7.5^2$
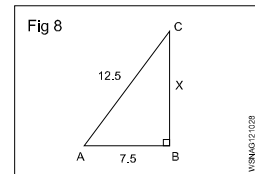
$x^2 \quad = (12.5)^2 - (7.5)^2$

$\quad\quad\; = (12.5 + 7.5)(12.5 - 7.5)^2$

$\quad\quad\; = 20 \times 5$

$\quad\quad\; = \sqrt{100}$ = 10

$x \quad = 10$ m


Fig 8

9   What is the value of AB.

$AC^2 \quad = AB^2 + BC^2$

$AB^2 \quad = AC^2 - BC^2$

$AB^2 \quad = x^2$

$AC^2 \quad = AB^2 + BC^2$

$10^2 \quad = x^2 + 6^2$

$x^2 \quad = 10^2 - 6^2$

$\quad\quad\; = 100 - 36 = 64$

$x \quad = \sqrt{64}$

$\quad\quad\; = 8$

$AB \quad = 8$

Fig 9
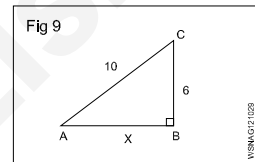
Assignment

1   What is the value of side AB, in a right angled triangle of side AC = 10 cm and BC = 5 cm.

2   What is the value of side AC, in a right angled triangle of side AB = 6.5 cm and BC = 4.5 cm.

3   What is the value of side BC, in a right angled triangle of side AC = 14.5 cm and AB = 10.5 cm.

4   What is the value of side AC, in a right angled triangle of side AB = 7 cm and BC = 5 cm.

5   What is the value of side BC, in a right angled triangle of side AC = 13.25 cm and AB = 8.75 cm.

Square root, Ratio and Proportions, Percentage - Ratio and proportion

Ratio

Introduction

It is the relation between two quantities of the same kind and is expressed as a fraction.

Expression

a, b two quantities of the same kind. $\frac{a}{b}$ or a:b or a ÷ b or

a in b is the ratio.

Ratio is always reduced to the lowest terms.

Example

$$7:14 = \frac{7}{14} = \frac{1}{2} = 1:2$$

Proportion

It is the equality between the ratios, a : b is a ratio and c : d is another ratio. Both ratios are equal. Then

a :b :: c : d or $\frac{a}{b} = \frac{c}{d}$

Example

250 : 2000 :: 1 : 8

Proportion fundamentals

If $\frac{a}{b} = \frac{c}{d}$ then

- ad = bc

- $\frac{a}{c} = \frac{b}{d}$

- $\frac{b}{a} = \frac{d}{c}$

- $\frac{a+b}{b} = \frac{c+d}{c}$ and $\frac{a+b}{a} = \frac{c+d}{c}$

- $\frac{a-b}{b} = \frac{c-d}{d}$

- $\frac{a+b}{b+d} = \frac{a}{c} = \frac{c}{d}$

  3:4::6:8 or $\frac{3}{4} = \frac{6}{8}$

- 3 x 8 = 6 x 4

- $\frac{3}{6} = \frac{4}{8}$

- $\frac{4}{3} = \frac{8}{6}$

- $\frac{3+4}{4} = \frac{6+8}{8}$

- $\frac{3-4}{4} = \frac{6-8}{8}$

- $\frac{3+6}{4+8} = \frac{9}{12} = \frac{3}{4}$

**Ratio - relation of two quantities of the same kind.
Proportion - equality between two ratios.**

Example

- A steel plate of 800 x 1400 mm is to be drawn to a scale of 1:20. What will be the lengths in the Fig 1.

Fig 1
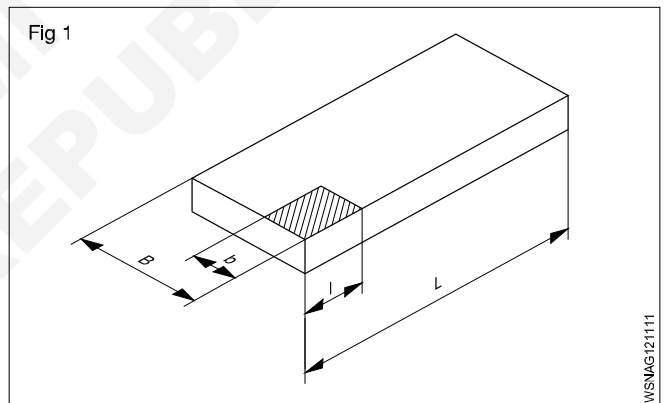
The reduction ratio is $\frac{1}{20}$.

B is reduced from 800 to 800 x $\frac{1}{20}$ = 40 mm.

L is reduced from 1400 x $\frac{1}{20}$ = 70 mm.

- Find the number of teeth of the larger gear in the gear transmission shown in the Fig 2.

Fig 2
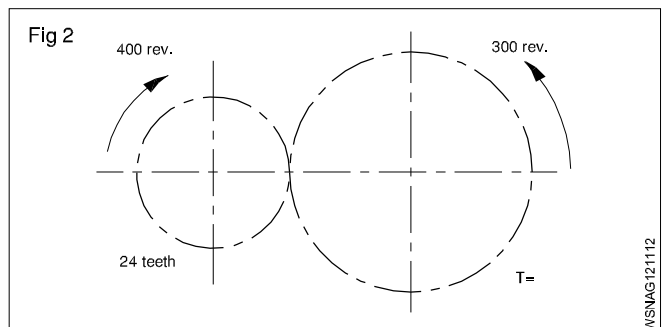
Speed ratio = 400 : 300

Teeth ratio = 24 : T

$$\frac{400}{300} = \frac{T}{24}$$

$$\therefore T = \frac{24 \times 400}{300} = 32 \, \text{Teeth}$$

Find the ratio of A:B:C

If A:B= 2:3 and B:C=4:5

A:B = 2:3

B:C = 4:5

A:B = 8 :12 (Ratio 2:3 multiply by 4)

B:C = 12:15 (Ratio 4:5 multiply by 3)

∴ A:B:C = 8:12:15

Assignment

1

Fig 1
L = 2.75metre
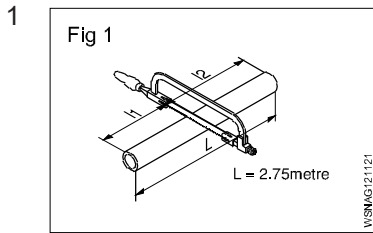
$l_1 : l_2$ = 2:3

L = 2.75 metres

l_1 =_____ metres

l_2 =_____ metres

5

Fig 5
D : d = 1.75 : 1
35

D : d = 1.75: 1

D = 35 mm

d = _____ mm

2

Fig 2
d : L = 2 :7
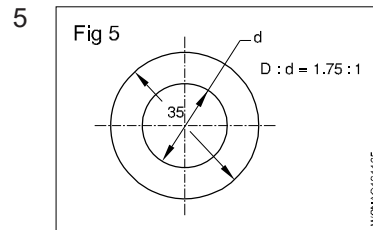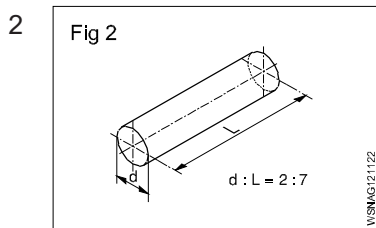
d: L of shaft = 2:7

d = 40 mm

L = _____ mm

6

Fig 6
a:s = 5:1
1.5

a:s = 5:1

s = 1.5mm

a =_____ mm

3

Fig 3
10
L
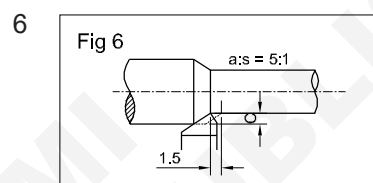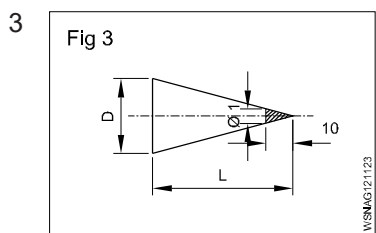
D : L=1:10

L=150mm

D=_____ mm

7 A:B=9:12

B:C=8:10

Then A:B:C=_____

8 A:B=5:6

B:C=3:4

Then A:B:C= _____

4

Fig 4
20
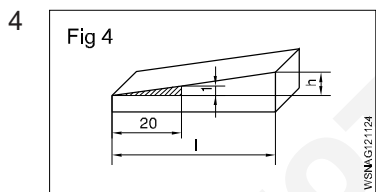
$$\frac{\Delta h}{l} = \frac{1}{20}$$

l = 140 mm

Δh = _____ mm

9 A:55=9:11

A = _____

10 15:9.3=40:x

x = _____

Square root, Ratio and Proportions, Percentage - Ratio and proportion - Direct and indirect proportions

Proportion

Description

It is the equality between the ratios, a:b is a ratio and c:d is another ratio. Both ratios are equal. Then

a : b::c : d or   e.g. 250 : 2000::1 : 8

Rule of three

A three step calculation

statement

single

multiple.

Direct proportion

The more in one the more in the other - An increase in one denomination produces an increase in the other. (Fig 1)

Fig 1
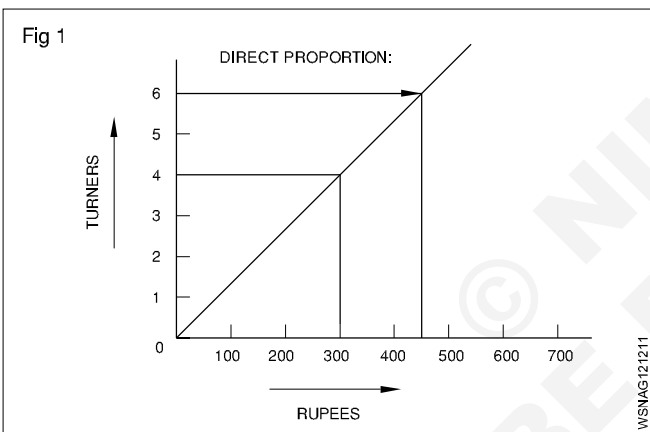
Examples

1   4 turners earn 300 Rupees. How much will 6 Turners earn?

Statement

4 turners = 300 Rupees

Single

1 Turner = 75 Rupees

Multiple

6 Turners = 6 x 75 = 450 Rupees

2   One vehicle consumes 30 litres of petrol per day how much petrol is used by 6 Vehicles operating under similar condition.

One vehicle uses petrol   = 30 litres per day.

Then six vehicles will use = 6 Times as much

= 6 x 30 = 180 litres/day.

3   4 vehicles consumes 120 gallons of petrol per day how much petrol will be used by 12 vehicles operating under the same condition.

4 vehicles use 120 gallons per day

1 Vehicle will use $\dfrac{120}{4}$ = 30 gallons/day

12 vehicles will use 12 x 30 = 360 gallons/day

> **Both examples are called simple proportion because only two quantities were used and the day is common for both ratios.**

4   If 2 litres of petrol costs Rs 60. Find the cost of 50 litres.

Quantity of Petrol	Cost of Petrol
2 litres	Rs.60
50 litres	x

1 litre petrol $= \dfrac{60}{2}$ = Rs.30

50 litres petrol   = 30 x 50 = Rs 1500

5   A 150mm dia gear meshes with 50mm dia gear. If the larger gear has 30 teeth. How many teeth will have the smaller gear have?

Gear dia	No. of Teeth
150 mm	30
50 mm	x

$x = \dfrac{50}{150}$ x 30 = 10 teeth.

6   A mechanic assembles 7 machines in 2½ days. How long will it take time to assemble 70 machines at the same rate.

Machines	Days
7	2½
70	x

$x = \dfrac{70 \times 2.5}{7}$ = 25 days

Assemble for 70 machines will take 25 days.

7   A roll of wire weighs 1.24 kg from this roll a piece of 3.7cm long is cut and it is found to weigh 2.93 gm. What is the length of the wire in the roll?

Weight of wire	Length of wire
2.93 gm	3.7 cm
1.24 kg (1240 gm)	x

$$x = \frac{1240}{2.93} \times 3.7 = 1566 \text{ cm}$$

Length of wire = 1566 cm.

Indirect or inverse proportion

The more in one the lesser other - Increase in one quantity will produce a decrease in the other. (Fig 2)

Fig 2
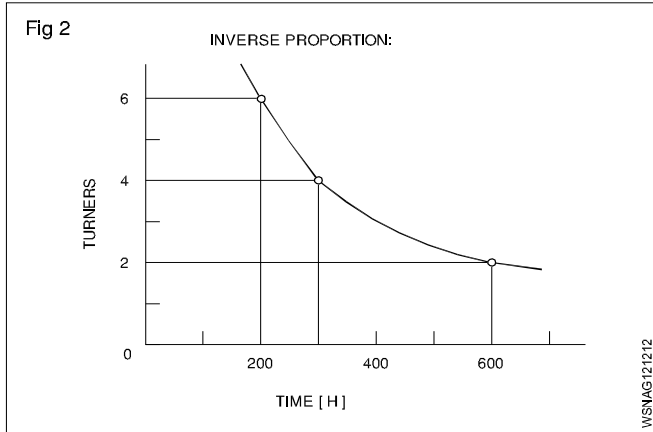
Example

1 4 turners finish a job in 300 hours. How much time will 6 turners take to do the same job?

Solution procedure in three steps:

Statement   4 turners taken = 300 hours

The time will reduce if 6 turners to do the same job. Therefore this is inverse proportion.

Multiple fraction $\dfrac{4 \text{ Turners}}{6 \text{ Turners}} \times 300$ hours

6 Turners   = 200 hours

Result - The more the less.

2 8 workman take 6 days to complete a job. How many days it will take for 4 workman to complete the same job?

Workman	Days
8	6
4	x

$$x = \frac{8}{4} \times 6 = 12 \text{ days}$$

4 workers complete the work = 12 days.

3 5 men working on a job finished it in 32 days. Find out in how many days 8 men will finish the same job?

Men	Days
5	32
8	x

$$x = \frac{5 \times 32}{8} = 4 \times 5 = 20 \text{ days}$$

8 men will complete the job = 20 days.

4 An engine running at 150 rpm drives a shaft by pulley diameter is 55cm and that of the driven shaft pulley is 33 cm. Find the speed of the shaft?

Dia of pulley	Rpm of shaft
55 cm	150
33 cm	x

$$x = \frac{55 \times 150}{33} = 250 \text{ rpm.}$$

Speed of the 33cm diameter will run 250 rpm.

5 A pulley of 80 cm diameter is rotating at 100 rpm and drives another pulley of 40 cm diameter. Find the rpm of driven pulley. If slip is 2.5% find the rpm?

Dia of pulley	Rpm of pulley
80 cm	100
40 cm	x

40 cm diameter = 200 rpm.

Slip is 2.5%   = 195 rpm.

Problems involving both

Example

2 turners need 3 days to produce 20 pieces. How long will it take for 6 turners to produce 30 such pieces?

Statement

   2 turners, 20 pieces = 3 days

   6 turners, 30 pieces = how many days.

First step (Fig 3)

Statement   2 turners for 20 pieces = 3 days

              1 turner for 20 pieces = 3 x 2 = 6 days

Multiple 6 turners for 20 pieces = $\dfrac{6}{6}$ = 1 day

Statement   6 turners for 20 pieces = 1 day

Single   6 turners for 1 piece   = $\dfrac{1}{20}$ days

Multiple   6 turners for 30 pieces = $\dfrac{1}{20} \times 30 = 1.5$ days

Inverse proportion - More the less.

Fig 3
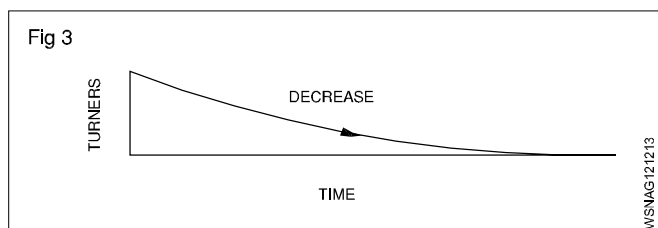
Second step (Fig 4)

Fig 4
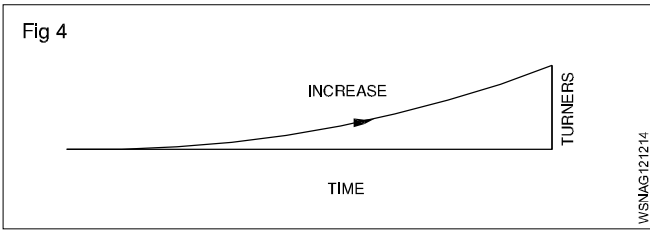
Direct proportion - More the more.

Solve the problem by first writing the statement and proceed to single and then to the multiple according to the type of proportion that is involved.

Introduction

Proportional fundamentals, as applicable to motor vehicle calculations are discussed below.

Simple Proportion

• Proportion

This is an equality between two ratios

Compound and Inverse proportions

• Compound proportions

Example

5 Fitter take 21 days to complete overhauling of 6 vehicles how long 7 Fitters will take to over haul 8 vehicles (Assume time of overhauling each vehicle is constant)

In this both direct and indirect proportions are used.

• 1 Fitter will overhauling 1 vehicle in days (shorter time).

• Quantities (No. of days) are taken in last as that is the answer required in this case.

Fitters	Vehicle	Days
5	6	21
7	8	x

$$\left(\frac{21 \times 5}{6 \times 7} \times 8\right) = 20 \text{ days}$$

Ans: 7 Fitters will overhaul 8 vehicles in 20 days.

Inverse proportion

Some times proportions are taken inversely.

Examples

• If one water pump fills the fuel tank in 12 minutes, two pumps will take half the time taken.

The time should not be doubled.

• 2 pumps will take 30 minutes to fill up a tank how long will 6 similar pumps take this to fill this tank.

Pump	Time
2	30
6	x

Ans: Time taken by 6 pumps = $\frac{30 \times 2}{6} = 10$ minutes

Assignment

1

Fig 1
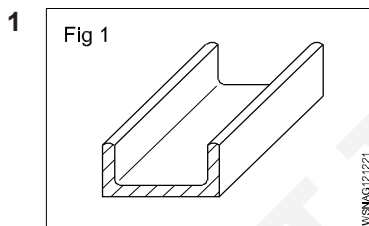
Length = 6.1 metre

Weight = 32 kgf

Weight of 1 metre of the same channel = _____ kgf

2

Fig 2
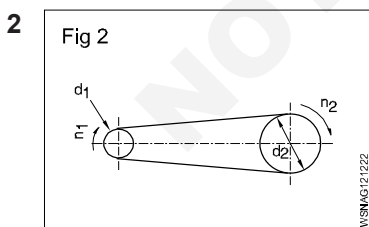
d_1 = 120 mm

d_2 = 720 mm

n_1 = 1200 rpm

n_2 = _____ rpm

3

Fig 3
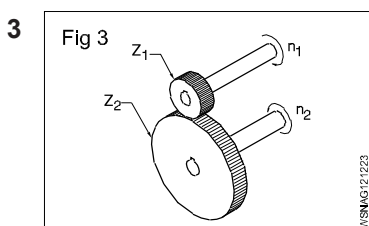
Z_1 = 42 T

n_2 = 96 rpm

n_1 = 224 rpm

Z_2 = _____ T

4

Fig 4
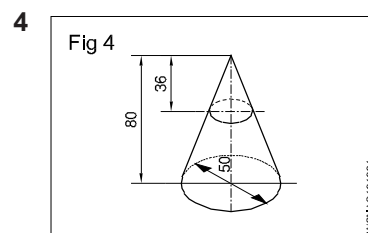
D = 50 mm

H = 80 mm

h = 36 mm

d = _____ mm

5 If a mechanic assembles 8 machines in 3 days, how long he will take to assemble 60 machines.

6 In an auto shop the grinding wheel makes 1000 rpm and the driven pulley is 200 mm dia. If the driving pulley is 150 mm dia. Find out the rpm of the driving pulley.

7 In a gearing of a vehicle the following facts are found.

A 180 mm dia of gear meshes with 60mm dia gear. If the bigger gear makes 60 rpm. What will be the rpm of smaller gear.

8 A vehicular job is completed by 5 mechanics in 4 days. If only 3 mechanics are available, in how many days the work can be completed.

Square root, Ratio and Proportions, Percentage - Percentage

Percentage

Percentage is a kind of fraction whose denominator is always 100. The symbol for percent is %, written after the number. e.g. 16%.

Ex. $\dfrac{16}{100} = 0.16$

In decimal form, it is 0.16. Percentage calculation also involves rule of three. The statement (the given data), for unit, and then to multiple which is for calculating the answer. (Fig 1)

Fig 1

25 BOX = 100%
4 BOX = ?
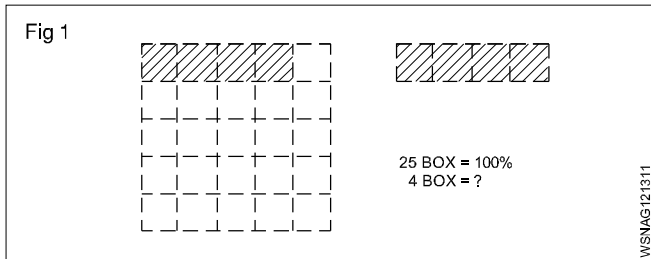
Example

The amount of total raw sheet metal to make a door was 3.6 metre² and wastage was 0.18 metre². Calculate the % of wastage. (Fig 2)

Fig 2
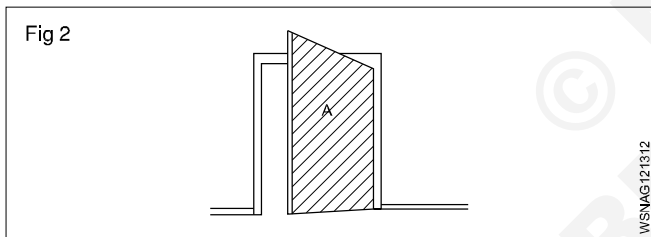
Solution procedure in three steps.

Statement:

Area of door (A) = 3.6 m² = 100 %.

Wastage = 0.18 m²

Single: $\dfrac{100}{3.6}$ x 1 m²

Multiple: for 0.18 m² = $\dfrac{100}{3.6}$ x 0.18.

Wastage   = 5%.

> **Analyse the given data and proceed to arrive at the answer through the unit.**

Example

A fitter receives a take-home salary of 984.50 rupees.

If the deduction amounts to 24%, what is his total salary? (Fig 3)

Fig 3

GROSS - DEDUCTIONS = NET
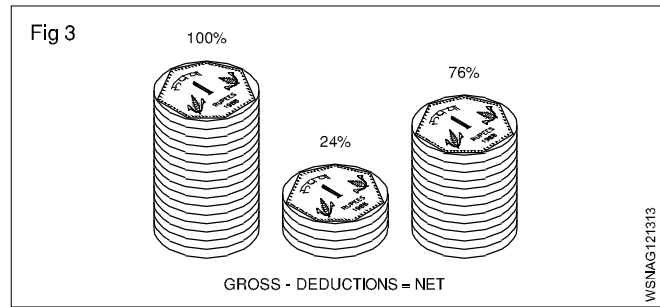
Total pay 100%

Deduction 24%

Take home salary 76%

If the take home pay is Rs.76, his salary is 100.

For 1% it is $\dfrac{1}{76}$

For Rs.984.50, it is $\dfrac{1}{76}$ x 984.50.

For 100% it is $\dfrac{984.50}{76}$ X 100 = 1295.39

100% i.e. gross pay = Rs.1295.40.

Example 1

75 litres of oil is taken out from a oil barrel of 200 litres capacity. Find out the percentage taken in this.

Solution

% of oil taken = Oil taken out (litres) / Capacity of Barrel (litres) x 100

$= \dfrac{75}{200}$ x 100 = $37\frac{1}{2}$ %

Example 2

A spare part is sold with 15%. Profit to a customer, to a price of Rs.15000/-. Find out the following (a) What is the purchase price (b) What is the profit.

Solution: CP = x ,

CP = cost price

SP = sale price

SP = CP + 15% of CP

$15000 = x + \dfrac{15\,x}{100} = \dfrac{100\,x + 15\,x}{100}$

$x = \dfrac{1500000}{115} = 13043.47$

Profit = SP - CP = 15000 - 13043.47 = 1956.53

Purchase price = Rs.13,043/, Profit = Rs. 1957

Example 3

Out of 80000 cars, which were tested on road, only 16000 cars had no fault. What is the percentage in this acceptance.

$$= \frac{160000}{80000} \times 100 = \frac{100}{5} = 20\%$$

Example 4

The price of a motor cycle dropped to 92% of original price and now sold at Rs.18000/- What was the original price.

Solution

Present price of Motor cycle Rs.18000

This is the value of 92% of original price

Original Price $= 18000 \times \frac{100}{92} = \frac{1800000}{92}$

$= Rs.19565$

Example 5

A Motor vehicle uses 100 litres of Petrol per day when travelling at 30 kmph. After top overhauling the consumption falls to 90 litres per day. Calculate percentage of saving.

Solution
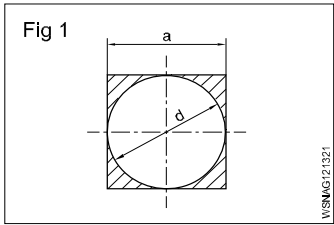
Percentage of saving = Decrease in consumption/Original consumption x 100
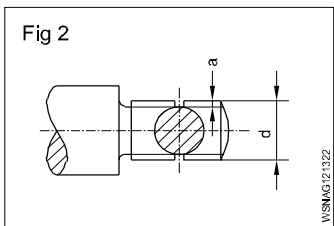
$= (100 - 90) \frac{litres}{100} \times 100$
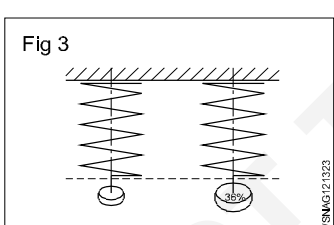
$= \frac{10}{100} \times 100$
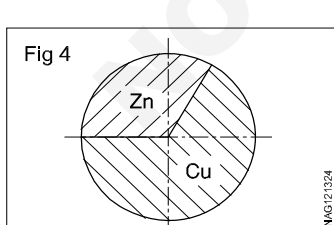
= 10% Saving in fuel.

Assignment

1.

Fig 1
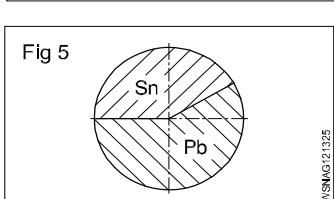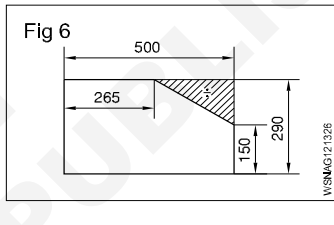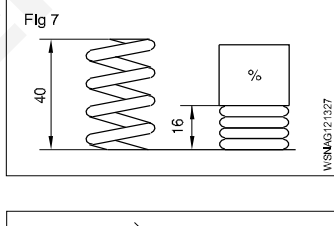
a = 400mm (side of square)

d = 400 mm

Wastage = _____ %.

2.

Fig 2
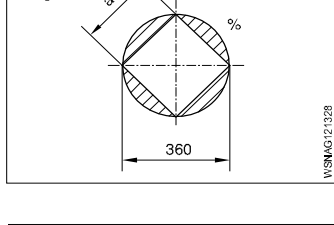
d = 26mm

'a' depth of u/cut = 2.4mm

reduction of area at cross-section = _____ %

3.

Fig 3
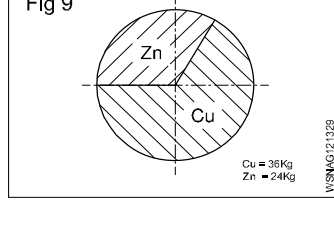
Percentage of increase = 36%

Value of increase = 611.2 N/mm²

Original tensile strength = _____ N/mm².

4.

Fig 4
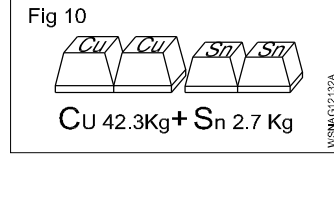
Copper in alloy = 27 kg

Zinc in alloy = 18 kg

% of Copper = _____ %

% of Zinc = _____ %.

5.

Fig 5

Weight of alloy = 140 Kgf

Weight of Sn 40%

Pb = _____ Kgf

Sn = _____ Kgf.

6.

Fig 6

Shaded portion = _____ %.

7.

Fig 7

Compression length = _____ %.

8.

Fig 8

d = 360 mm

a = 0.707 x d

Wastage = _____ %.

9.

Fig 9

Cu = 36 Kg

Zn = 24 Kg

Cu = _____ %

Zn = _____ %

10.

Fig 10

Cu = 42.3 Kg

Sn = 2.7 Kg

Cu _____ %

Sn = _____ %.

Square root, Ratio and Proportions, Percentage - Changing percentage to decimal amd fraction

Conversion of Fraction into Percentage

1 Convert $\dfrac{1}{2}$ into percentage.

Solution: $\dfrac{1}{2}$ x 100

= 50%

2 Convert $\dfrac{1}{11}$ into percentage

Solution: $\dfrac{1}{11}$ x 100 = $\dfrac{100}{11}$

= 9.01%

Convert the following fraction into percentage.

1 $\dfrac{1}{4}$

2 $\dfrac{1}{5}$

3 $\dfrac{2}{3}$

4 $\dfrac{3}{8}$

Conversion of Percentage into Fraction

1 Convert 24% into fraction.

Solution: $\dfrac{24}{100}$ = $\dfrac{6}{25}$

2 Convert $33\dfrac{1}{3}$% into fraction.

Solution: $\dfrac{33\dfrac{1}{3}}{100}$ = $\dfrac{\dfrac{100}{3}}{100}$ = $\dfrac{100}{3}\times\dfrac{1}{100}$

= $\dfrac{1}{3}$

Convert the following percentage into fraction

1 15%

2 $87\dfrac{1}{2}$%

3 80%

4 12.5%

Conversion of Decimal Fraction into Percentage

1 Convert 0.35 into percentage.

Solution: 0.35 x 100

= 35%

2 Convert 0.375 into percentage.

Solution: 0.375 x 100

= 37.5%

Convert the following Decimal Fraction into Percentage

1 0.2

2 0.004

3 0.875

4 0.052

Conversion of Percentage into Decimal fraction

1 Convert 30% into decimal fraction.

Solution: $\dfrac{30}{100}$ = 0.3

2 Convert $33\dfrac{1}{3}$% into decimal fraction.

Solution: $\dfrac{33\dfrac{1}{3}}{100}$ = $\dfrac{\dfrac{100}{3}}{100}$ = $\dfrac{100}{3}\times\dfrac{1}{100}$

= $\dfrac{1}{3}$ = 0.333

Convert the following percentage into decimal fraction

1 15%

2 7%

3 $12\dfrac{1}{2}$%

4 90%

Material science - Types of metal, types of ferrous and non ferrous metals

Types of metals

The metals is of two types:

1 Ferrous metal   2   Non-ferrous metal

1   Ferrous metals : The metals that contains major part of iron and contain carbon are called ferrous metals such as pig iron, mild steel, nickel etc., they have iron properties such as rusting, magnetisations etc.

2   Non-ferrous metals : The metals that do not contains iron or carbon and do not have the property of iron are called non-ferrous metals such as copper, aluminum etc.

Ferrous and Non ferrous alloys

Alloying metals and ferrous alloys

An alloy is formed by mixing two or more metals together by melting.

For ferrous metals and alloys, iron is the main constituent metal. Depending on the type and percentage of the alloying metal added, the property of the alloy steel will vary.

Metals commonly used for making alloy steels

Nickel (Ni)

This is a hard metal and is resistant to many types of corrosion rust.

It is used in industrial applications like nickel, cadmium batteries, boiler tubes, valves of internal combustion engines, engine spark plugs etc. The melting point of nickel is 1450°C. Nickel can be magnetised. In the manufacture of permanent magnets a special nickel steel alloy is used. Nickel is also used for electroplating. Invar steel contains about 36% nickel. It is tough and corrosion resistant. Precision instruments are made of Invar steel because it has the least coefficient of expansion.

Nickel-steel alloys are available containing nickel from 2% to 50%.

Chromium (Cr)

Chromium, when added to steel, improves the corrosion resistance, toughness and hardenability of steel. Chromium steels are available which may contain chromium up to 30%.

Chromium, nickel, tungsten and molybdenum are alloyed for making automobile components and cutting tools.

Chromium is also used for electroplating components. Cylinder liners are chrome-plated inside so as to have wear resistance properties. Stainless steel contains about 13% chromium. Chromium-nickel steel is used for bearings. Chrome-vanadium steel is used for making hand tools like spanners and wrenches.

Manganese (Mn)

Addition of manganese to steel increases hardness and strength but decreases the cooling rate.

Manganese steel can be used to harden the outer surface for providing a wear resisting surface with a tough core. Manganese steel containing about 14% manganese is used for making agricultural equipment like ploughs and blades.

Silicon (Si)

Addition of silicon for alloying with steel improves resistance to high temperature oxidation.

This also improves elasticity, and resistance against corrosion. Silicon alloyed steels are used in manufacturing springs and certain types of steel, due to its resistance to corrosion. Cast iron contains silicon about 2.5%. It helps in the formation of free graphite which promotes the machinability of cast iron.

Tungsten (W)

The melting temperature of tungsten is 3380° C. This can be drawn into thin wires.

Due to this reason it is used to make filaments of electric lamps.

Tungsten is used as an alloying metal for the production of high speed cutting tools. High speed steel is an alloy of 18% tungsten, 4% chromium and 1% vanadium.

Stellite is an alloy of 30% chromium, 20% tungsten, 1 to 4% carbon and the balance cobalt.

Vanadium (Va)

This improves the toughness of steel. Vanadium steel is used in the manufacture of gears, tools etc. Vanadium helps in providing a fine grain structure in tool steels.

Chrome-vanadium steel contains 0.5% to 1.5% chromium, 0.15% to 0.3% vanadium, 0.13% to 1.10% carbon.

This alloy has high tensile strength, elastic limit and ductility. It is used in the manufacture of springs, gears, shafts and drop forged components.

Vanadium high speed steel contains 0.70% carbon and about 10% vanadium. This is considered as a superior high speed steel.

Cobalt (Co)

The melting point of cobalt is 1495°C. This can retain magnetic properties and wear- resistance at very high temperatures. Cobalt is used in the manufacture of magnets, ball bearings, cutting tools etc.   Cobalt high speed steel (sometimes known as super H.S.S.) contains about 5 to 8% cobalt. This has better hardness and wear resistance properties than the 18% tungsten H.S.S.

Molybdenum (Mo)

The melting point of molybdenum is 2620°C. This gives high resistance against softening when heated. Molybdenum high speed steel contains 6% of molybdenum, 6% tungsten, 4% chromium and 2% vanadium. This high speed steel is very tough and has good cutting ability.

Cadmium (cd)

The melting point of cadmium is 320°C. This is used for coating steel components.

Alloying Metals and Non Ferrous Alloys

Non-ferrous Metals And Alloys

Copper and its alloys

Metals without iron are called non-ferrous metals. Eg. Copper, Aluminium, Zinc, Lead and Tin.

Copper

This is extracted from its ores 'MALACHITE' which contains about 55% copper and 'PYRITES' which contains about 32% copper.

Properties

Reddish in colour. Copper is easily distinguishable because of its colour.

The structure when fractured is granular, but when forged or rolled it is fibrous.

It is very malleable and ductile and can be made into sheets or wires.

It is a good conductor of electricity. Copper is extensively used as electrical cables and parts of electrical apparatus which conduct electric current.

Copper is a good conductor of heat and also highly resistant to corrosion. For this reason it is used for boiler fire boxes, water heating apparatus, water pipes and vessels in brewery and chemical plants. Also used for making soldering iron.

The melting temperature of copper is 1083° C.

The tensile strength of copper can be increased by hammering or rolling.

Copper Alloys

Brass

It is an alloy of copper and zinc. For certain types of brass small quantities of tin or lead are added. The colour of brass depends on the percentage of the alloying elements. The colour is yellow or light yellow, or nearly white. It can be easily machined. Brass is also corrosion-resistant.

Brass is widely used for making motor car radiator core and water taps etc. It is also used in gas welding for hard soldering/brazing. The melting point of brass ranges from 880 to 930°C.

Brasses of different composition are made for various applications.

Bronze

Bronze is basically an alloy of copper and tin. Sometimes zinc is also added for achieving certain special properties. Its colour ranges from red to yellow. The melting point of bronze is about 1005°C. It is harder than brass. It can be easily machined with sharp tools. The chip produced is granular. Special bronze alloys are used as brazing rods.

Bronze of different compositions are available for various applications.

Lead and its alloys

Lead is a very commonly used non-ferrous metal and has a variety of industrial applications.

Lead is produced from its ore 'GALENA'. Lead is a heavy metal that is silvery in colour when molten. It is soft and malleable and has good resistance to corrosion. It is a good insulator against nuclear radiation. Lead is resistant to many acids like sulphuric acid and hydrochloric acid.

It is used in car batteries, in the preparation of solders etc. It is also used in the preparation of paints.

Lead Alloys

Babbitt metal

Babbitt metal is an alloy of lead, tin, copper and antimony. It is a soft, anti-friction alloy, often used as bearings.

An alloy of lead and tin is used as 'soft solder'.

Zinc and its alloys

Zinc is a commonly used metal for coating on steel to prevent corrosion. Examples are steel buckets, galvanized roofing sheets, etc.

Zinc is obtained from the ore-calamine or blende.

Its melting point is 420° C.

It is brittle and softens on heating; it is also corrosion-resistant. Due to this reason it is used for battery containers and is coated on roofing sheets etc.

Galvanized iron sheets are coated with zinc.

Tin and tin alloys

Tin

Tin is produced from cassiterite or tinstone. It is silvery white in appearance, and the melting point is 231° C. It is soft and highly corrosion-resistant.

It is mainly used as a coating on steel sheets for the production of food containers. It is also used with other metals, to form alloys.

Example: Tin with copper to form bronze. Tin with lead to form solder. Tin with copper, lead and antimony to form Babbitt metal.

Aluminium

Aluminium is a non-ferrous metal which is extracted from 'BAUXITE'. Aluminium is white or whitish grey in colour. It has a melting point of 660° C. Aluminium has high electrical and thermal conductivity. It is soft and ductile, and has low tensile strength. Aluminium is very widely used in aircraft industry and fabrication work because of its lightness. Its application in the electrical industry is also on the increase. It is also very much in use in household heating appliances.

Material science - Physical and mechanical properties of metals

Metal:

Metal is a mineral used in all types of engineering works such as machineries, bridges, aero planes etc., so we must have basic knowledge about the metals.

Understanding the physical and mechanical properties of metals has become increasingly important for a machinist since he has to make various components to meet the designed service requirements against factors, such as the raise of temperature, tensile, compressive and impact loads etc. A knowledge of different properties of materials will help him to do his job successfully. If proper material/metal is not used it may cause fracture or other forms of failures, and endanger the life of the component when it is put into function.

Fig 1 shows the way in which the metals get deformed when acted upon by the same load.

Note the difference in the amount of deformation.

Fig 1
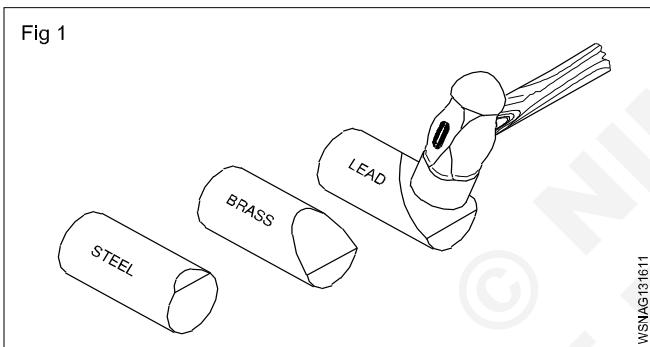
Physical properties of metals

- Colour
- Weight/specific gravity
- Structure
- Conductivity
- Magnetic property
- Fusibility

Colour

Different metals have different colours. For example, copper is distinctive red colour. Mild steel is blue/black sheen.

Weight

Metals may be distinguished, based on their weights for given volume. Metals like aluminium lighter weight (Specific gravity 2.7) and metals like lead have a higher weight. (Specific gravity 11.34)

Structure (Figs 2&3)

Generally metals can also be differentiated by their internal structures while seeing the cross-section of the bar through a microscope. Metals like wrought iron and aluminium have a fibrous structure and metals like cast Iron and bronze have a granular structure.

Fig 2

FERRITE GIVES DUCTILITY AND SLAG FIBRES IMPROVE CORROSION RESISTANCE

Fig 3

FLAKES OF GRAPHITE REDUCE STRENGTH AND IMPROVE MACHINEABILITY
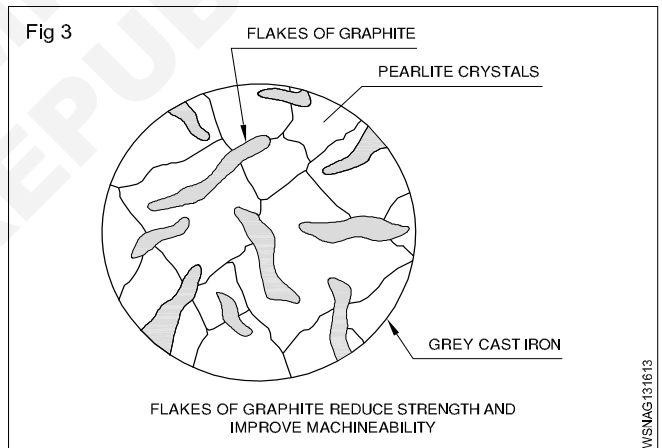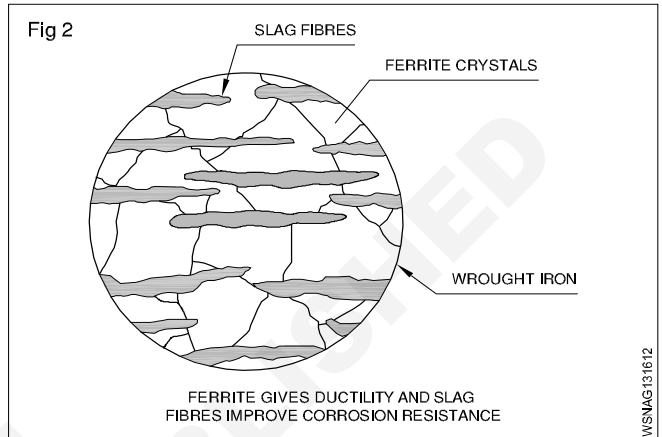
Conductivity (Figs 4&5)

Thermal conductivity and electrical conductivity are the measures of ability of a material to conduct heat and electricity. Conductivity will vary from metal to metal. Copper and aluminium are good conductors of heat and electricity.

Fig 4

33

Fig 5
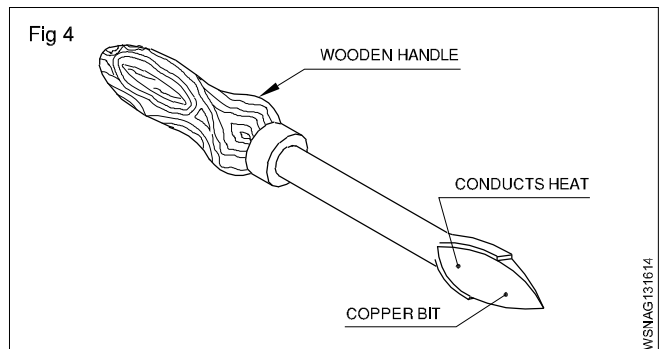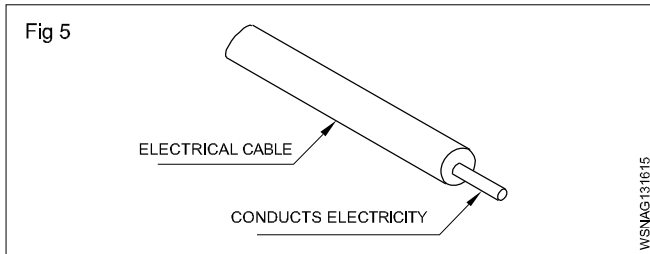
Magnetic property

A metal is said to possess a magnetic property if it is attracted by a magnet.

Almost all ferrous metals, except some types of stainless steel, can be attracted by a magnet, and all non-ferrous metals and their alloys are not attracted by a magnet.

Fusibility (Fig 6)

It is the property possessed by a metal by virtue of which it melts when heat is applied. Many materials are subject to transformation in the shape (i.e) from solid to liquid at different temperatures. Lead has a low melting temperature while steel melts at a high temperature.

Tin melts at 232°C.

Tungsten melts at 3370°C.

Fig 6
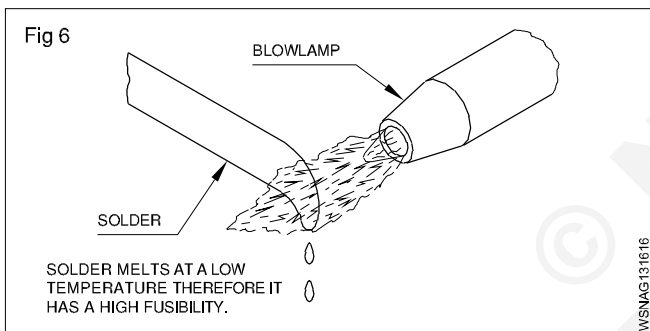
Mechanical properties

- Ductility
- Malleability
- Hardness
- Brittleness
- Toughness
- Tenacity
- Elasticity

Ductility (Fig 7)

A metal is said to be ductile when it can be drawn out into wires under tension without rupture. Wire drawing depends upon the ductility of a metal. A ductile metal must be both strong and plastic. Copper and aluminium are good examples of ductile metals.

Fig 7
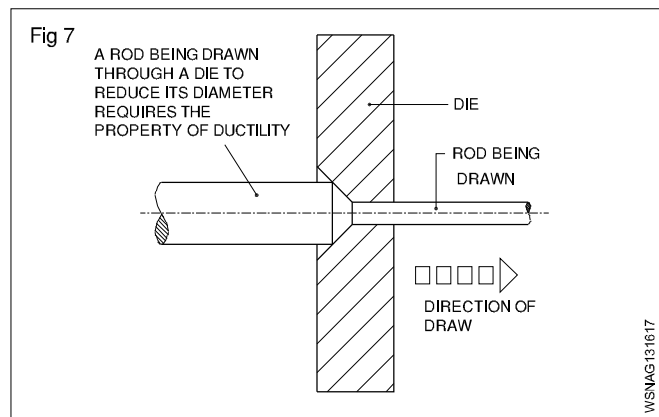
Malleability (Figs 8 and 9)

Malleability is the property of a metal by which it can be extended in any direction by hammering, rolling etc. without causing rupture. Lead is an example of a malleable metal.

Fig 8

Fig 9
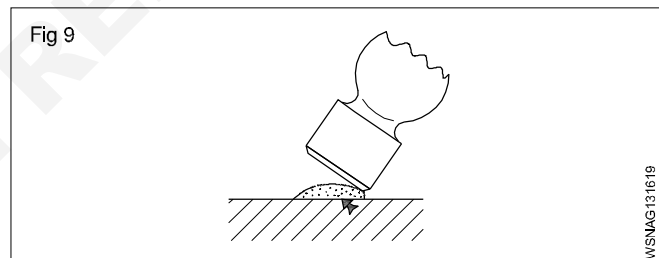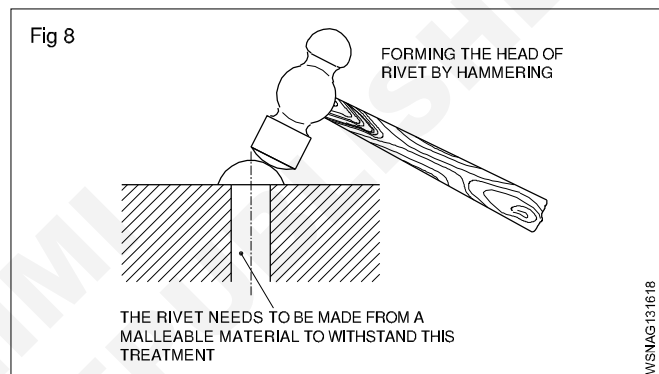
Hardness (Fig 10)

Hardness is a measure of a metal's ability to withstand scratching, wear and abrasion, indentation by harder bodies. The hardness of a metal is tested by marking by a file etc.

Fig 10
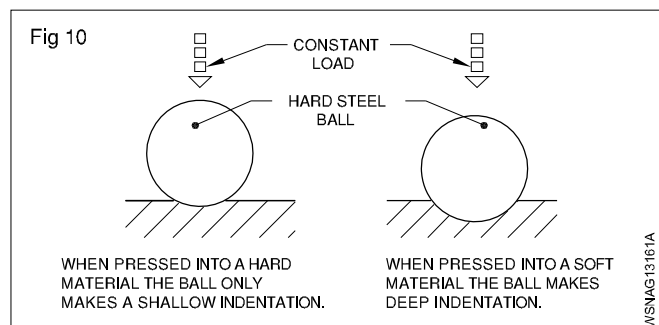
Brittleness (Fig 11)

Brittleness is that property of a metal which permits no permanent distortion before breaking. Cast iron is an example of a brittle metal which will break rather than bend under shock or impact.

Fig 11

THE IMPACT FORCE OF THE HAMMER CAUSES THIS MATERIAL TO BREAK AS IT POSSESSES BRITTLENESS.
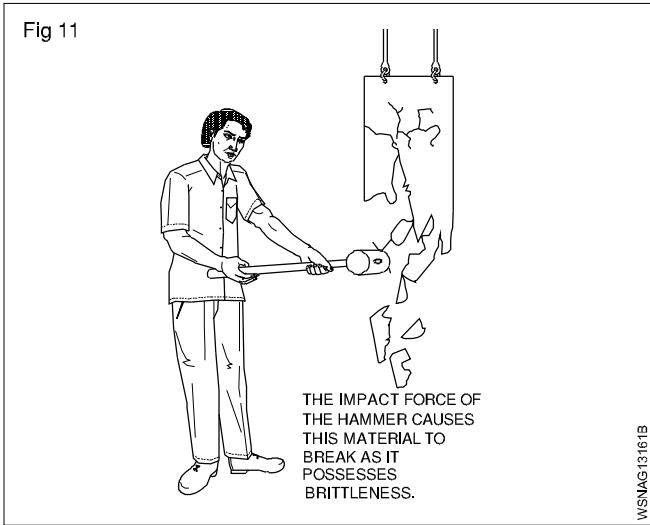
Toughness (Fig 12)

Toughness is the property of a metal to withstand shock or impact. Toughness is the property opposite to brittleness. Wrought iron is an example of a tough metal.

Fig 12

THE CHISEL ABSORBS THE SHOCK OF THE HAMMER BLOW
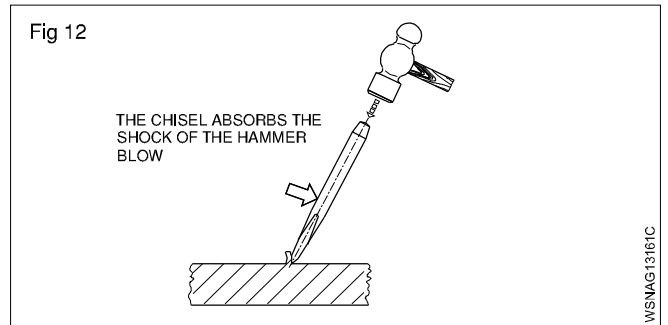
Tenacity

The tenacity of a metal is its ability to resist the effect of tensile forces without rupturing. Mild steel, Wrought Iron and copper are some examples of tenacious metals.

Elasticity

Elasticity of a metal is its power of returning to its original shape after the applied force is released. Properly heat-treated spring is a good example for elasticity.

Mass, Weight, Volume and Density - Mass, volume, density, weight and specific gravity

Mass

Mass of a body is the quantity of matter contained in a body. The unit of mass in F.P.S system is pound (lb), in C.G.S. system gram (gr) and in M.K.S and S.I systems kilogram (kg). 1 ton which is 1000 kg is also used sometimes. The conversion factor is 1000. Three decimal places are shifted during conversion. E.g. 1 ton = 1000 kg 1g = 1000mg.

m - mass of a body

g - acceleration due to gravity in metre/sec^2 = 9.81 m/sec^2

V - volume of the body

ρ - density (pronounced as `rho')

W or FG - weight or weight force

Mass (Fig 1)

Fig 1
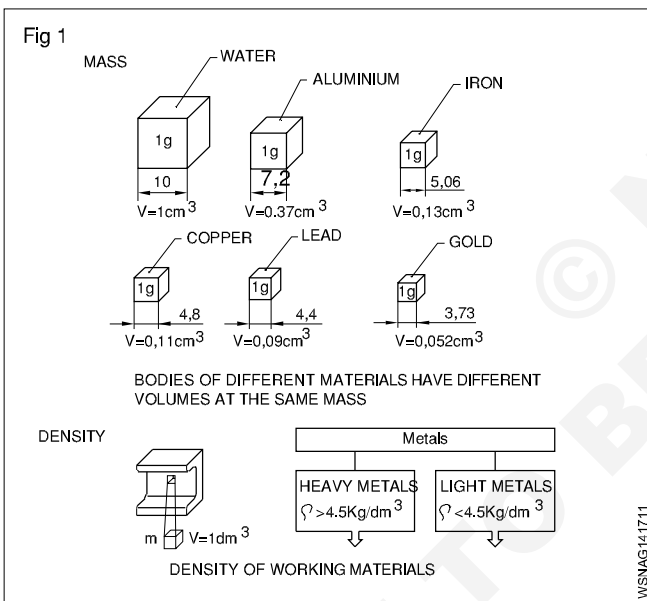
Density

Density is the mass of a body per unit volume. Hence its unit will be gr/cm^3 or kg/dm^3 or ton/m^3.

$$\text{Density} = \frac{\text{mass}}{\text{volume}} = \frac{m}{v} = \rho$$

Weight (Fig 2)

Weight is the force with which a body is attracted by the earth towards its centre. It is the product of the mass of the body and the acceleration due to gravity. The weight of a body depends upon its location.

Fig 2
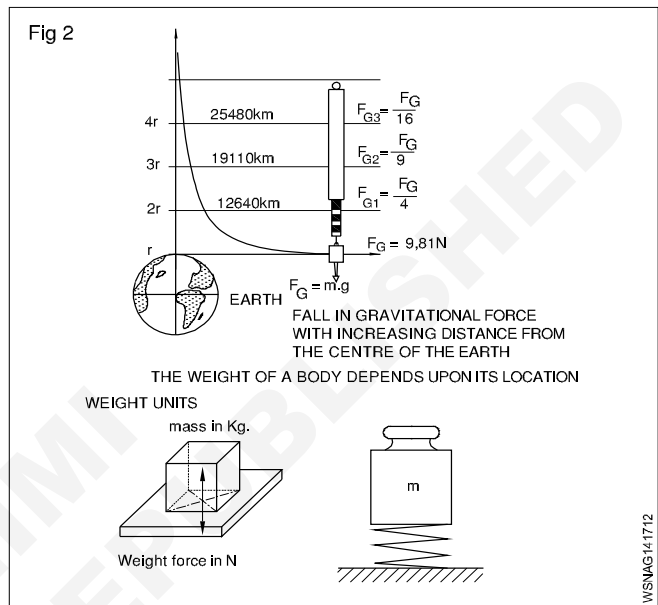
weight = W or FG = mass x gravitational force = m x g

System	Absolute unit	Derived unit	Conversion
F.P.S. system	1 poundal	1 Lb wt	32.2 poundals (1 lb x 1 ft/sec^2 = 1 pound)
C.G.S. system	1 dyne 1 gr x 1 cm/sec^2	1 Gr.wt	981 dynes
M.K.S.	Newton	1 kg.wt	1 Newton =
S.I.system	Newton	Newton	1 kg x 1 m/sec^2

1 kg.wt = 9.81 Newton (approximately 10N)	1 Newton = 10^5 dynes.

Difference between mass and weight

S. No	Mass	Weight
1	Mass is the quantity of matter in a body (ie) measurement of matter in a body	Weight is measure of amount of force acting on mass due to acceleration due to gravity
2	It does not depend on the position or space	It depends on the position, location and space
3	Mass of an object will not be zero	Weight of an object will be zero if gravity is absent
4	It is measured using by physical balance	It is measured using by spring balance
5	It is a scalar quantity	It is a vector quantity
6	When immersed in water mass does not change	When immersed in water weight will change
7	The unit is in grams and kilogram	The unit is in kilogram weight, a unit of force

> **Mass and weight are different quantities.**
>
> **Mass of a body is equal to volume x density.**
>
> **Weight force is equal to mass x acceleration due to gravity.**

Weight , Density and Specific gravity

It is now seen that the mass of a substance is measured by its weight only without any reference to volume. But if equal weights of lead & aluminium, are compared the volume of lead is much smaller than volume of aluminium. So we can now say that lead is more dense than aluminium,. i.e In other words the density of lead is greater than aluminium. (Fig 3 & 4)

Fig 3
COMPARISON BETWEEN MASS & WEIGHT
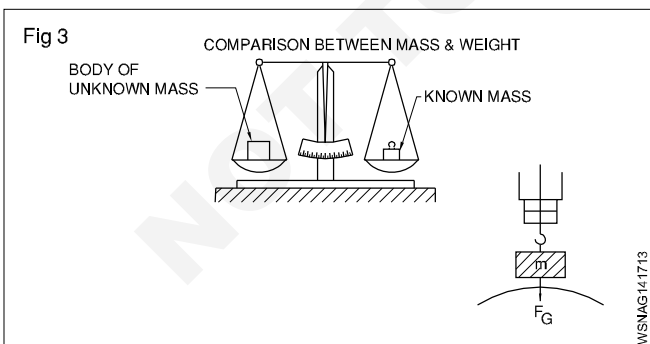
The relation of mass and volume is called density.

The density expresses the mass of volume E.g. 1 dm^3 of water has the mass of 1kg - thus the density of 1kg/dm^3 (Fig 2)

Fig 4 DENSITY
COMPARISON
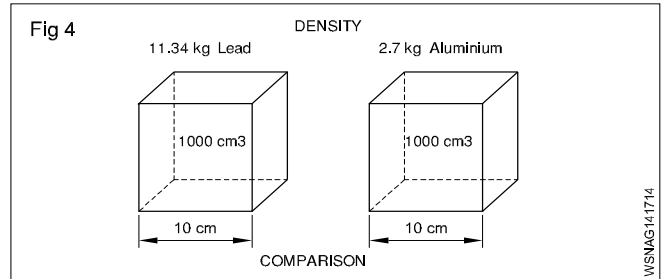
Unit

The density is measured as below

MKS/SI= Kg/m^3, CGS - 1 gm/cm^3 FPS–lbs/c ft

	Solids	gm/cc	Liquids	gm/cc
1	Aluminum	2.7	Water	1.00
2	Lead	11.34	Petrol	0.71
3	Cast iron	6.8 to 7.8	Oxygen	1.43
4	Steel	7.75 to 8.05	Diesel Oil	0.83

The specific gravity of a substance is also called its relative density.

Formula

Specific gravity (or) Relative density $= \dfrac{\text{Density of the substance}}{\text{Density of the water at } 4°C}$

$= \dfrac{\text{Mass of any volume of a substance}}{\text{Mass of an equal volume of water at } 4°C}$

Comparison Between Density And Specific Gravity (Relative Density)

Density	Relative density or Specfic gravity
Mass per unit volume of a substance is called its density	The density of substance to density of water at 4°C is its relative density
Its unit is gm per cu cm; lbs per cu.ft and kg/cubic meter	It has no unit of measurement simply expressed in a number
Density $= \dfrac{\text{Mass}}{\text{Volume}}$	Relative density $= \dfrac{\text{Density of the substance}}{\text{Density of water at } 4°C}$

	Solids	Sp.gy	Liquids	Sp.gy
1	Aluminium	2.72	Petrol	0.71
2	Lead	11.34	Battery acid	1.2 to 1.23
3	Cast iron	6.8 to 7.8	Water	1.00
4	Steel	7.82	Diesel Oil	0.83

From the above table, we can calculate the weight of any given volume of a substance (say Diesel oil) in any units provided we know the specific gravity of the substance. Also vice-versa for volume of density is known.

Mass, Weight, Volume and Density - Related problems for mass, volume, density, weight and specific gravity

1 Calculate the mass in kg of a rectangular steel plate of dimensions 220 x 330 x 15 mm (Fig 1) (density of steel = 7.82 gm/cm³⁾)

Mass = Volume x density

= 22 x 33 x 1.5cm x 7.82 gm/cm³

= 1089 cm³ x 7.82 gm/cm³

mass = 8.516 kg

Fig 1
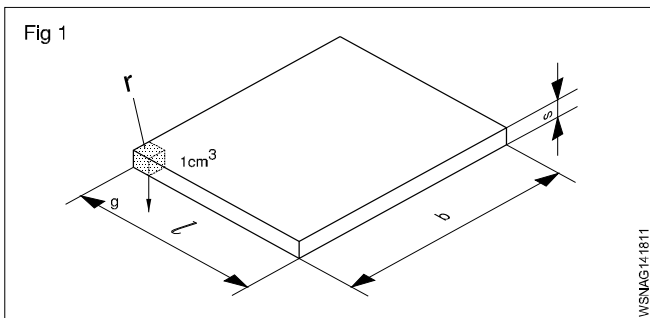
2 What is the weight in Newton if a storage container holds 250 litres of water and amount of water exert on the surface which it is standing? (Fig 2)

(1 litre of water = 1 kg of water)

Density of water 1 gm/cm³ or 1 kg/dm³

Fig 2
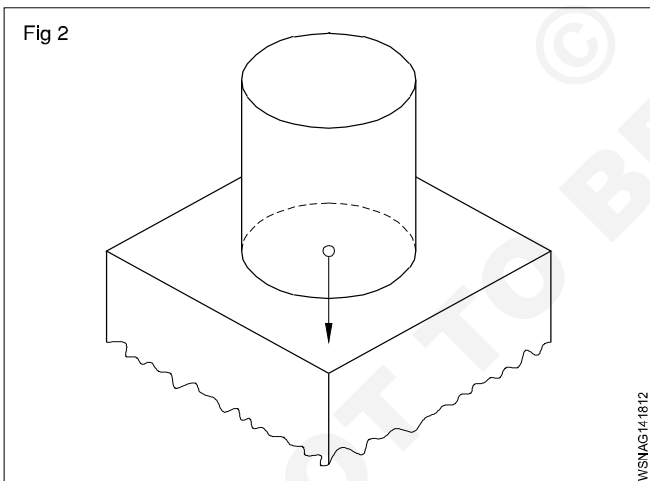
Acceleration due to gravity is taken as 10 metre/sec² (approximation).

Capacity = 250 litres = 250 dm³ in volume.

Mass of water = volume x density of water

= 250 dm³ x 1 kg/dm³ = 250 kg

Weight extended = mass x acceleration due to gravity

= 250 kg x 10 metre/sec²

= 2500 kg.metre/sec² = 2500 N($\because$ 1 kg.m/sec²=1N)

3 A force of 15 dynes acting on a mass of `m' produces an acceleration of 2.5 cm/sec². Find the mass.

1 Gr. wt. = 981 dynes

$\therefore$ 15 dynes = $\dfrac{15}{981}$ Gr.wt

Force = m x acceleration produced by the force

$\therefore$ Gr.wt = mass x 2.5 cm/sec²

$\therefore$ gr.cm/sec² = mass x 2.5 cm/sec²

$\therefore$ mass = $\dfrac{15}{981 \times 2.5}$ grams = $\dfrac{gm.cm/sec^2}{cm/sec^2}$

mass = 0.00612 gram

4 A force of 2 N acts on a mass of 10 kg. Find the acceleration produced by the force on the mass.

Force = 2 N ($\because$ 1 N = 1kg.m/sec²)

Force = mass x acceleration

$\therefore$ 2 kg.metre/sec² = 10 kg x acceleration produced

$\therefore$ 2 x 1 kg.metre/sec² = 10 kg x acceleration produced

$\therefore$ acceleration produced   = $\dfrac{2}{10}$ metre/sec²

= 0.2 metre/sec²

5 Calculate the weight of a body having a mass of 1 kg if the acceleration due to gravity is 9.81 metre/sec²

Weight force = mass x acceleration due to gravity
= 1 kg x 9.81 metre/sec²

(1 kg.metre/sec² = 1 N)

$\therefore$ 9.81 kg metre/sec² = 9.81 N

In the examples solved the value of `g' is taken as 10 metre/sec², unless specifically mentioned otherwise.

• The outside and inside diametres of a hollow sphere are 150 & 70mm respectively. Calculate its mass if the density of material is 7.5 gm/cm³. (Fig 3)

Fig 3

HOLLOW SPHERE
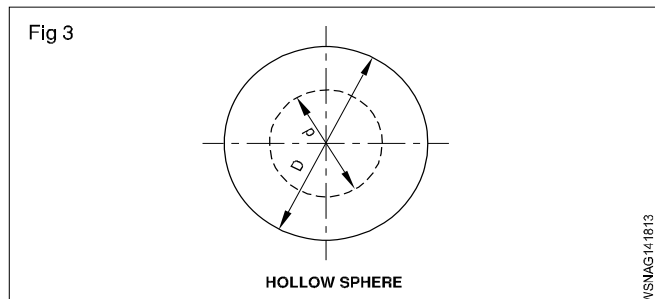
Mass = Volume x Density

= Volume x 7.5 gm/cm³

D= 150 mm = 15cm   R= 7.5 cm

d = 70mm = 7 cm   r = 3.5 cm

$$Volume = \frac{4}{3}\pi\left(R^3 - r^3\right)unit^3$$

$$= \frac{4}{3}\pi(7.5^3 - 3.5^3)$$

=1587.5 cm³

Mass = 1587.5 cm³ X 7.5 gm/cm³

= 11906.6 gm=11.9kg   say 12kg

6   A car has a mass of 800 kg. Find out its weight force (Take 9.81 m/sec²)

($\because$ 1n = 1kg.m/sec²)

The Wt. force of a car=Mass of car x gravitational acceleration

= 800 x 9.81 N

= 7848 Newtons

7   A cylindrical tank 2m dia x 3.5 m length is filled with petrol. Find the weight of petrol in Tonnes, Assume density of petrol 720 Kg/m³. (Fig 4)

Fig 4
PETROL TANK
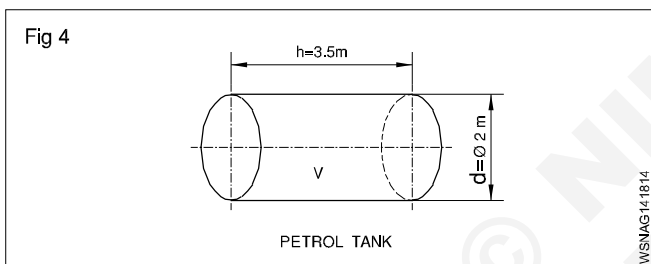
Volume of Tank

$$v = \pi r^2\, l\ (or)\ \frac{\pi d^2}{4} \times l\ \ unit^3 = \frac{\pi \times 2^2}{4} \times 3.5\, m^3$$

3.14 x 3.5 m³ = 10.99 m³

Since 1 m³ = 1000 litres

Volume of Tank = 10.99 x 1000 litres

Density of petrol = 720 Kg/m³.

Weight of Petrol in Kg =10.99x1000 litresx720Kg

= 720 x 10990 Kg

Weight of Petrol in Tonnes

(Metric Units) $= \dfrac{720 \times 10990}{1000}$

Weight of Petrol = 7912.8 Tonnes

8   If the battery acid specific gravity is 1.3, and this is being filled up into a cylindrical tank. Find out its density.

(Density of water = 1000 gm/cm³)

Specific gravity or Relative density

$= \dfrac{Density\ of\ the\ substance}{Density\ of\ water\ at\ 4°c}$

Now, density of battery acid

= Specific gravity x Density of water

= 1.3 x 1000 gm/cm³

= 1300 gm/cm³

Determination of specific gravity of a substance

The specific gravity of a substance may be determined by

1   Archimedes Principle

2   Hydrometer

Archimedes Principle

Archimedes principle states that when a body is fully or partially immersed in a liquid, the amount of liquid displaced by the body is equal to the loss of weight of the body in the liquid.

Weight of a body in a liquid = total weight of the body

- weight of the liquid displaced by the body

This quantity if it is zero then the body will float. It is negative the body will rise up till the weight of liquid displaced by the immersed portion of the body is equal and equal to the weight of the body. If it is positive the body will sink. Specific gravity of solids soluble in water

$= \dfrac{weight\ of\ solid\ in\ air}{loss\ of\ weight\ of\ solid\ in\ water}$

specific gravity of solids soluble in water

$= \dfrac{weight\ of\ solid\ in\ air \times specific\ gravity\ of\ the\ liquid}{loss\ of\ weight\ of\ solid\ in\ which\ the\ solid\ is\ in\ solution}$

specific gravity of a liquid

$= \dfrac{loss\ weight\ of\ a\ solid\ in\ water}{loss\ of\ weight\ of\ the\ same\ solid\ in\ liquid}$

The solid chosen should be such that it is insoluble in both water and the liquid whose specific gravity is to be determined.

Example

1   An iron piece weighs 160 kgf in air and 133 kgf when it is fully immersed in water. Determine the volume and specific gravity of the iron piece.

Weight of the solid in air   = 160 kgf
Weight of the solid in water   = 133 kgf
$\therefore$ Loss of weight in water   = 27 kgf

By Archimedes principle the loss of weight of a solid in water = volume of water displaced.

$\therefore$ Volume of water displaced = 27 cm³

$\therefore$ Volume of the solid= 27 cm³

Density of the iron piece = $\dfrac{\text{mass of iron}}{\text{volume of the piece}}$

$$= \dfrac{160}{160 - 133} = \dfrac{160}{27} = 5.93$$

Specific gravity = $\dfrac{\text{density of iron}}{\text{density of water}} = \dfrac{5.93}{1} = 5.93$

Specific gravity of iron piece = 5.93

2   A metal piece weighs 6.5 kgf in air and 3.5 kgf in water. Find its weight when it is fully immersed in a liquid whose specific gravity is 0.8 and also the S.G of the metal.

Weight of metal piece in air   = 6.5 kgf
Weight of metal piece in water = 3.5 kgf
∴ Loss of weight in water   = 3.00 kgf (6.5 - 3.5)
∴ Specific gravity of metal

$$= \dfrac{\text{Weight of substance in air}}{\text{Loss of weight in water}} = \dfrac{6.5 \text{kgf}}{3 \text{kgf}} = 2.166$$

By applying the principle of Archimedes the above results are derived.

The weight of the metal piece in the liquid = W

∵ loss of weight of the metal in the liquid = 6.5 kgf - W

Specific gravity of the liquid = $\dfrac{\text{loss of weight in liquid}}{\text{loss of weight of water}}$

$$\therefore 0.8 = \dfrac{6.5 \text{kgf} - W}{3 \text{kgf}}$$

∴ W = 6.5 kgf - 3 kgf x 0.8 = 4.1 kgf

∴ loss of weight of the metal in the liquid = 4.1 kgf.

By using a hydrometer, the specific gravity of a liquid is determined. The most common type of hydrometer is the Nicholson's hydrometer which is a variable weight but constant immersion type.

Specific gravity of a liquid

$\dfrac{\text{wt. of hydrometer+ wt. required to sink the hydrometer in the liquid to a fixed mark}}{\text{wt. of hydrometer+ wt. required to sink the hydrometer in water up to the same mark}}$

3   A piece of wood having 80cc volume, when floated on water remains 60cc volume above water. Find the weight of the water displaced.

Water displaced   = Immersed volume

Immersed volume   = volume of wood - volume of wood above water level

= 80 - 60 = 20c.c

Weight of water displaced = volume x density of water

= 20 x 1 = 20 grams

Sl.No	Substance	Density gm/cc
1	Aluminium	2.7
2	Cast Iron	6.8 - 7.8
3	Copper	8.92
4	Gold	19.32
5	Iron	7.86
6	Lead	11.34
7	Nickel	8.912
8	Silver	10.5
9	Steel	7.75 - 8.05
10	Tin	7.31
11	Zinc	7.14
12	Diamond	3.51
13	Bismuth	9.78
14	Brass	8.47
15	Phosphrous Bronze	8.7 - 8.9
16	Ice	0.93
17	Air	0.0013
18	Mercury	13.56
19	Petrol	0.71
20	Diesel	0.83
21	Kerosene	0.78 - 0.81
22	Water	1.0

Assignment

1

Fig 1

l = 1800 mm

b = 65 mm

h = 12 mm

ρ = 7.85 g/cm^3

m = _____ kg

2

Fig 2

Capacity = 36 litres

d = 32 cm

H = _____ cm

3

Fig 3

D = 74 mm

d = 68 mm

l = 115 mm

ρ = 8.6 gm/cm^3

m = _____ gms

4

Fig 4

D_1 = 80 mm

D_2 = 61 mm

d = 39 mm

L = 112 mm

l = 90 mm

ρ = 7.85 gm/cm^3

m = _____ kg

5

Fig 5

D = 44 mm

d = 20 mm

L = 120 mm

l_1 = 60 mm

l_2 = 40 mm

ρ = 7.85 gm/cm^3

m = _____ kg

6

Fig 6

L = 120 mm

B = 90 mm

b_1 = 60 mm

b_2 = 30 mm

d = 55 mm

H = 42 mm

h = 18 mm

ρ = 7.85 gm/cm^3

m = _____ kg

7

Fig 7
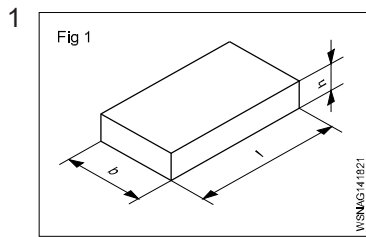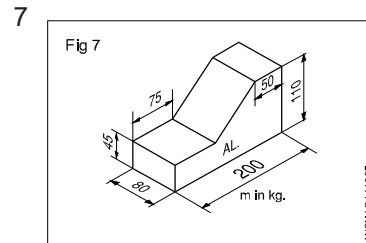
L = 200 mm

l_1 = 75 mm

l_2 = 50 mm

B = 80 mm

H = 110 mm

h = 45 mm

ρ = 2.7 gm/cm^3

m = _____ kg

8

Fig 8

V = 320 cm^3

ρ = 8.9 gm/cm^3

g = 9.80665 metre/ sec^2

m = _____ kg

FG = _____ N

9

Fig 9
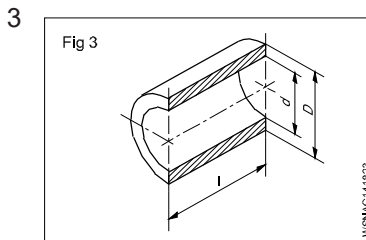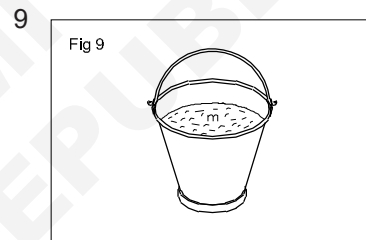
Capacity = 35 litres

g = 10 metres/sec^2

FG = _____ N

10

Fig 10
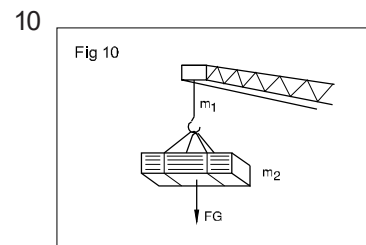
(m_1) mass of chain = 150 kg

Total FG = 8 KN

Load = _____ N

mass m_2 = _____ kg

11

Fig 11

W (FG) = 22.5 N

V (volume) = _____

12

Fig 12
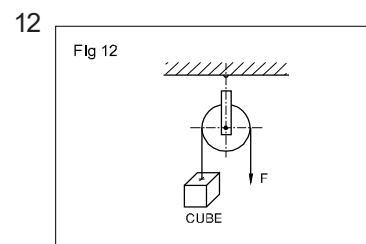
F = 250 d N

side of cube = _____ mm

(cubical counter weight balances `F')

Speed and Velocity, Work, Power and Energy - Speed and velocity - Rest, motion, speed, velocity, difference between speed and velocity, acceleration and retardation

Body at rest

When a body does not change its position, with respect to its surroundings, it is said to be at rest.

Body at motion

When a body changes its position, with respect to its surroundings, it is said to be in motion. The motion may be linear if the body moves in a straight line or it may be circular when it moves in a curved path.

Terms relating to motion

Displacement

When a body is in motion from one place to another, the displacement is the distance from the starting position to the final position.

Speed

It is the rate of change of displacement of a body in motion. It has got no direction and it is a scalar quantity.

Speed = distance travelled per unit time $\dfrac{s}{t} = \dfrac{(Distance)}{Time}$

Unit = m/s, km/Hr.mile/Hr.

Velocity

It is the rate of change of displacement of a body in motion in a given direction. It is a vector quantity and can be represented both in magnitude and direction by a straight line. Velocity may be linear or angular. The unit of linear velocity is metre/sec,

Velocity = $\dfrac{S}{t} = \dfrac{Displacement}{Time}$

Unit = m/s, km/Hr,mile/Hr.

Difference between speed & velocity

Speed	Velocity
The rate of change of place of an object is its speed.	The speed in a definite direction is called velocity.
In the speed, direction is not indicated. Only the magnitude is expressed.	Both the magnitude and direction are expressed.
Speed $= \dfrac{Distance\ covered}{Time}$	Velocity $= \dfrac{Distance\ in\ definite\ direction}{Time}$

Acceleration

Rate of change of velocity is known as acceleration or it is the change of velocity in unit time. Its unit is metre/sec^2. It is a vector quantity.

$a = \dfrac{change\ in\ velocity}{Time}$ m/sec^2

unit = m/s^2 (metre per square second)

u = Initial velocity in metre per second(m/sec)

v = Final velocity in metre per second(m/sec)

s = Distance in metre (m)

t = Time in second (sec)

a = Acceleration m/sec^2 (positive value)

R = Retardation m/sec^2 (negative value of acceleration)

Equations of motion

Then v = u + at

$s = ut + \dfrac{1}{2}\ at^2$ and $v^2 - u^2 = 2as$

$v^2 = u^2 + 2as$

Retardation

When the body has its initial velocity lesser than its final velocity it is said to be in acceleration. When the final velocity is lesser than the initial velocity the body is said to be in retardation. Then the three equation of motion will be

v = u – at

$s = ut -\ at^2$

$u^2 - v^2 = 2as$

Average speed

Vm - Average speed in metre/min, (metre/sec)

  n - Revolutions per minute or number of strokes per minute

  s - Distance travelled, length of stroke.

Stroke speed (Fig 1)

For one revolution of the point k, of the crank pin the distance the power saw blade moves = 2 x s

Therefore 'n' revolutions in a minute the distance = 2 x s x n. Since the stroke of the blade will be given in metre to determine the average speed

Vm = 2 x s x n

Fig 1
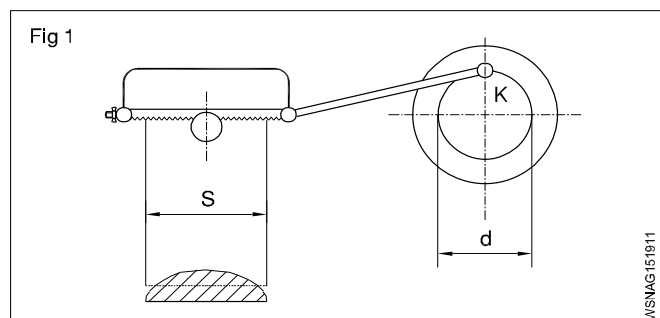
Piston speed (Fig 2)

As the piston moves backward and forward, its speed constantly changes between the upper and lower dead

centres. Hence in this case also the average speed V_m = 2 x s x n. Since s is expressed in mm and n in number of revolutions/per minute and since V_m is given in metre/sec, we have

$$V_m = 2 \times s \times \frac{n}{1000} \text{ metre/min.}$$

$$= \frac{2 \times s \times n}{1000 \times 60} \text{ m/sec}$$

Fig 2
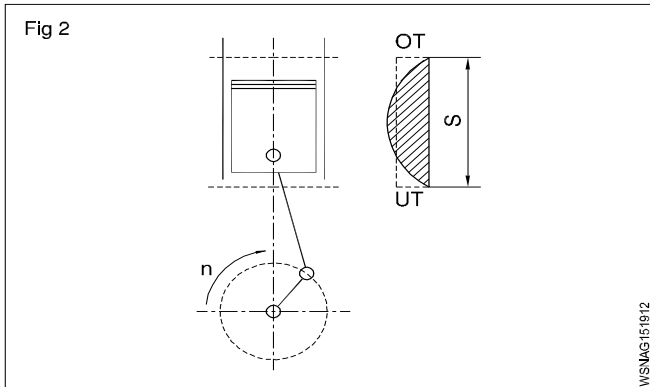
If s is given in metres then

$$V_m = 2 \times s \times \frac{n}{60} = s \times \frac{n}{60} \text{ metre/sec.}$$

2 x s denotes a double stroke.

In case of the reciprocating motion the average speed is taken into account for calculations.

V_m = 2 x s x n metre/min if s is given in metres

Example (Fig 3)

An extrusion press has a crank radius of 20 cm and an rpm of 30/min. Calculate the average speed in metre/min, metre/sec.

s = The diameter = 40 cm.

One crank revolution makes the piston to travel in 2s=80cm

$$V_m = 2 \times 400 \times \frac{30}{100} \text{ metre/min.}$$

= 24 metre/min = 0.4 metre/sec

Fig 3
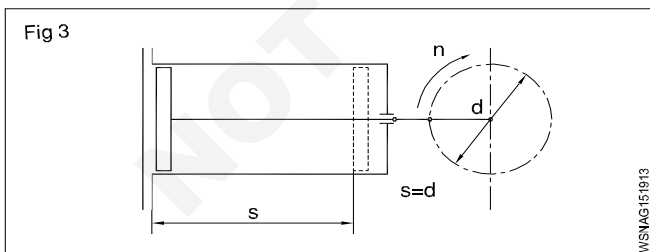
NEWTON'S LAWS OF MOTION

Equations of motions under gravity

Upward	Downward
$V = u - gt$	$v = u + gt$
$s = ut - \frac{1}{2}gt^2$	$s = ut + \frac{1}{2}gt^2$
$u^2 - v^2 = 2gs$	$v^2 - u^2 = 2gs$

Motion under gravity

A body falling from a height, from rest, has its velocity goes on increasing and it will be maximum when it hits the ground. Therefore a body falling freely under gravity has a uniform acceleration. When the motion is upward, the body is subjected to a gravitational retardation. The acceleration due to gravity is denoted with 'g'.

Momentum

It is the quantity of motion possessed by a body and is equal to the product of its mass, and the velocity with which it is moving. Unit of momentum will be kg metre/sec.

Momentum = mass x velocity

Newton's laws

First law

Every body continues to be in a state of rest or of uniform motion in a straight line unless it is compelled to change that state of rest or of uniform motion by some external force acting upon it.

Second law

The rate of change of momentum of a moving body is directly proportional to the external force acting upon it and takes place in the direction of the force.

Third law

To every action there is always an equal and opposite reaction.

In the rivet joint equal forces act on the strap and they opposite force F_2. (Fig 4)

Fig 4
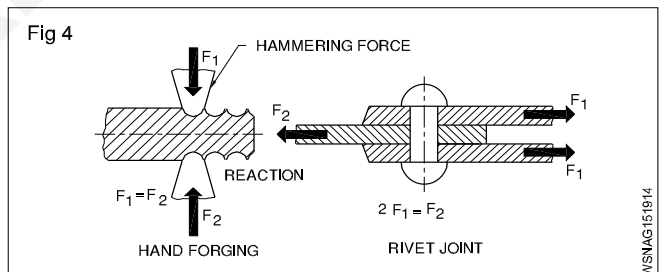
Law of conservation of momentum

When two moving bodies have an intentional or unintentional impact, then sum of the momentum of the bodies before impact = sum of the momentum after impact, or the change in momentum after the impact is zero.

m_1 - mass of one body and

v_1 - velocity with which it moves

m_2 - mass of second body

v_2 - velocity with which it moves

Momentum = m x v= mass of the body x its velocity

Rate of change of momentum = force acting on the body

$$m\left(\frac{(V - u)}{t}\right) = F$$

force = mass x acceleration

Momentum of two bodies before impact = momentum after impact

$m_1 \times v_1 + m_2 \times v_2 = (m_1 + m_2)V$

Terms - Some Examples in vehicles

Displacement

The piston displacement is the space between 2 dead centres (TDC and BDC) where in the piston moves in the cylinder. (Fig 5)

Fig 5
PISTON DISPLACEMENT
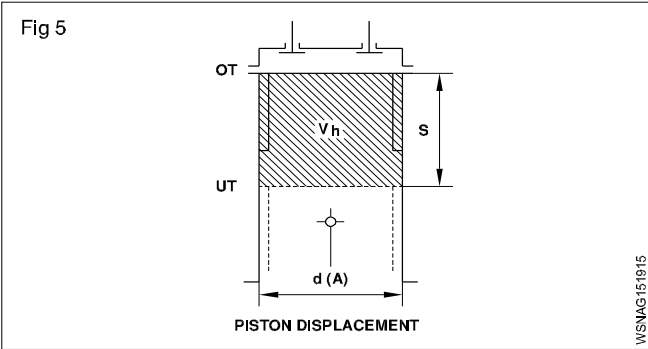
Speed

This is reckoned in 2 ways in a vehicle

– Vehicle speed in kmh/mph

– Engine speed in rpm

Velocity

A motor vehicle, normally changes its speed and direction on road. Hence used in velocity calculation.

Acceleration (Fig 6)

When the speed of the vehicle is increased on road, it is said to be accelerated.

Deceleration (Fig 6)

Deceleration or Retardation (this is further explained)

During the application of brakes of a vehicle the speed of the vehicle is decreased. Then it is said to be decelerated or retarded.

Fig 6
VELOCITY-TIME GRAPH OF A VEHICLE
THE GRAPHICAL REPRESENTATION OF THE ACCELERATION AND DECELERATION
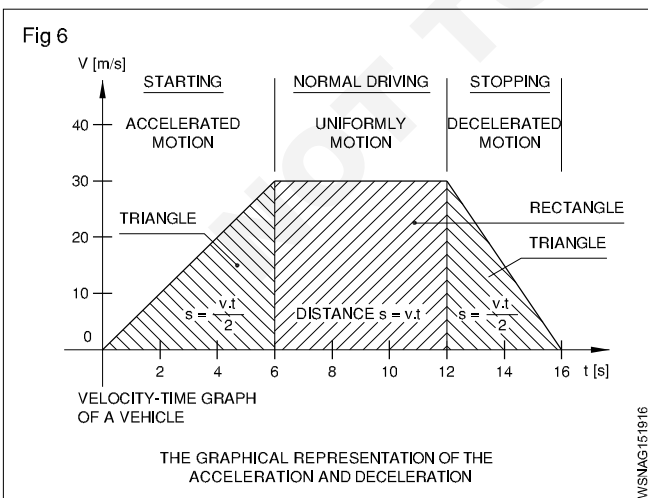
Circular or Angular motion (Fig 7)

When a body rotates about an axis, it is said to have angular motion or circular motion.

Fig 7
CIRCULAR MOTION
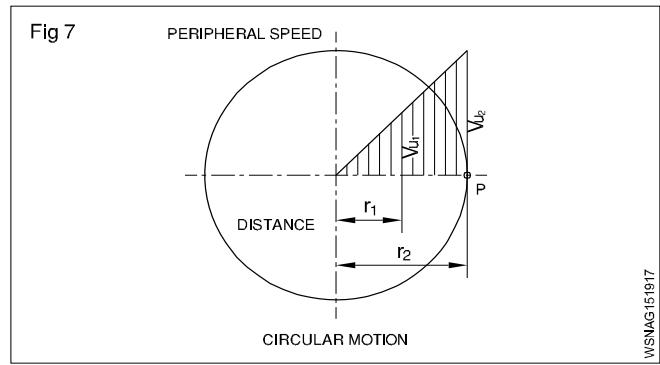
Example

In circular motion bodies (like shafts, axles, gear-wheels, pulleys, flywheels, grinding wheels) turn with constant speed around its axis.

The angular of circular motion is also called Angular velocity or Peripheral speed.

Expressed in Metre/sec or Radians per second.

Bodies at rest and in motion

Terms related to brake system

Every vehicle has a brake system. When brakes are applied on a moving vehicle (with certain velocity) its velocity is reduced and vehicle is decelerated and it stops at a certain distance. So the definition of the terms related to Brake application are set forth below.

Deceleration (a) (Fig 8)

Fig 8
DECELERATION, DECELERATION TIME, TOTAL STOPPING DISTANCE
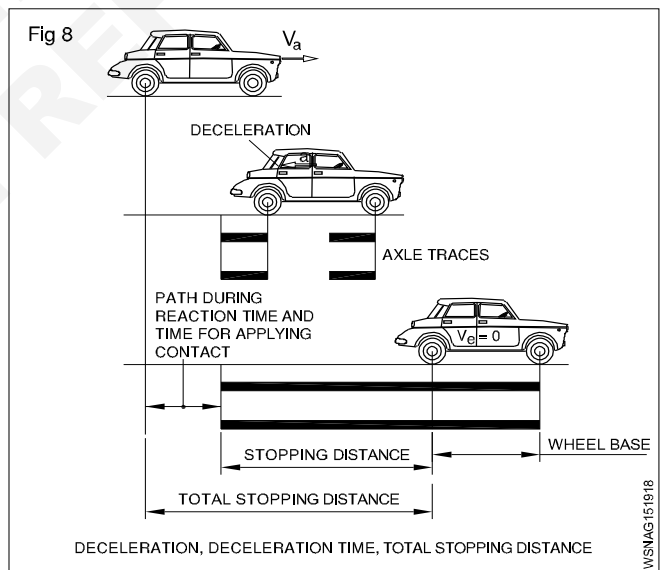
This is the decrease in velocity within a certain time. e.g A car travelling at 90 kmph stops after 10 Sec.

The deceleration $= 90 \times \dfrac{1000}{3600} \times 1/10$

= 25 m/s/10 sec

= 2.5 m/sec^2

Deceleration time

The time 10 seconds is called the above time to stop the vehicle.

Stopping distance

During the deceleration time the car travels a distance called i.e Stopping distance 'd'.

But the total stopping distance is reckoned as equal to normal stopping distance and distance travelled by the car during reaction time of the driver.

The reaction time is explained as below

During the application of brakes, the driver takes sometime to recognise the danger and then apply the brakes. The time (thus elapsed) is called reaction time. During this time the vehicle travels some more distance before coming to a stop. So the total stopping distance actually varies due to the reaction time of the driver and it is longer than the normal stopping distance. The reaction time varies between driver to driver.

Example

A car is travelling with a speed of 72 kmph and its acceleration (a) = 5 m/sec². The reaction time of driver to apply brakes is 1.5 seconds. calculate the total stopping distance.

Solution

Velocity of car = 72 kmph

$$\left(1\,kmph = \frac{1000\ m}{3600\ sec} = \frac{5}{18}\,m/sec\right)$$

$$= \frac{5}{18} \times 72$$

= 20 m/sec

acceleration = 5 m/sec²

$$\text{Normal stopping distance S} = \frac{V^2}{2a}\ (m) = \frac{(20)^2}{2(5)} = 40$$

Total stopping distance

= 40 metre + Velocity x Reaction time

= 40 m + (20 x 1.5) m

= 70 metres.

Newton's Law of Motion

Some Examples in vehicles

First law (with examples) (Fig 9)

Fig 9
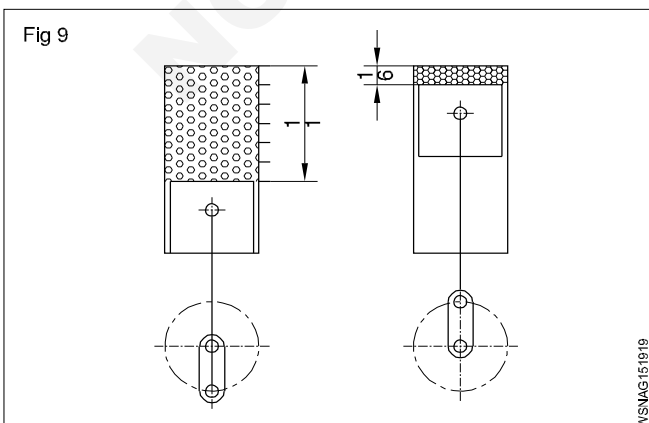
Bodies at rest or in Uniform motion

The diesel engine piston remains at rest at TDC or BDC due to its inertia. Expansion of gas pressure or flywheel momentum moves the piston from TDC or BDC.

Second law (with examples) (Fig 10)

The rate of change of momentum of a moving body (say Engine part or Vehicle)is directly proportional to external force acting take place in the direction of force.

– A connecting rod in motion is brought to rest at BDC.

– The direction of movement of a vehicle is altered by force of wind.

– When a vehicle travels in a down gradient its speed increases.

– The speed of vehicle is decreased when travelling up gradient.

Fig 10
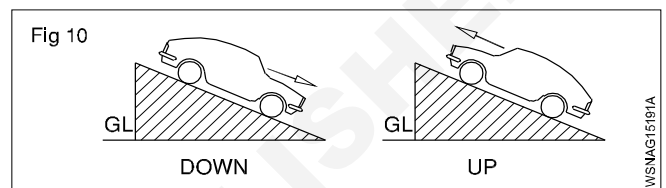
Third law (with examples) (Fig 11&12)

Fig 11

SCREW JACK

Fig 12
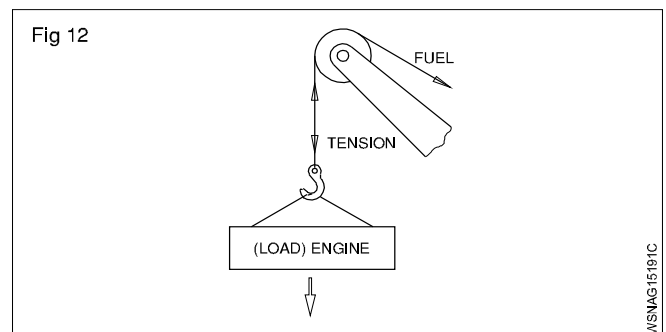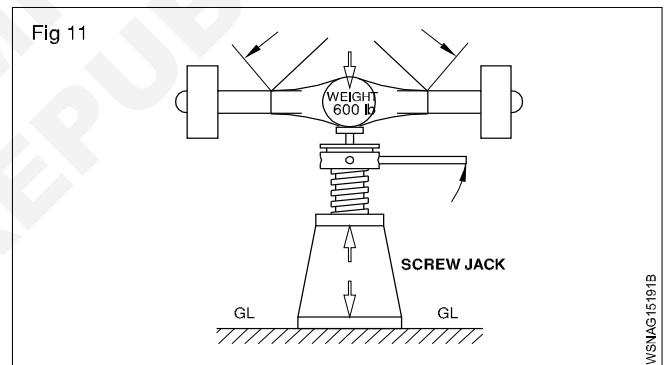
To every action there is always an equal and opposite reaction.

All upward force = All downward forces

– Jack is lifting a differential

– Crane rope is lifting an engine.

Speed and Velocity, Work, Power and Energy - Speed and velocity - Related problems on speed & velocity

Examples

- A body travels a distance of 168 metres in a straight line in 21 secs. What velocity the body is travelling.

  Velocity = distance travelled/time

  = 168 metre / 21 sec

  = 8m/sec

- A train covers a distance of 150 kilometres, between two stations, in 2 1/2 hours. Determine the average velocity with which the train is moving.

  Average velocity = Distance travelled/time taken

  = 150 Km/2 1/2 hrs = $\dfrac{150}{\dfrac{5}{2}} = 150 \times \dfrac{2}{5}$ Km/hr

  = 60 Km/hr

- A vehicle accelerates uniformly from a velocity of 8 km/hr to 24 km/hr in 4 secs. Determine the acceleration and the distance travelled by it during that time.

  Initial velocity = 8 km/hr (u)

  Final velocity = 24 km/hr (v) $a = \dfrac{v - u}{t}$ m/sec^2

  time = 4 sec (t)   acceleration (a)

  $\therefore v = u + at$

  24 km/hr = 8 km/hr + a x 4 sec

  (24km/hr - 8km/hr = 16km/hr)

  $\therefore$ 4a sec = 16 km/hr = 16000 metre/3600 sec

  $\therefore$ acceleration (a) = 16000 metre/3600 x 4 sec^2

  4a = 4.44

  Acceleration (a) = 1.1 metre/sec^2

  Distance travelled (4a) = 4 x 1.1m = 4.4 m

- A car moving with a velocity of 50 km/hr is brought to rest in 45 secs. Find out the retardation.

  Initial velocity = 50 km/hr   (1km= 1000 metres)

  Final velocity = 0 km/hr   (1 Hour = 3600 seconds)

  Time = 45 secs

  v = u – at   50km/hr x $\dfrac{5}{18}$ m/sec = 13.88 m/sec

  0 = u – at $a = \dfrac{u}{t} = \dfrac{13.88 \text{ m/sec}}{45 \text{ sec}} = 0.3 \text{m/sec}^2$

  u = at

  50000/3600 metre/sec = a x 45 sec

  $\therefore$ Retardation = 50000/3600 x 45 metre/sec^2

  = 0.30 metre/sec^2

- A body falling freely under the action of gravity reaches the ground in one second. Determine the height from which the body fell. Take g = 9.81 metre/sec^2.

  Initial velocity = 0 metre/sec (U)

  Acceleration due to gravity = 9.81 metre/sec^2 (g)

  Time taken = 1 sec (t)

  = $ut + \dfrac{1}{2} gt^2$ = 0 x 1 sec + $\dfrac{1}{2}$ x 9.81 m/sec^2 x 1^2 sec

  = 0 x 1 sec + $\dfrac{1}{2}$ x 9.81 metre/sec^2 x 1 sec^2

  1 Sec^2 = 4.905 metres.   s = 4.905 metres

- A force of 30 N acts on a body at rest. The mass of the body is 50 kg. Determine the velocity of the body after 4 secs, the distance it covers during that period and the acceleration

  F = m x a

  30 N = 50 kg x a

  30 kg x metre/sec^2 = 50 kg x a

  $\therefore$ acceleration = 30/50 metre/sec^2

  = 0.6 metre/sec^2 a = 0.6 m/sec^2

  v = u + at

  = 0 + 0.6 metre/sec^2 x 4 sec = 2.4 metre/sec

  s = ut + 1/2 at^2 = 0 + 1/2 x 0.6 metre/sec^2 x 16 sec^2

  = 4.8 metre   s = 4.8 metre

- A stone is thrown vertically upwards with a velocity of 120 metre/sec. Determine (a) the maximum height to which it travels before starting to return to earth. (b) The total time taken by the stone to go up and come down. (c) The velocity with which it will strike the ground.

  Initial velocity of throw = 120 metre/sec (u)

  Final velocity = 0 metre/sec (v) (taken g = 10 m/sec^2)

  Retardation due to gravity = 10 metre/sec^2

  $u^2 - v^2 = 2g.s$

  $\therefore$ 120^2 metre^2/sec^2 – 0 = 2 x 10 metre/sec^2 x s

  $\therefore$ s = 120 x120/2 x 10 metre = $\dfrac{120 \times 120}{2 \times 10}$

  = 720 metre

  when it comes down its velocity at start = 0 metre/sec.

The acceleration due to gravity = 10 metre/sec^2 and the distance travelled = 720 metre

$\therefore$ v^2– u^2 = 2as   v^2-0 = 2x 10 m/sec^2 x 720 m

v^2– 0 = 2 x 10 x 720 metre^2/sec^2 $v = \sqrt{14400}$ m^2/sec^2

$\therefore$ v = 120 metre/sec

Time taken to go up and reach a velocity of 0 metre/sec = u/g = 120 metre/sec/10 metre/sec^2 = 12 sec.

Time taken to start from rest and attain a velocity of 120 metre/sec = v/g = 12 sec.

$\therefore$ Total time taken = 24 sec.

- Calculate the Angular velocity in radian/second of an engine flywheel when it is rotating at 2800 rpm. (Fig 1 & 2)

Angular velocity (W) = This is the rate of change of displacement or angle turned through per unit time.

Solution

Angular velocity of flywheel W = $2\pi N/60$ rad/sec. [N = 2800 rpm]

= 2π x 2800/60 radian/sec.

= 293.3 radian/sec.

Fig 1

Fig 2
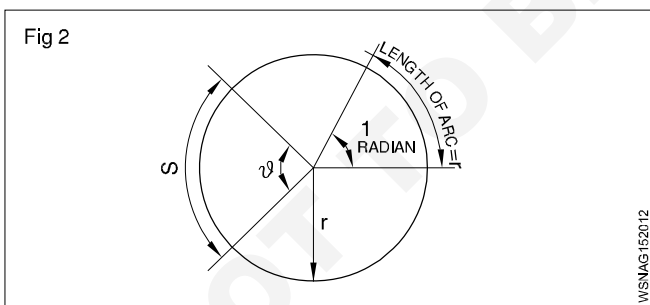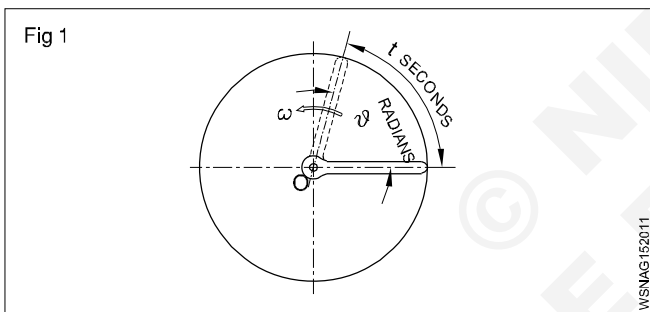
- A motor car road wheel of dia 540 mm turns through an angle of 120°. Calculate the distance moved by a point on tyre thread of the wheel.

Solution

There are 2π radians in one turn of wheel. i.e 2π radians = 360°

Since wheel turns 120° angle, 120° = 120 x 2π/360

= 2.094 radians

Distance moved by a point on tyre S – re

[where r = 270 mm

θ = 2.094 radian]

S = 270 x 2.094 mm

  = 565.38 mm

Circumferential distance moved by the point = 565.38 mm

- The rear wheels of a car have diameter of 600 mm. The rear axle makes 250 rpm. Find out the peripheral speed of rear wheels in m/sec.

Solution

Peripheral speed V = $\dfrac{\pi dN}{1000} \times \dfrac{1}{6}$ (m/s)

$= \dfrac{3.14 \times 600}{60} \times \dfrac{250}{1000} = 7.85$ m/sec

- Calculate the stopping distance of a car travelling with a speed of 72 km/h and being accelerated with a - 5 m/ sec^2.

Solution

Va (initial speed of a car) = 72 kmph

$(1 \text{ kmph} \times \dfrac{1000}{3600} \text{ m/sec}) = 72 \dfrac{5}{18}$ m/sec
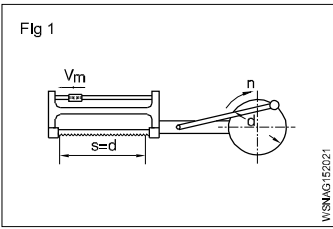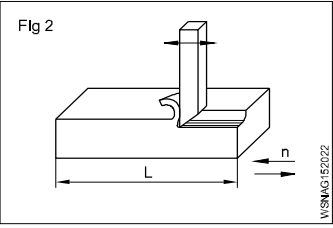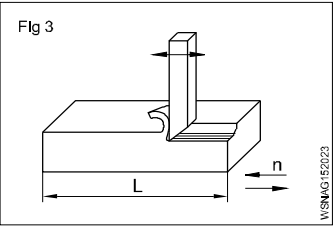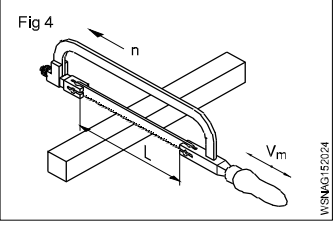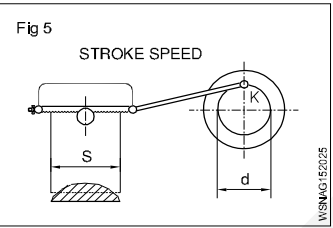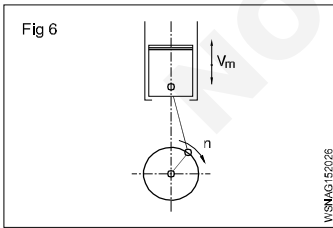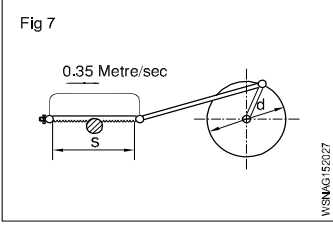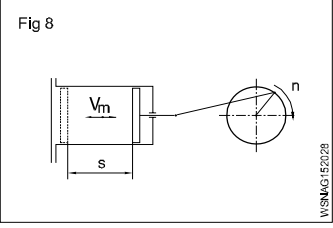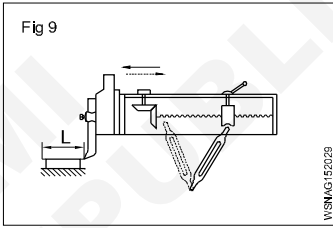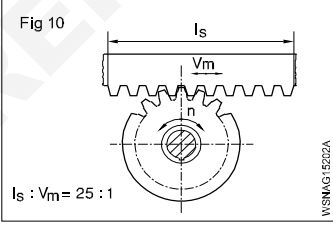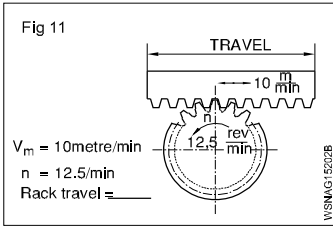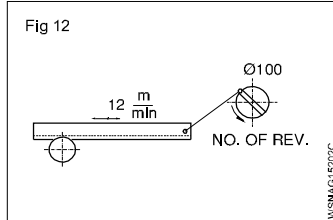
= 20 metres/sec

Stopping distance S = $\dfrac{Va^2}{2a}$ (metre)

$= \dfrac{20^2}{2 \times 5} = \dfrac{400}{10}$

$= 40$ metre

Assignment

1

S = 180 mm

n = 65 (double stroke)

Vm = _____ metre/min

Vm is average cutting speed)

2

V = 16 metre/min

s = 210 mm

n = _____

3

(V is the cutting speed)

n = 22 strokes (Double stroke)/min

V = 18 metre/min

s = _____ mm

4

s = 240 mm

n = 30 (working stroke)

V = _____ metre/min

5

n = 50 cutting strokes

V = 32 metre/min

d = _____ mm

6

s = 64 mm

n = 3600 rpm

Vm = _____ metre/sec

Vm is the average piston speed)

7

Vm = 0.35 metre/sec

s = 200 mm

n = _____ rpm

8

s = 650 mm

Vm = 90 metre/min

n = _____ rpm

9 Vm_1 = 5.2 metre/sec

Increased to

Vm_2 = 6.3 metre/sec

Increase in n (rpm) = _____ %

10

s = 250 mm

n = 45 (double strokes)

V = _____ metre/min

11

Is : Vm = 25 : 1

n = _____ (double strokes)

Is = rack travel

Vxm = stroke speed/ min

12

Vm = 10 metre/min.

n = 12.5 / min.

Rack travel = _____

13

dia of crank = 100 mm

Rack

speed = 12 metre/min

Crank disc 'n" = _____ rpm

14

Fig 13
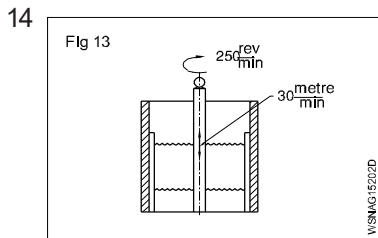
spindle 'n' = 250 rpm

Average stroke speed = 30 metre/min

stroke length = _____ mm

15

Fig 14

Car Speed = 90 km/hr

Time to stop = 10 sec

Deceleration = _____ metre/sec^2

16

Fig 15

Car speed = 80 km/hr

Distance stopped = 60 metre

Deceleration of car = _____ metre/sec^2

17

Fig 16

Deceleration = 4.5 m/sec^2

Stopping distance = 50 metres

Velocity of car = _____ km/hr

18

Fig 17

Distance travelled by car = 600 km

Time = 8 hrs 20 min

Average velocity = _____ km/hr

19

Fig 18
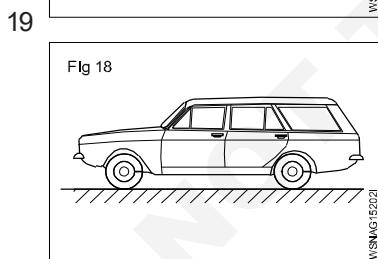
Average velocity = 56.3 km/hr

Distance travelled = 464.475 km

Travelling time = _____ hrs

20

Fig 19

CAR WHEEL

Car wheel

n = 720 rpm

Peripheral speed = 18.84 m/sec

d = _____

21

Fig 20

ANGULAR SPEED

Angular speed

n = 2000 rpm

Angular velocity = _____ radians/sec

Use

$W = 2\pi N/60$ rad/sec

22

Fig 21

Piston Velocity/Speed

S = 74 mm

n = 4500 rpm

Mean velocity = _____ m/sec

Maximum velocity = _____ m/sec

(Average Speed of Piston)

23 Total Stopping Distance $= \dfrac{V^2}{2a} + \text{velocity} \times \text{reaction time}$

(Use $= V^2/2a$)

V = Vehicle speed = 80 km/hr

Deceleration = 5 m/sec^2

Reaction Time of driver = 2 seconds

Total Stopping Distance = _____ meter

Speed and Velocity, Work, Power and Energy - Work, power, energy, HP, IHP, BHP and efficiency

Work (Fig 1)

Work is said to be done by a force, when it moves, its point of application through a distance. Applied force 'F' moves a body through a distance's.

Work done 'W' = F x s.

The S.I. unit of work is 1 joule which is the work done by a force of moving the body through a distance of 1 metre.

Therefore joule = 1 N x 1 metre = 1 Nm

Also 1 joule = 1 Nm = 10^5 dynes x 100 cm = 10^7 dynes cm = 10^7 ergs.
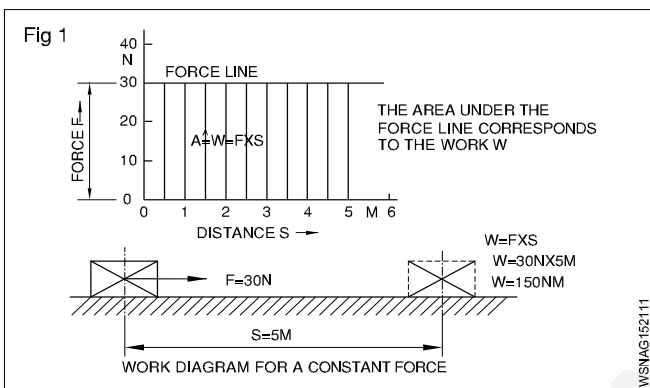
F - force or weight force in N

s - distance the body on which force acts is moved in metres

t - time in seconds

v - speed in metre/sec

w - work done by the force in joules

P - Power in Watts

P_{out} - Power output

P_{in} - Power input

Force

A Force is that which changes or tends to change the state of rest or motion of a body.

Force = Mass x Acceleration

   F   = Ma

Unit

   F   = M x a

        = kg x m/sec^2

        = 1 Newton (SI unit)

> **(Newton: If 1 kg of mass accelerates at the rate of 1m/sec^2 then the force exerted on the mass is 1 newton)**

FPS   = 1 pound x 1 Feet/second^2

          = 1 pound

CGS   = 1 gm x 1cm/second^2

          = Dyne

MKS   = 1 kg x 1m/second^2

          = Newton.

1 Newton = 10^5 dynes

1kg wt   = 9.81N

1 pound = 4.448N,

Newton = 0.225 pound.

Absolute units

In C.G.S. system unit of work = 1 erg = 1 dyne x 1 cm

In F.P.S system unit of work = 1 Foot poundal = 1 poundal x 1 foot

In M.K.S. system unit of work = 1 joule = 1 Newton x 1 metre

Derived units

C.G.S. system 1 Gm Wt x 1 cm = 981 ergs.

F.P.S. system 1 ft LB = 981 foot poundal

M.K.S. system 1 kgf metre = 981 joule.

Power (Fig 2)
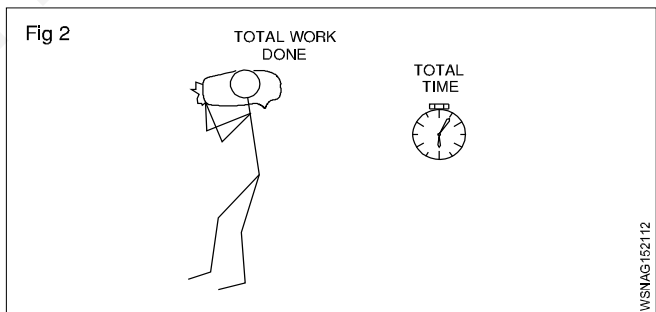
It is the work done in unit time.

$$\text{Power } P = \frac{\text{total work done}}{\text{total time}}$$

$$P = \frac{Nm}{sec}$$

The S.I units of power = 1Nm/sec = $\dfrac{1 \text{ joule}}{sec}$

which is = 1 watt. power in watts = $\dfrac{w}{t} = \dfrac{F.s}{t}$ = FXV

which is equal to 1 Watt. Power in watts = w/t = F.s/t = F x V

In M.K.S. system the unit is 1 kgf meter/sec. One horse power is = 75 kg metre/sec or 4500 kgf metre/min.

1HP (metric) = 735.5 Watts

1HP (British) = 746 Watts = 0.746 KW

1 KW = 1.34 HP

Power input is the power given to a machine to do work. Power output is what we get out of the machine. Power output is always less than power input due to friction in the machine. The ratio between power output to power input is efficiency of the machine and it is expressed in percentage. (Fig 3)

Fig 3
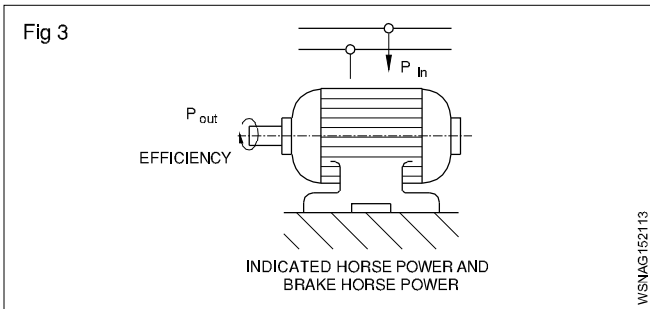
$$efficiency = \frac{power\ output}{power\ input} \times 100\%$$

Indicated Horse Power and Brake Horse Power

The power actually generated by the engine or generator is the indicated horse power which is indicated on the plate.

The Brake horse power is the power available to do useful work. B.H.P is always less than I.H.P. due to losses to overcome frictional resistance.

$$\therefore mechanical\ efficiency = \frac{B.H.P}{I.H.P} \times 100\%$$

Work done by a force = Magnitude of the force x distance moved by the body

Power = Total work done / total time taken

$$efficiency = \frac{power\ output}{power\ input} \times 100\%$$

Energy

The energy of a body is its capacity to do work. It is equal to power x time. Hence the unit of energy is the same as the unit of work in all systems.

Forms of energy

Mechanical energy, Electrical energy, Atomic energy, Heat energy, Light energy, Chemical energy, sound energy. Energy of one form can be transformed into energy of another form.

Law of conservation of energy

– The energy can neither be created nor destroyed.

– Total energy possessed by a body remains the same.(Fig 4)

Depending upon the position of the body or body in motion, mechanical energy possessed by the body may be potential energy or kinetic energy respectively.

Fig 4
CONSERVATION OF ENERGY
1. STATE OF REST
2. ACCELERATED DOWNWARD MOMENT IN AN ARC
3. STATE OF MAXIMUM VELOCITY
4. RETARDED UPWARD MOVEMENT IN AN ARC
5. STATE OR REST
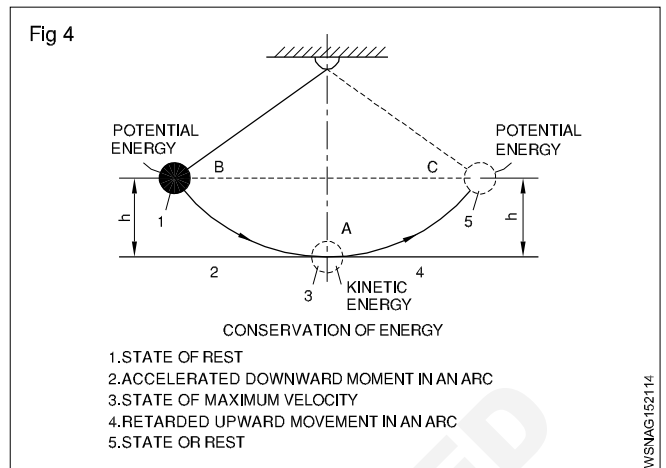
Examples

1 A man weighting 75kg climp 200 metre high hill. Find the Work done by a man?

Formula: Work done (W) = F x S

Given data: F = 75 kg

S = 200m

To find: Work done (W) = ?

Solution: Work done (W) = F x S

= 75 x 200 = 15000

Ans: Work done (w) = 15000 kgm

2 Find the work required to lift a mass of 36.3 Newtons through a height of 3.7 metres?

Formula: Work done (W) = F x S

Given data: F = 36.3 N

S = 3.7m

To find: Work done (W) = ?

Solution: Work done (W) = F x S

= 36.3 x 3.7 N.m

= 134.31 Joules

Ans: Work done (W) = 134.31 Joules

3 Calculate the Work done by a man weighing 50kg in carrying a mass of 20kg over his head when he covers a distance of 15metres in vertical direction.

Formula: Work done (W) = F x S

Given data: F = 50kg + 20kg = 70kg

S = 15 m

To find: Work done (W) = ?

Solution: Work done (W) = F x S

= 70 x 15 = 1050

Ans: Work done (W) = 1050 kg.m

4 A man weighing 60kg lifts a weight of 40kg to the top of building 12 metres height. Find the useful Work done by him and also the efficiency?

Formula: Work done (W)   = F x S

Given data: Man weight   = 60kg

Lifts a weight   = 40kg

Total weight   = 60 + 40 = 100kg

Distance   (S)   = 12 m

To find: a) Work done (W) = ?

b) Efficiency (η)   = ?

Solution:

a) Work done (W) = F x S

= 100 x 12 = 1200 kg.m

b) Efficiency (η)   = $\dfrac{Output}{Input}$ x 100%

= $\dfrac{40 \times 12}{60 \times 12}$ x 100%

= $\dfrac{480}{720}$ x 100%

= 66.67%

Ans: a) Work done (W)   = 1200 kg.m

b) Efficiency (η)   = 66.67%

5 A pump pumps 4000kg of water from 50 metres depth in 40 minutes. Find the Work done by pump in one second?

Formula: Work done (W) = F x S

Given data: F   = 4000 kg

S   = 50 m

To find: Work done per second = ?

Solution:

Work done in 40 minutes,

Work done (W) = F x S

= 4000 x 50 = 200000 kgm

= $\dfrac{200000}{40}$ = 5000

Work done in 1 second = $\dfrac{5000}{60}$ = 83.3

Ans: Work done in 1 second (W) = 83.33 kg.m

6 A body of 225 kg is moved by 300 metres in 90 seconds. Find the power required to lift this body?

Formula: Power (P) = $\dfrac{FxS}{t}$

Given data: F   = 225 kg

S   = 300m

t   = 90 sec

To find: Power   (P) = ?

Solution: Power   (P) = $\dfrac{FxS}{t}$

= $\dfrac{225 \times 300}{90}$ kg.m/sec

= 750 kg.m/sec

Ans: Power (P) = 750 kg.m/sec

7 A hydraulic press lifts a load of 5 tonnes in 5 minutes to a height of 5 metres. Calculate the power of the press?

Formula: Power   (P) = $\dfrac{FxS}{t}$

Given data: F = 5 tonnes = 5000 kg

S = 5 metres

t = 5 minutes = 5 x 60 = 300 sec

To find: Power   (P) = ?

Solution: Power   (P) = $\dfrac{FxS}{t}$

= $\dfrac{5000 \times 5}{300}$ = 83.33

Ans: Power (P) = 83.33 kg.m/sec

8 A man weighing 750N takes 25N material to a height of 10 metres in one minute. calculate the power of man?

Formula: Power (P) = $\dfrac{FxS}{t}$

Given data:

Man weight   = 750N

Material weight   = 25N

F   = 750 + 25 = 775N

S   = 10 m

t   = 1 min = 60 sec

To find: Power   (P) = ?

Solution: Power   (P) = $\dfrac{FxS}{t}$

= $\dfrac{775 \times 10}{60}$ = 129.17N m/sec

Ans: Power (P) = 129.17N m/sec (or) watts

9 What is the power of pump which takes 15 seconds to lift 90kg of water to a tank situated at a height of 30 metres. (Take g = 10m/sec²)?

Formula: Power $(P) = \dfrac{F \times S}{t}$

Given data:　　F = 90 kg

　　　　　　　　S = 30 m

　　　　　　　　t = 15 sec

To find: Power $(P) = ?$

Solution: Power $(P) = \dfrac{F \times S}{t}$

$$= \dfrac{f \times g \times s}{t}$$

$$= \dfrac{90 \times 10 \times 30}{15}$$

$$= 18 \text{N m/sec}^2$$

Ans: Power $(P) = 180$ watts

10 A hoist lifts a weight of 1000kg through a height of 33 metres in one minute. Find out the horsepower of the hoist?

Formula: Horsepower $HP = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

Given data:　　F = 1000 kg

　　　　　　　　S = 33 m

　　　　　　　　t = 1 minute = 60 sec

To find: Horsepower $HP = ?$

Solution: Horsepower $HP = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

　　　　　　(∵ 75 kg.m/sec = 1 HP)

$$= \dfrac{1000 \times 33}{60} \times \dfrac{1}{75}$$

$$= 7.33 \text{ H.P.}$$

Ans: Horsepower, HP = 7.33 H.P.

11 A pump can raise 900 litres of water per minute to a height of 45 metres. Calculate the H.P of pump?

Formula: Horsepower $HP = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

Given data:　　F = 900 litres = 900 kg

　　　　　　　　S = 45 m

　　　　　　　　t = 1 minute = 60 sec

To find: Horsepower $HP = ?$

Solution: Horsepower $HP = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

　　　　　　(∵ 1 HP = 75 kg.m/sec)

$$= \dfrac{900 \times 45}{60} \times \dfrac{1}{75} = 9 \text{ H.P}$$

Ans: Horsepower, HP = 9 H.P.

12 Find the horsepower of an engine to lift a weight of 2 tonnes to a height of 30 metres in two minutes?

Formula: Horsepower $HP = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

Given data:　　F = 2 tonnes = 2000 kg

　　　　　　　　S = 30 m

　　　　　　　　t = 2 minutes = 120 sec

To find: Horsepower $HP = ?$

Solution: Horsepower $HP = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

　　　　　　(∵ 1 HP = 75 kg.m/sec)

$$= \dfrac{2000 \times 30}{120} \times \dfrac{1}{75} = 6.67 \text{ H.P.}$$

Ans: Horsepower, HP = 6.67 H.P.

13 Find out horsepower of a pump required to lift 10000 litres of water in 3 minutes at height of 16 metres. Assume efficiency of pump as 94%?

Formula: Horsepower $HP = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

　　　　　　$\eta = \dfrac{\text{Output}}{\text{Input}} \times 100\%$

Given data:　　F = 10000 litres = 10000 kg

　　　　　　　　S = 16 litres

　　　　　　　　t = 3 minute = 180 sec

To find: Horsepower $HP = ?$

Solution: Horsepower $HP = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

　　　　　　(∵ 1 HP = 75 kg.m/sec)

$$= \dfrac{10000 \times 16}{180} \times \dfrac{1}{75}$$

$$= 11.85 \text{ H.P.}$$

　　　　　　$\eta = \dfrac{\text{Output}}{\text{Input}} \times 100\%$

　　　　　　$94 = \dfrac{11.85}{\text{Input}} \times 100\%$

　　Input $= \dfrac{11.85 \times 100}{94} = \dfrac{1185}{94}$

$$= 12.606 \text{ H.P.}$$

Ans: Input H.P of Pump = 12.606 H.P.

14 Find the horsepower of a motor which is required to lift 500 tonnes of coal per hour from a mine of 320 metre depth. Efficiency of motor is 0.75?

Formula: $\eta = \dfrac{\text{Output}}{\text{Input}} \times 100\%$

$\text{Output H.P} = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

Given data:

$F = 500$ tonnes $= 500000$ kg

$S = 320$ metres

$t = 1$ hour $= 3600$ sec

$\eta = 0.75 = 75\%$

To find: Pump HP = ?

Solution:

$\text{Output HP} = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

($\because$ 1 HP = 75 kg.m/sec)

$= \dfrac{500000 \times 320}{3600} \times \dfrac{1}{75}$

$= 592.59$ H.P.

$\eta = \dfrac{\text{Output}}{\text{Input}} \times 100\%$

$75 = \dfrac{592.59 \times 100}{\text{Input}}$

$\text{Input} = \dfrac{59259}{75}$

Ans: Input = 790.12 H.P

15 A train weighing 25 tonnes is moving at a speed of 90km/hour. Find the horsepower of the engine, if the frictional force is 5kg per tonnes?

Formula: Horsepower $HP = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

Given data: Train speed $= 90$ km/hour

$= 90 \times \dfrac{1000}{3600} = 25$ m/sec

Train weight $= 25$ tonnes

Frictional force per tonnes $= 5$ kg

25 tonnes frictional force

$(F) = 25 \times 5 = 125$kg

To find: Horsepower of the engine = ?

Solution: $HP = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

$= \dfrac{125 \times 25}{1} \times \dfrac{1}{75}$

Ans: HP = 41.67 H.P.

16 A pump delivers 9000 litres of water per minute to a height of 14 metres. The efficiency of the pump is 78%. The efficiency of electric motor which drives the pump is 92%. Find out the input of the motor?

Formula: $\eta = \dfrac{\text{Output}}{\text{Input}} \times 100\%$

$\text{Output H.P} = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

1 H.P = 0.7355 KW (metric)

Given data:

$F = 9000$ litres $= 9000$ kg

$S = 14$ metres

$t = 1$ minute $= 60$ sec

pump $\eta = 75\%$

motor $\eta = 92\%$

To find: Electric motor (KW) = ?

Solution:

$\text{Pump Output HP} = \dfrac{F \times S}{t} \times \dfrac{1}{75}$

$= \dfrac{9000 \times 14}{60} \times \dfrac{1}{75}$

$= 28$ H.P.

Input of the pump

$\eta = \dfrac{\text{Output}}{\text{Input}} \times 100\%$

$78 = \dfrac{28}{\text{Input}} \times 100$

$\text{Input} = \dfrac{28 \times 100}{78} = 35.9$ H.P

Output of the motor = Input of the pump

$\text{Output} = 35.9$ H.P

Input of the motor

$\text{Motor } \eta = \dfrac{\text{Output}}{\text{Input}} \times 100\%$

$92 = \dfrac{35.9}{\text{Input}} \times 100$

$\text{Input} = \dfrac{35.9 \times 100}{92} = 39.02$ H.P

Ans: Motor input = 39.02 H.P

17 I.H.P of generator is 6 H.P and its efficiency is 90%. Find tis B.H.P.

Formula: $\eta = \dfrac{B.H.P}{I.H.P} \times 100\%$

Given data:

$$I.H.P = 6 \text{ H.P}$$
$$\eta = 90\%$$

To find: B.H.P = ?

Solution: $\eta = \dfrac{B.H.P}{I.H.P} \times 100\%$

$$90 = \dfrac{B.H.P}{6} \times 100\%$$

$$\dfrac{90 \times 6}{100} = B.H.P$$

$$B.H.P = 5.4 \text{ H.P}$$

Ans: B.H.P of generator = 5.4 H.P

18 A machine is working on 80% efficiency I.H.P of machine is 50. Calculate the power lost in friction.

Formula: I.H.P = B.H.P + Frictional loses

$$\eta = \dfrac{B.H.P}{I.H.P} \times 100\%$$

Given data: Efficiency $\eta = 80\%$

$$I.H.P = 50$$

To find: Friction = ?

Solution: $\eta = \dfrac{B.H.P}{I.H.P} \times 100\%$

$$80 = \dfrac{B.H.P}{I.H.P} \times 100\%$$

$$80 = \dfrac{B.H.P}{50} \times 100\%$$

$$\dfrac{80 \times 50}{100} = B.H.P$$

$$B.H.P = 40$$

$$B.H.P = I.H.P - F.H.P$$

$$40 = 50 - F.H.P$$

$$40 + F.H.P = 50$$

$$F.H.P = 50 - 40 = 10$$

Ans: Loss of friction = 10 H.P

Assignment

1

Fig 1
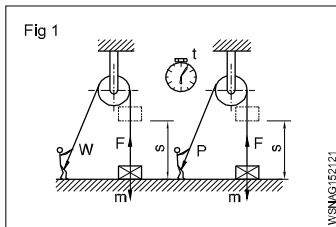
m= 55 kg

a) s = 1.82 metres
W = _____ joules

b) s = 1.40 metres
W= _____ joules

c) s = 0.85 metres
W = Joules

4

Fig 4
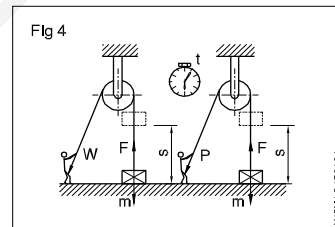
m = 75 kg

s = 100 metres

t = 12 secs

W = _____ Nm

P = _____ Watts

2

Fig 2
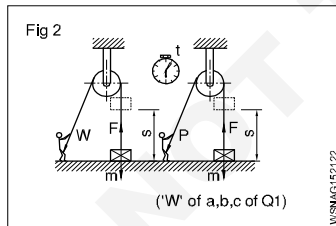
('W' of a,b,c of Q1)

t = 8 secs

a) P = _____ Watts

b) P = _____ Watts

c) P = _____ Watts

5

Fig 5

PUMP

V = 1 m³/min

H = 2 m
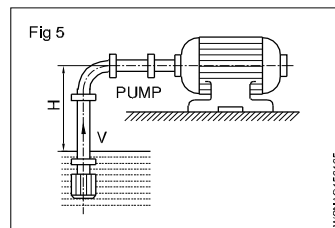
η = 0.75

Power input = _____ kW

3

Fig 3
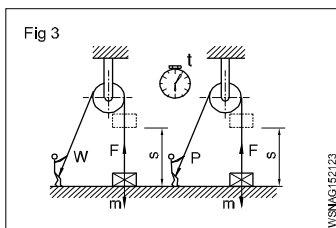
W = 1312.5 Joules

m = 350 kg

s = _____ metres

6

Fig 6

MASS
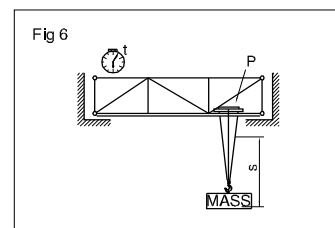
P = 12 kw

s = 4 metres

t = 20 secs

m = _____ kg

Heat & Temperature and Pressure - Concept of heat and temperature, effects of heat, difference between heat and temperature, boiling point & melting point of different metals and non-metals

Heat

It is a form of energy. Heat energy can be transformed into other forms of energies. Heat flows from a hotter body to a colder body. (Fig 1)

Fig 1
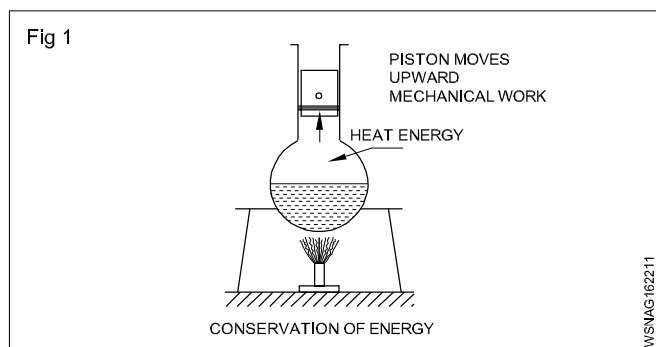
Units of heat

Calorie: It is the quantity of heat required to raise the temperature of 1 gram of water through 1°C.

BTHU: It is the quantity of heat required to raise 1 lb of water through 1°F. (British thermal unit).

C.H.U; It is the quantity of heat required to raise 1 lb of water through 1°C.

Joule : S.I. Unit (1 Calorie = 4.186 joule)

Effects of heat

• Change in temperature

• Change in size

• Change in state

• Change in structure

• Change in Physical properties

Specific heat

The quantity of heat required to raise the temperature of one gm of a substance through 1^0C is called specific heat. It is denoted by the letter 's'.

Specific heat of water	= 1
Aluminium	= 0.22
Copper	= 0.1
Iron	= 0.12

Thermal capacity:

It is the amount of heat required to raise the temperature of a substance through 1^0C is called the thermal capacity of the substance.

Thermal capacity = ms calories.

Calorific value: The amount of heat released by the complete combustion of unit quantity of the fuel (Mass or volume) is known as calorific value of fuels.

Water equivalent

It is the mass of water which will absorb the same amount of heat as the given substance for the same temperature rise. Water equivalent = Mass of the substance x specific heat of the substance.

Therefore water equivalent = ms

Types of heat

1   Sensible heat and

2   Latent heat

1   Sensible heat

Sensible heat is the heat absorbed or given off by a substance without changing its physical state. It is sensible and can be absorbed by the variation of temperature in the thermometers.

2   Latent heat

The heat gained or given by the substance during a change of state (from solid to liquid to gas) is called latent heat or hidden heat. The heat absorbed or given off does not cause any temperature change in the substance.

Types, 1. Latent heat of fusion of solid

2. Latent heat of vaporisation of solid.

1   Latent heat of fusion of solid

The amount of heat required per unit mass of a substance at melting point to convert it from the solid to the liquid state is called latent heat of fusion of solid. Its unit is cal/gram.

Latent heat of fusion of ice

The amount of heat required to convert per unit mass of the ice into water at 0^0C temperature is called latent heat of fusion of ice.

Latent heat of fusion of ice(L) = 80 cal/gram

2   Latent heat of vaporisation of liquid

The amount of heat required to vaporise a unit mass of liquid at its boiling point is called latent heat of vaporisation.

Latent heat of vaporisation of water or latent heat of steam

The amount of heat required to convert into steam of a unit mass of water at its boiling point (100^0C) is called latent heat of vaporisation of water or latent heat of steam.

Latent heat of steam(L) = 540 cal/gram

Temperature

It is the degree of hotness or coldness of a body. The temperature is measured by thermometers.

Difference between heat and temperature

Heat	Temperature
1 It is a form of energy.	This tells the state of heat.
2 Its unit is calorie.	Its unit is degree.
3 Heat is measured by calorimeter.	Temperature is measured by thermometer.
4 By adding quantity of heat of two substances their total heat can be calculated.	By adding two temperatures we cannot find the temperature of the mixture.
5 By heating a substance the quantity of heat is increased regardless of increase in temperature.	Two substances may read the same temperature though they might be having different amount of heat in them.

Boiling point

Any substance starts turning into a gas shows the temperature at which it boils this is known as the boiling point. The boiling point of water is 100^0C.

Melting point

The temperature at which any solid melts into liquid or liquid freezing to solid is called the melting point of substance. ` The melting point of ice is 0^0C.

List of melting point and boiling point of metals and Non -metals

Metals and Non-metals	Melting point °C	Boiling point °C
Aluminium	660.25	2519
Argon	-189.19	-185.85
Arsenic	817	614
Barium	729	1897
Beryllium	1287	2469
Bromine	-7.1	58.8
Cadmium	321.18	767
Calcium	839	1484
Carbon (diamond)	3550	4827
Carbon (graphite)	3675	4027
Chlorine	-100.84	-34.04
Cobalt	1495	2927
Copper	1084.6	2562
Gold	1064.58	2856
Helium	-	-268.93
Hydrogen	-259.98	-252.87
Iodine	113.5	184.3
Iridium	2443	4428
Iron	1535	2861
Lead	327.6	1749
Lithium	180.7	1342
Magnesium	650	1090

Metals and Non-metals	Melting point °C	Boiling point °C
Manganese	1246	2061
Mercury	-38.72	357
Molybdenum	2617	4639
Nickel	1453	2913
Nitrogen	-209.86	-195.79
Oxygen	-226.65	-182.95
Phosphorus (white)	44.1	280
Plutonium	640	3228
Potassium	63.35	759
Radium	700	1737
Silicon	1410	3265
Silver	961	2162
Sodium	98	883
Sulfur	115.36	444.6
Tin	232.06	2602
Titanium	1660	3287
Tungsten (wolfram)	3422	5555
Uranium	1132	4131
Zinc	419.73	907

Heat & Temperature and Pressure - Concept of pressure - Units of pressure, atmospheric pressure, absolute pressure, gauge pressure and gauges used for measuring pressure

Concept of pressure

Continuous physics force exerted on or against an object by something in contact with it.

Definition

Pressure is an expression of force exerted on a surface per unit area, i.e., the force applied is perpendicular to the surface of object per unit area.

$$\text{Pressure} = \frac{\text{Force}}{\text{Area}} = \frac{\text{Newton}}{\text{sq.meter}} = P = \frac{F}{A} \, N/m^2$$

As the amount of gas increases assuming the volume of chamber and the temperature remain constant the pressure increases.

Unit: Standard unit and also the S.I. unit of pressure is Pascal (Pa) and Metric unit of pressure is Bar.

1 Pascal is defined as a force of one newton per square metre

i.e.,   1 Pascal = 1 N/m^2

     1 Bar   = 10^5 N/m^2

Pressure units in different systems

British unit FPS	Pounds per square inch	lb/in^2
Metric units CGS	Gram per square centimetre	g/cm^2
MKS	Kilogram per square metre	kg/m^2
International unit SI	Newtons per square metre	N/m^2

Types of Pressure
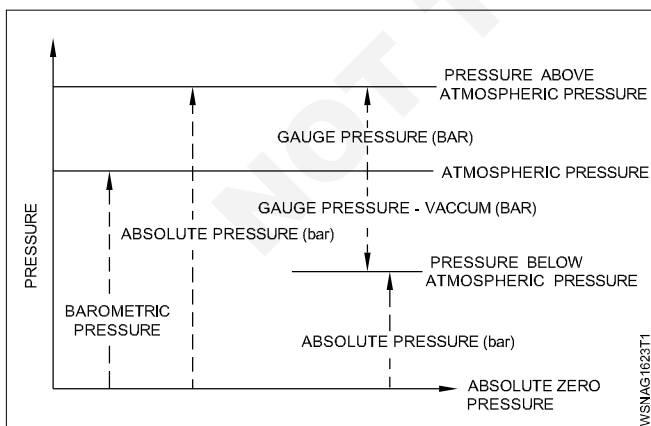
1   Absolute pressure

2   Atmosphere pressure

3   Gauge pressure

Measuring Instruments

I   Manometers

    a   Simple manometer

       i   Piezometer

       ii   'U' tube manometer

       iii   single column manometer

    b   Differential manometer

       i   'U' tube differential manometer

       ii   Inverted 'U' tube manometer

II   Mechanical Gauges

    a   Diaphragm pressure gauge

    b   Bourdon's tube pressure gauge

    c   Dead weight pressure gauge

    d   Bellows pressure gauge

Example

A liquid gives force of 100 N over an area of 2m^2. What is the pressure?

    Force   = 100 N

    Area   = 2 m^2

    Pressure   = ?

$$P = \frac{F}{A} = \frac{100}{2}$$

$$= 50 \, N/m^2$$

CONCEPT OF PRESSURE

Fig 1
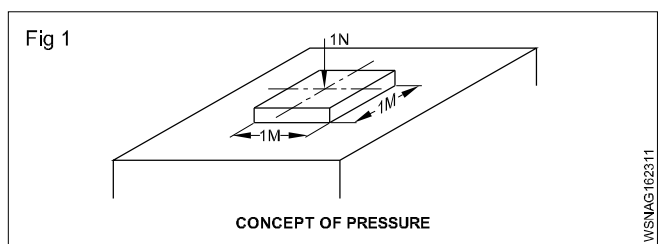
Unit of pressure N/m^2, 1 N/m^2 = 1 pascal.

This unit is too small (Pressure of a fly on a area of 1 cm^2). Hence 'bar' is introduced as the unit of pressure. 1 bar = 10^5 pascal.

$$10^5 \, P_a = 10^5 \, \frac{N}{m^2} = 10 \, \frac{N}{cm^2} = 1 \, bar$$

1 bar = 1000 mbar. [SI unit of Pressure is Pascal (Pa) and Metric unit of Pressure is bar]

Properties of Pressure

1   Liquid pressure increase with depth.

2   Liquid pressure depends upon the density of the liquid

3   The pressure is same in all directions about a point in liquid at rest

4   Upward pressure at a point in a liquid is equal to downward pressure

Pascal's Law

A French scientist, Pascal stated that the pressure applied at any point in liquid, at rest is transmitted equally in all directions. This is known as Pascal' law.

Applications of Pascal's law

Pascal's law is applied in many devices like the siphon, hydraulic press, hydraulic lift, brahma press, air compressor, rotary pump and hydraulic brake. These hydraulic machines are based on the principle of transmission of pressure in liquids.

Principle of Hydraulic press

Two cylinders having different cross sectional area are connected to each other by a horizontal connecting tube. The apparatus is filled with a liquid. The two cylinders are fitted with air tight piston .

By giving a small input force on a plunger of a small cross sectional area cylinder a large output force are produced on the ram of large cross sectional area cylinder. According to Pascal's law, small input pressure exerted on plunger is transmitted by the liquid to the ram without any loss. Therefore a small force can be used to lift a much large force or weight. (Fig 2)

PRINCIPLE OF HYDRAULIC PRESS
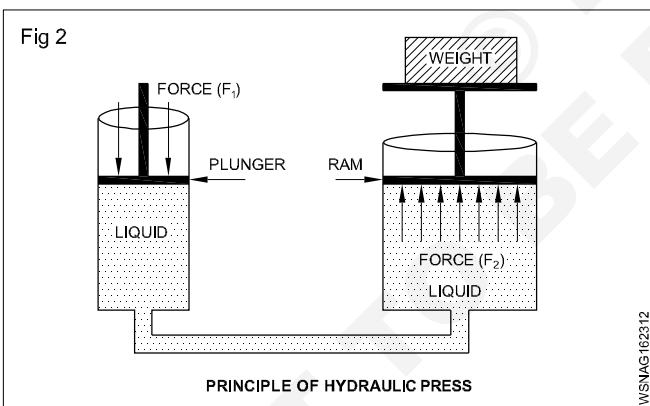
$$\frac{\text{Force on plunger(F)}}{\text{Plunger area(a)}} = \frac{\text{Weight on the ram(W)}}{\text{Ram area(A)}}$$

$$\frac{F}{a} = \frac{W}{A}$$

Weight on the ram (W) = $\frac{F \times A}{a}$

Properties of Air

• Actually speaking, air is a mixture of gases. Air is invisible, colourless, odourless, and tasteless.

• Composition: The main constituents of air by volume are 78% nitrogen, 21% oxygen, and 1% other gases such as argon and carbon dioxide.

• The gaseous layer of air around the earth is known as atmosphere

Pressure Relationship

• **Atmospheric pressure :** The air surrounding the earth exerts a pressure on the earth's surface. The pressure prevailing directly on the earth's surface is known as atmospheric pressure.

• The atmospheric pressure is also referred to as reference pressure. Normally it considers the sea level as its reference point.

• The atmospheric pressure may be calculated from the fundamental principle of barometer which states that the barometer reads the pressure due to the height of mercury (Hg) in the tube and its weight.

∴   Atmospheric pressure = ρ g h

Where (rho) ρ = Density of mercury (Hg) = 13600 kg/m^3

g = Acceleration due to gravity = 9.81 m/s^2, and

h = height of mercury (Hg) column = 760 mm of Hg at normal sea level.

Substituting the above values in equation, we get

Atmospheric pressure   = 13600 x 9.81 x 0.76

= 1,01,396 N/m^2

= 1.013 bar

But for easy and simple calculation, we take the atmospheric pressure as 1 bar.

1   **Absolute pressure:** absolute pressure is defined as the pressure which is measured with reference in absolute vacuum pressure.

2   **Gauge pressure:** It is defined as the pressure which is measured with the help of a pressure measuring instrument in which the atmospheric pressure is taken an datum. The atmospheric pressure on the scale is marked a zero.

3   **Vacuum pressure:** It is defined as the pressure below the atmospheric pressure.

Mathematically:

i)   Absolute pressure = Atmospheric pressure + Gauge pressure

P_{ab} = P_{atm} + P_g

ii)   Absolute pressure = Atmospheric pressure – Vacuum pressure

P_{ab} = P_{atm} - P_{vacc}

iii) Vacuum pressure = Atmospheric pressure – Absolute pressure

1 Atmospheric pressure = 76 cm of mercury = 33.91 ft of water

= 76 x 13.6 gm/cm^2

= 76 x 13.6 x 10^{-3} kg/cm^2

= 76 x 13.6 x 10^{-3} x 9.8 N/cm^2

= 10.13 N/cm^2

= 1.013 bar

= 1013 mbar [1 bar = 1000 mbar]

1 Pascal = 1 N/m^2

1 bar = 10^5 Pascal = 10^5 N/m^2 = 10 N/cm^2

1 bar = 0.986923 atmosphere

1 millibar = 0.01 N/cm^2 = 10^{-2} N/cm^2

1 atmospheric Pressure (FPS) = 14.7 Pound/inch^2 (psi)

1 atmospheric Pressure (Metric) = 1.0336 Kg/cm^2

1 atmospheric Pressure (Metric) = 1.014 x 10^6 dyne/cm^2

Effects of altitude on atmospheric pressure

Atmospheric pressure changes according to altitude a tabulation is shown here with variations.

> **For every 11 meter above sea level drop in air pressure is 1.3 m bar.**
>
> **For every 1000 ft above sea level drop in air pressure is 1" Hg (mercury)**

S. No.	Place	Unit of Pressure	Mercury column	Inch units
1	Sea level	1013 m bar	750 mm	14.7 psi
2	520 metres above sea level	951.5 m bar	700 mm	13.7 psi

Pressure gauges

They are instruments or devices used to measure the pressure of liquid steam or gas contained in a vessel. There are also known as mark meters.

Types of manometers

- Open tube
- Closed tube
- Differential type
- Inverted type

Mechanical pressure gauges

- Bourdon's pressure gauge
- Diaphragm pressure gauges
- Dead weight pressure gauges

Open tube manometer (Fig 3)

OPEN TUBE MANOMETER (OVER PRESSURE)
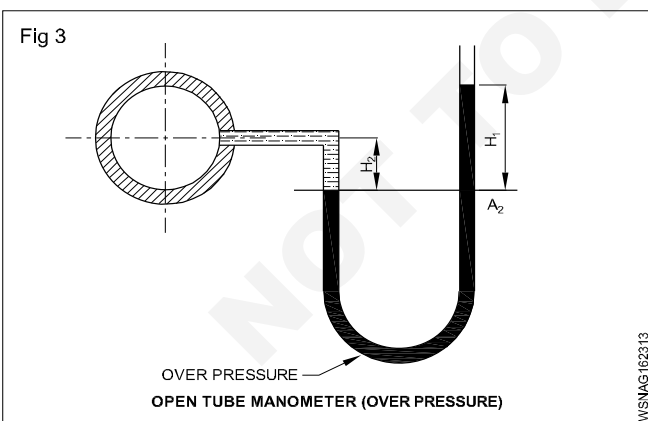
It is more suitable to measure pressure in vessels which is having little variation to atmospheric pressure. It is a 'u' shaped tube containing mercury having its one end connected to the vessel container in which the liquid is there whose pressure is to be determined. The other end is open. The manometer will show a difference in both the limbs of the tube when the pressure inside the vessel is more or less than the air pressure outside.

For a barometer reading with reference to an atmospheric pressure of 1 bar we have

P_a = 1 + P_o (shown in Fig 3)

P_a = 1 - P_u (shown in Fig 4)

OPEN TUBE MANOMETER (UNDER PRESSURE)
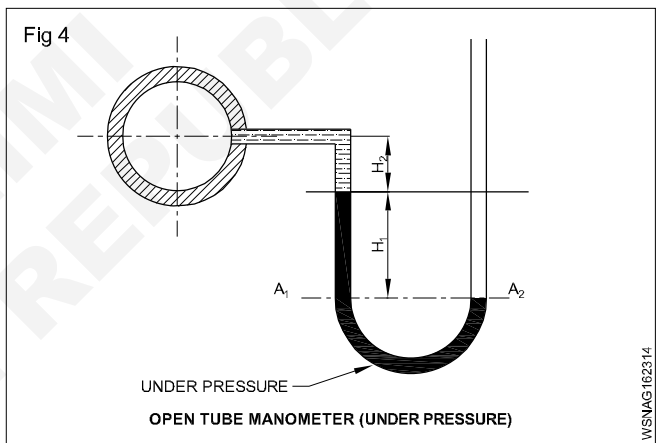
Example (Fig 5)

A manometer is connected to an air pressure tank and it indicates an over pressure of 615 mm pressure head. The external air pressure is 1015 mbar. Calculate the absolute pressure in bar and in Pascal (Fig 5).

OPEN TUBE MANOMETER
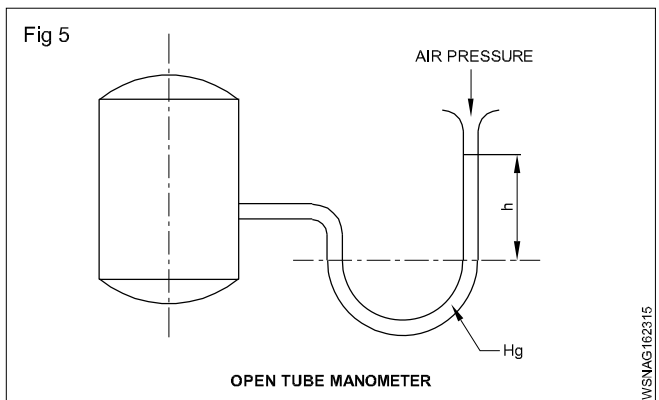
Absolute Pressure = External Air Pressure + Over Pressure

P_a = 1015 mbar + 100 mbar x 615 mm/750 mm

= 1835 mbar

P_a = 1.835 bar = 1.835 x 10^5 Pascal

> **If the barometer reading is in mm, it is always necessary to convert into m bar.**

Pressure and Vacuum gauges

Bourdon tube pressure gauges (Fig 6)

THE BOURDON PRESSURE GAUGE
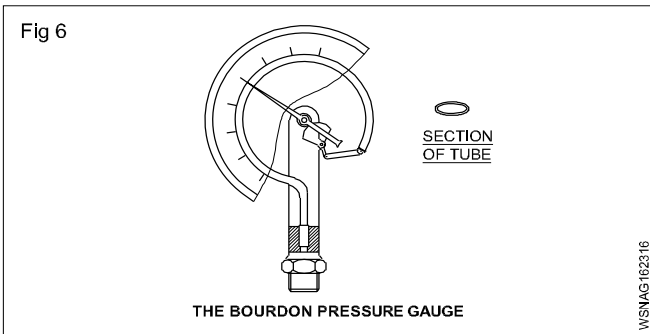
In I.C. Engines, Bourdon tube pressure gauges are widely employed for measurement of pressure, temperature and vacuum. In these gauges, a Bourdon tube which is a tempered, one is used and it attempts to straighten out under pressure and temperature and contact under vacuum.

The working is briefly described here refer to figure. A phosphor bronze tube or elliptical cross section is used and bent to an arc of a circle. The free end of the tube is sealed under internal pressure (or temperature), it attempts to straighten out. During this process, it operates sector, pinion and needle which indicates pressure or temperature over a calibrated dial. The entire unit is mounted on a casing and covered with glass and frame and around it.

Vacuum gauges

These are also of Bourdon tube type gauges where the tube attempts to contract under vacuum thus recording vacuum of the engine in mm Hg (millimeters of mercury)

> **A reading of 760 mm Hg is prefect vacuum (zero absolute pressure)**
>
> **A zero of say 300 mm Hg means to say that 300 mm of vacuum is equivalent to (760-300) 460 milliHg absolute pressure.**

* Vacuum gauges are often used by service mechanics to find out the mechanical condition of the engine and whether valves, ignition timing and carburetor setting are correct and carry out fine adjustments to obtain the best performance of the engine.

* **Vacuum in Diesel Engine governors:** This is measured by water column methods in fuel injection test bench

* **Vacuum in manifolds of an engine:** This can be measured by using vacuum gauge

* **Over-pressure:** The gas pressure of the tyre is bigger than the pressure of the atmosphere. In the tyre we have over pressure.

* **Under-pressure :** The gas pressure in the cylinder during the suction process is smaller. There is under pressure in the cylinder.

* **Absolute pressure:** The absolute pressure = air pressure + over-pressure. The pressure in vacuum is 0 bar.

The manometer indicates the over-pressure. The absolute pressure on the earth is normally 1 bar. The measured pressure plus 1 bar is the absolute pressure in normal conditions.

The unit for gas pressure is bar.

P_a = absolute pressure

P_o = over pressure

P_u = under pressure

Air pressure in technical calculations is assumed to be 1 bar.

Rules and examples

Absolute pressure = over-pressure + air pressure

$P_a = P_o$ + 1 bar

Over-pressure = absolute pressure - air pressure

$P_o = P_a$ - 1 bar

Under-pressure = air pressure - absolute pressure

P_u = 1 bar - P_a

Absolute pressure = air pressure - under-pressure

P_a = 1 bar - P_u

Examples

* What pressure is 2 bar over-pressure?

P_a = 2 bar + 1 bar = 3 bar

* What over-pressure is 4 bar?

P_o = 4 bar - 1 bar = 3 bar over-pressure

* How many bar under pressure is 0.7 bar?

P_u = 1 bar - 0.7 bar = 0.3 bar under-pressure.

* How many bar is 0.3 bar under-pressure?

0.7 bar.

Properties of gases

1 Charles's law

First law or law of volume

At constant pressure the volume (V) of a given mass of gas is directly proportional to its absolute temperature(T)

$$V \alpha T ; \frac{V}{T} = K \text{ (K - Constant)}$$

Second law or law of pressure

At constant volume the pressure (P) of a given mass of gas is directly proportional to its absolute temperature (T).

$$P \propto T \; ; \; \frac{P}{T} = K \; (K \text{ - Constant})$$

2 Boyle's law or Gas law

At constant temperature the volume (V) of a given mass of gas is inversely proportional to its pressure. (P)

$$V \propto \frac{1}{P} \; ; \; PV = K \; (K \text{ - Constant})$$

3 Perfect gas equation

Since boyle's law and charles's law can not be applied independently due to changes in pressure, volume and temperature a combined law called "gas equation" has been formulated. Gas equation is relating to pressure, volume and temperature of perfect gas which obeys both the boyle's law and charles's law. A gas which obeys boyle's and charles's law is called ideal gas.

As per boyle's law

$$V \propto \frac{1}{P} \qquad PV = K \; (\text{Constant}) \; P_1V_1 = P_2V_2 = K$$

As per charle's law

$$V \propto T \qquad \frac{V}{T} = K \; (\text{Constant}) \; \frac{V_1}{T_1} = \frac{V_2}{T_2} = K$$

Combining the above two laws,

$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2} = R \; [R = \text{gas constant}]$$

$$\frac{PV}{T} = R$$

$$PV = RT$$

P = Pressure (KN/m²)
V = Volume (m³)
m = Mass (Kg)
R = gas constant (Kgf.m/kg/k)
T = absolute temperature (K)

If mass of the gas is m, then

$$PV = mRT$$

Gas constant R = 29.27 kgf.m / kg/ k

$$= 287 \text{ joule/Kg/k}$$

True gas and its properties

1 It has mass and volume. So, it has weight.

2 It can be compressed or expanded into a container.

3 It is invisible.

4 General Gas Law

Boyle's, Charles', and Gay-Lussac's laws can be combined to obtain the general gas law is given by,

$$\frac{PV}{T} = \text{Constant} \; (\text{or})$$

$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2} = \frac{P_3V_3}{T_3} = \ldots\ldots\ldots \frac{P_nV_n}{T_n}$$

> **In the perfect gas law, the P and T represents absolute pressure and absolute temperature (in °K) respectively.**

1 1 kg of air at 5 kgf/cm² and 30°C is expanded to atmospheric pressure and 20°C. What will be the volume occupied?

Solution: Assuming atmospheric pressure is 1.033 kgf/cm² and gas constant

R = 29.27 kg m/kg/°K;

$P_1 = 5 \text{ kgf/cm}^2 = 5 \times 10^4 \text{ kg/m}^2$

$T_1 = 30°C = 30 + 273 = 303°$ Kelvin

Mass of air = m = 1 kg

Applying formula:

$$P_1V_1 = m.R.T_1$$

$$V_1 = \frac{m.R.T_1}{P_1}$$

$$= \frac{1 \times 29.27 \times 303}{5 \times 10^4}$$

$$= 0.1774 \text{ cubic metre}$$

The following information is ready:

$P_1 = 5 \times 10^4 \text{ kg/metre}^2$

$V_1 = 0.1774$ cubic metre

$T_1 = 303°K$

$P_2 = 1.033 \text{ kgf/cm}^2 = 1.033 \times 10^4 \text{ kg/metre}^2$

$T_2 = 20°C = 20 + 273 = 293°K$

Let V_2 = Volume occupied = To Find

Applying formula:

$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$$

$$V_2 = \frac{P_1V_1T_2}{P_2T_1}$$

$$= \frac{(5 \times 10^4) \times 0.1774 \times 293}{(1.033 \times 10^4) \times 303}$$

$$= 0.8303 \text{ cubic metre}$$

Volume occupied = 0.8303 cubic metre

2 Find the volume of a gas, if its absolute temperature doubled and the pressure is reduced to one half.

Solution: At initial stage:

Let initial pressure = P_1

Initial Volume = V_1

Initial temperature = T_1

At final stage:

P_2 = Final pressure

Since pressure is reduced to one half of initial pressure, we can say

$$P_2 = \frac{1}{2} P_1$$

T_2 = Final temperature

Since temperature is doubled, we can say

$$T_2 = 2T_1$$

V_2 = Volume of gas required = To Find

Applying formula

$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$$

$$V_2 = \frac{P_1V_1T_2}{T_1P_2}$$

$$= \frac{P_1V_1 2T_1}{T_1 \frac{1}{2}P_1}$$

$$= 4V_1$$

$$V_2 = 4V_1$$

Final volume = 4 times of initial volume

3 Find the pressure at the depth of 40 metres below the surface of a lake in dynes per sq. cm., the atmospheric pressure being neglected.

Solution:

Depth of water level ρ = 40 m = 4000 cm

Density of water d = 1 gram/cc

Acceleration due to gravity g = 980 cm/sec^2

Pressure below the surface of lake is given by the formula

$$= \rho.d.g.$$

$$\text{Pressure} = \rho.d.g$$

$$= 4000 \times I \times 980$$

= 3920000 dynes per sq. cm.

4 At 5 atmospheric pressure 0.2 cu. metre air is filled in a container. If the same air is filled at constant temperature in a 1 cu. metre volume of container then calculate the air pressure in the container.

Solution: At constant temperature the gas follows Boyle's Law

$$P_1V_1 = P_2V_2$$

Here, P_1 = 5, V_1 = 0.2 cu. metre, V_2 = 1 cu. metre

$$P_1V_1 = P_2V_2$$

$$5 \times 0.2 = P_2 \times 1.0$$

$$P_2 = \frac{5 \times 0.2}{1.0} = 1$$

Air pressure in the container = 1 atmospheric.

5 The column of mercury in a barometer is 76 cm. If instead of mercury the kerosene oil is filled in the barometer, what would be the state of column when relative density of kerosene oil is 0.8?

Solution: Suppose the height of column of kerosene in the mercury tube is h_2, then the pressure of column of kerosene = pressure of column of mercury. Assuming relative density of mercury = 13.6

$$h_2 d_2 g = h_1 d_1 g$$

$$h_2 = \frac{h_1 d_1 g}{d_2 g} = \frac{h_1 d_1}{d_2}$$

$$= \frac{76 \times 13.6}{0.8}$$

$$= 1292 \text{ cm}$$

= 12.92 metres

6 The volume of a gas at 770 mm pressure is 403 cc. Find the pressure when the volume is reduced to 341 cc.

As per Boyles Law

$$P_1V_1 = P_2V_2$$

$$770 \times 403 = P_1 \times 341$$

$$P_1 = \frac{770 \times 403}{341}$$

Pressure when volume is reduced **= 910 mm**

7 At 80 cm pressure the volume of a gas is 800 cu. cm. How much pressure be increased to bring the volume of gas at 200 cu. cm?

Pressure P_1 = 80 cm

Volume V_1 = 800 cu. cm

Volume V_2 = 200 cu. cm

As per Boyle's law

$$P_1V_1 = P_2V_2$$

$$80 \times 800 = P_2 \times 200$$

$$P_2 = \frac{80 \times 800}{200} = \frac{640}{2} = 320 \text{ cm}$$

Pressure to be increased = 320 - 80 = 240 cm

= 2.4 metres

8 A gas has a pressure of 2 kg/cm^2 and volume of 5m^3. What will be the volume of gas if the pressure is reduced to 1 kg/cm^2 keeping the temperature constant?

Gas pressure P_1 = 2 kg/cm^2

Volume V_1 = 5 m^3

Pressure P_2 = 1 kg/cm^2

As per Boyle's law

$$P_1 V_1 = P_2 V_2$$

$$V_2 = \frac{P_1 \times V_1}{P_2} = \frac{2 \times 5}{1}$$

Volume of gas = 10m³

9 A gas at 1.5 kgf/cm² occupying 0.2 m³ is at 20°C. It is compressed to a pressure of 5 kgf/cm² such that its volume becomes 0.03m³. What will be final temperature of the gas?

Temperature T_1 = 20°C = 20 + 273 = 293° Kelvin

Volume of gas V_1 = 0.2 m³

Pressure of gas P_1 = 1.5 kgf/cm²

                 = 1.5 x 10⁴ kgf/m²

    Volume V_2 = 0.03 m³

    Pressure P_2 = 5 kgf/cm²

                 = 5 x 10⁴ kgf/m²

As per perfect gas equation

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$T_2 = P_2 V_2 \times \frac{T_1}{P_1 V_1}$$

$$= 5 \times 10^4 \times 0.03 \times \frac{293}{1.5 \times 10^4 \times 0.2}$$

$$= \frac{439500}{1.5 \times 10^4 \times 0.2}$$

$$= \frac{439500}{3000}$$

$$= 146.5$$

T_2 = 146.5 Kelvin

        = 146.5 - 273

Final temperature of gas = -126.5° C

10 An automobile tyre contains 0.14 kg of air at 2 kg/cm² gauge pressure at 27°C. What is the volume of air in cubic cm?

In this sum gauge pressure is given. To solve it absolute pressure is necessary. Atmospheric pressure = 1.033 kg/cm²

Absolute pressure = Gauge pressure + Atmospheric pressure

        = 2 + 1.033

        = 3.033 kg/cm²

Pressure P = 3.033 kg/cm²

        = 3.033 x 10⁴ kg/m²

Weight of air m = 0.14 kg

Temperature T   = 27°C = 27+273

        = 300° Kelvin

Gas constant R = 29.27 kgm kg/ Kelvin

(or) 287 Joule / kg/ Kelvin

As per perfect gas equation

  PV = mRT

$$V = \frac{0.14 \times 29.27 \times 300}{3.033 \times 10^4}$$

$$= \frac{1229.34}{30330} = 0.0405 \text{ cu.m}$$

$$= 0.0405 \times 10^6$$

Volume of air = 40532 cu. cm

Assignment

1 At 10 atmospheric pressure 0.4 cu. metre air is filled in a container. If the same air is filled at constant temperature in a 2 cu. metre volume of container then calculate the air pressure in the container

2 The volume of a gas at 780 mm pressure is 413 cc. Find the pressure when the volume is reduced to 351cc.

3 A gas is transferred from one container of volume 100 cc. of a pressure of 1.5 kg/cm² into another container of capacity 200 cc. Find the pressure in the new container.

4 5 litre of air at 30°C and 1.1 atmospheric pressure is compressed to one litre and 10 atmospheric pressure. Calculate the temperature after compression.

Basic Electricity - Introduction and uses of electricity, electric current AC,DC their comparison, voltage, resistance and their units

Electricity is a kind of energy. It is the most useful sources of energy which is not visible but its presence can be felt by its effects. Electricity is obtained by conversion of other forms of energy like heat energy, chemical energy, nuclear energy, mechanical energy and energy stored in water etc.,

To understand electricity, one must understand the structure of an atom.

Basically an atom contains electrons, protons and neutrons. The protons and neutrons are located in the centre of an atom and the electrons, a negative electric charge particle revolving around the nucleus in an atom. The proton has a positive charge. Neutrons are neutral and have no charge.

Sources of electricity

Battery

Battery stores electrical energy in the form of chemical energy and it gives power when required. Battery is used in automobiles and electronics, etc.,

Generator

It is a machine which converts the mechanical energy into electrical energy.

When a conductor rotates between a magnetic field using prime mover an emf will be induced. By using this method all types of AC and DC generator - generates power.

E.g.   Thermal power station
         Hydro power station
         Nuclear power station
         Wind power station
         Solar power station

Thermo couple

If two dissimilar pieces of metals are twisted together and its joined end is heated in a flame, then a potential difference or voltage will be induced across the ends of the wires. Such a device is known as a Thermo couple. Thermo couple is used to measure very high temperature of furnaces.

Effects of electric current

When an electric current flows through a medium, its presence can be felt by its effects, which are given below.

1 Physical effect

Human body is a good conductor. when the body touches the bare current carrying conductor, current flows through the human body to earth and body gets severe shock or cause even death in many cases.

2 Magnetic effect

When an electric current passes through a coil, a magnetic field is produced around it.

E.g. : Electromagnet Motor, Generator, Electric bell

3 Chemical effect

When an electric current passes through an electrolyte, chemical action takes place. Because of that, an electrical energy is stored in a battery as a chemical energy.

E.g.: Electroplating, Cells and battery charging, refining of metals etc.,

4 Heating effect

When an electric current passes through any conductor, heat is produced in the conductor due to its resistance.

E.g. : Electric heater, Electric iron box, Electric lamp, Geyser, Soldering iron, Electric kettles, Electric welding etc.,

5 X-ray and Laser rays effect

When a high frequency voltage is passed through a vacuum tube, a special type of rays come out, which is not visible. These rays are called x-rays. Laser rays also can be produced by electric current.

6 Gas effect

When electrons pass through a certain type of sealed glass shell containing gas, then it emits light rays.

E.g: Mercury vapour lamp, Sodium vapour lamp, Fluorescent lamp, Neon lamp etc.,

Uses of Electricity

1	Lighting	- Lamps
2	Heating	- Heaters, ovens
3	Power	- Motor, fan
4	Traction	- Electromotive, lift, crane
5	Communication	- Telephone, telegraph, radio, wireless
6	Entertainment	- Cinema, radio, T.V.
7	Medical	- x-rays, shock treatment
8	Chemical	- Battery charging, electroplating
9	Magnetic	- Temporary magnets
10	Engineering	- Magnetic chucks, welding, x-rays of welding

Classification

• Static electricity

• Dynamic electricity

STATIC ELECTRICITY

If a dry glass rod is rubbed with silk cloth the glass rod gives out negative electrons, and therefore, becomes positively charged. The silk cloth receives negative electrons and therefore it becomes negatively charged. They acquire the property of attracting small pieces of paper etc. because like charges repel and unlike charges attract each other. The electric charge on the silk cloth is stationary and is called static electricity. This type of electricity cannot be transmitted from one place to another.

DYNAMIC ELECTRICITY

The electrons in motion are called current electricity or electric current. This type of electricity is carried through wires and cables. Therefore, this electricity can be transmitted from one place to another. This type of electricity can be produced by cells, batteries, generators alternators etc.

What is the difference between an atom and an element? How are molecules different from atoms? I am often asked these questions in my sessions over and over again and so I finally decided to write a comprehensive post on them. Find answers to all your questions in this section that is designed to help students explore and understand the relationship between atoms, elements, molecules, compounds and mixtures in a manner that is simple and easy to understand.

Types of electric current

• Direct current

• Alternating current

Direct current

In direct current (DC) the direction and magnitude of the current does not change (Fig 2). The steady current flow will be from the positive terminal to the negative terminal. (Fig 3)

Examples

DC Sources : Cells, batteries and DC generators (Fig 3)

Fig 1

DIRECT CURRENT (GRAPHIC REPRESENTATION)

Fig 2

CURRENT FLOWS FROM +VE TERMIINAL TO −VE TERMINAL

DIRECT CURRENT (D.C)
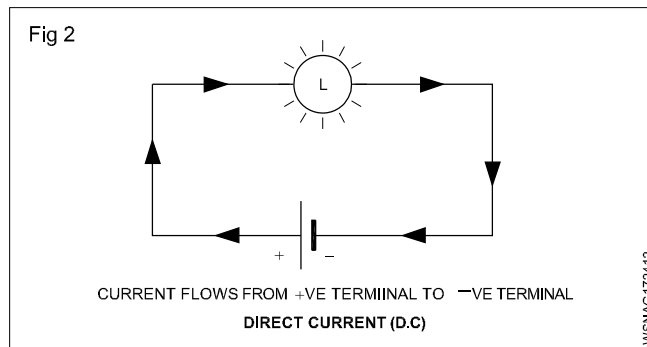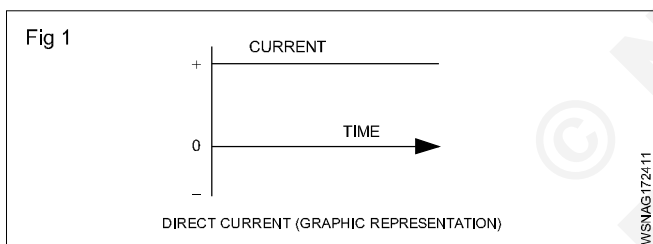
Alterating current (Fig 4)

The current flow will be from the phase terminal to the Neutral terminal. In the alternating current (AC) both the direction and magnitude of the current will be changing at definite intervals of time. The graph shows how an AC current or voltage changes with time. The current increases to the maximum value in one direction, falls to zero and increases to the maximum value in the other (opposite) direction before falling to zero again. Thus a cycle is one complete series of changes. The normal supply frequency is 50 cycles per second.

Fig 3

$(\frac{1}{50}$ SECONDS$)$

ALTERNATING CURRENT OR VOLTAGE
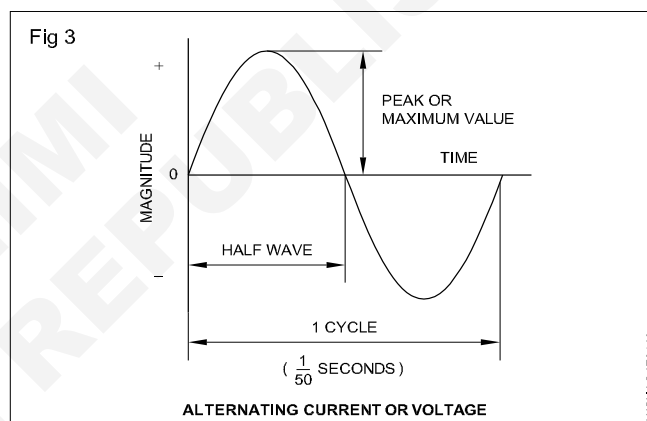
Difference between AC and DC

AC	DC
1 It is generated in the ranges of 6,600 V, 11000 V and 33,000 V.	It is generated up to 6,600 V only
2 Voltage can be stepped up or stepped down by using transformer	It is not possible
3 Transmission cost is less	Cost High
4 Less maintenance	High maintenance
5 Power up to 5,00,000 kw can be generated in a single alternator.	Power up to 10,000 kw can be generated in a single generator
6 AC generator can run at high speeds. So, speed control is not easy.	It can't run at high speeds. Speed control is easy.
7 Slip rings and brushes are used to collect the current.	Commutator and brushes are used to collect the current

Advantages of A.C.

i In transmission there is saving in copper wire.

ii Since there is no spark in A.C. machine there is no interference in Radio sound.

iii This can be produced to maximum voltage i.e. 33000 volts.

iv Voltage can be dropped or raised with the help of transformers.

v Its mechanism is simple and cheap.

vi Output is more due to availability of more than one phase.

Disadvantages of A.C.:

i   A single phase motor is not self-starter.

ii Due to thin wire in A.C., the voltage drop is more.

iii It cannot be used for electroplating and in charging secondary cells.

iv The speed of motors run by it is difficult to change.

v   There is danger to security due to high voltage.

Electrical terms and units

Quantity of electricity

The strength of the current in any conductor is equal to the quantity of electrical charge that flows across any section of it in one second. If 'Q' is the charge and 't' is the time taken then

$$I = \frac{Q}{t} \qquad Q = I \times t$$

The SI unit of current is coulomb. Coulomb is equivalent to the charge contained in nearly 6.24×10^{18} electrons.

Coulomb

In an electric circuit if one Ampere of current passes in one second, then it is called one coulomb. It is also called ampere second (As). Its larger unit is ampere hour (AH)

1 AH = 3600 As (or) 3600 coulomb

Electro motive force (EMF)

It is the force which causes to flow the free electrons in any closed circuit due to difference in electrical pressure or potential. It is represented by 'E.' Its unit is Volt.

Potential difference (P.D)

This is the difference in electrical potential measured across two points of the circuit. Potential difference is always less than EMF. The supply voltage is called potential difference. It is represented by V.

Voltage

It is the electric potential between two lines or phase and neutral. Its unit is volt. Voltmeter is used to measure voltage and it is connected parallel between the supply terminals.

Volt

It is defined as when a current of 1 ampere flows through a resistance of 1 ohm, it is said to have potential difference of 1 volt.

Current

It is the flow of electrons in any conductor is called current. It is represented by 'I' and its unit is Ampere. Ammeter is used to measure the current by connecting series with the circuit.

Ampere

When 6.24×10^{18} electrons flow in one second across any cross section of any conductor, the current in it is one ampere.(or) If the potential difference across the two ends of a conductor is 1 volt and the resistance of conductor is 1 ohm then the current through is 1 ampere.

Resistance

It is the property of a substance to oppose to the flow of electric current through it, is called resistance. Symbol: R, Unit : Ohm (Ω), Ohm meter is used to measure the resistance.

Ohm

If the potential difference across the two ends of conductor is 1 volt and the current through it is 1 ampere, then the resistance of the conductor is 1 Ohm.

Laws of resistance

The resistance offered by conductor depends on the following factors.

The resistance of the conductor

1   is directly proportional to the length of the conductor ($R \, \alpha \, L$)

2   Varies inversely proportional to its cross sectional area of the conductor $\left(R \; \alpha \; \dfrac{1}{A} \right)$

3   Depends on the material with which it is made.

Fig 4
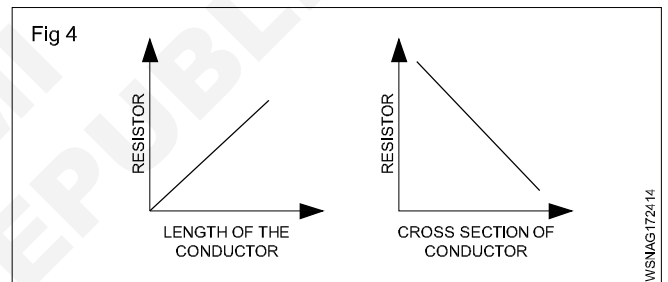
4   depends on the temperature of the conductor

$$R \; \alpha \; L \; ; \quad R \, \alpha \, \frac{1}{A}; \quad R \; \alpha \; \frac{L}{A}; \quad R \; = \; \rho \frac{L}{A}$$

Specific resistance

The specific resistance of a material is the resistance offered to a current it passed between the opposite faces of the unit cube of the material. Specific resistance is measured in Ohm - m or micro ohm - cm.

Each material has its own specific resistance or resistivity.

E.g. :   Copper - 1.72 $\mu\Omega$ cm, Silver - 1.64 $\mu\Omega$ cm, Eureka - 38.5 $\mu\Omega$ cm, Iron - 9.8 $\mu\Omega$ cm,

Aluminium - 2.8 $\mu\Omega$ cm, Nickel - 7.8 $\mu\Omega$ cm.

$R = \dfrac{\rho l}{A}$ ohm cm

R   =   Resistance in ohms

l   =   Length of the conductor in cm

r   =   Specific Resistance in ohm cm

(symbol pronounced as rho)

A   =   Area of cross - section in cm^2

Electric Power

In mechanical terms we defined power as the rate of doing work. The unit of power is Watt. In an electrical circuit also the unit of electrical power is 1 Watt. In mechanical terms 1 Watt is the work done by a force of 1 N to move the body through 1 metre in one second. In an electrical circuit, the electromotive force overcomes the resistance and does work. The rate of doing work depends upon the current flowing in the circuit in amperes. When an e.m.f of one volt causes a current of 1 ampere to flow the power is 1 Watt.

Hence Power = Voltage x Current

$$P = V \times I$$

Power in Watts = Voltage in Volts x Current in Amperes

Electric work, energy

Electrical work or energy is the product of electrical power and time

Work in Watt seconds = Power in Watts x time in sec

$$W = P \times t$$

Since 1 joule represents 1 Watt x 1 sec, which is very small, larger units such as 1 Watt hour and 1 kilowatt hour are used.

1 W.h	= 3600 Watt sec.
1 Kwh	= 1000 Wh = 3600000 Watt sec

Note: The charge for electric consumption is the energy cost per Kwh and it varies according to the country and states.

Fig 1

$$P = V \times I$$
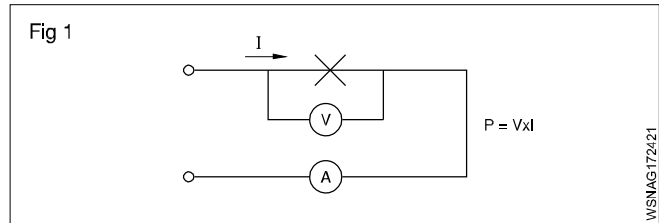
V - Voltage (Volts) V

i - Current Intensity (Amperes) A

P - Power (Watts, Kilowatts) W, kW

W - Work, Energy (Watt hour, Kilowatt hour) wh, Kwh

t - time (hours) h

Fig 2
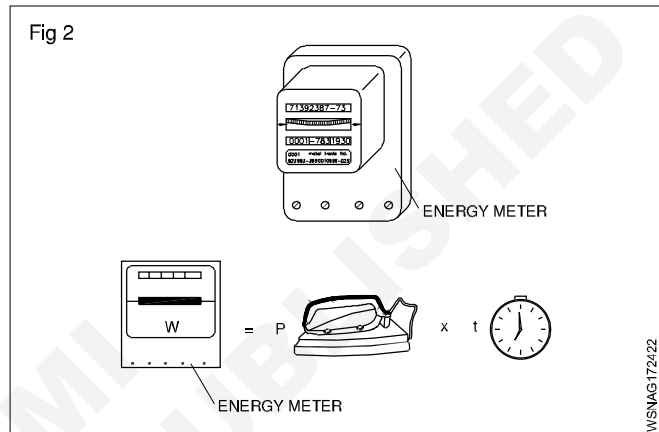
Table of analogies between mechanical and electrical quantities

Mechanical quantity	Unit	Electrical quantity	Unit
Force 'F'	N	Voltage 'V'	V
Velocity $v = \dfrac{\text{Displacement}}{\text{Time}}$	m/s	Current I	A
Time t	seconds	Time t	seconds
Power $P = F \times v$	$N\dfrac{m}{sec}$	Power $P = V \times i$	$W = V \times A$
Energy = $F \times v \times t$	$j = Nm$	Energy $W = V \times i \times t$	$j = W \times s$

$$\begin{aligned} W &= VI \\ &= I^2R \\ &= \frac{V^2}{R} \end{aligned}$$

$$\begin{aligned} R &= \frac{V}{I} \\ &= \frac{V^2}{W} \\ &= \frac{W}{I^2} \end{aligned}$$

$$\begin{aligned} V &= IR \\ &= \frac{W}{I} \\ &= \sqrt{WR} \end{aligned}$$

$$\begin{aligned} I &= \frac{V}{R} \\ &= \frac{W}{V} \\ &= \sqrt{\frac{W}{R}} \end{aligned}$$

Mensuration - Area and perimeter of square, rectangle and parallelogram

In Engineering field, an Engineer has to estimate the material, manpower, machinery, etc. required to prepare the geometrical objects. Hence we must be very conversant with all relevant formulae connected with geometrical objects.

Length   - l unit

Breadth or width - b unit

Diagonal   - d unit

Diameter   - d unit

Radius   - r unit

Semi perimeter - S unit

Perimeter   - P unit

Circumference   - C unit

Area   - A unit^2

Total surface area - T.S.A unit^2

Lateral surface area - L.S.A unit^2

Volume   - V unit^3

Square

This is also a four sided figure, opposite sides are parallel. All the four sides are equal. Angle between adjustment side are 90º.

Fig 1
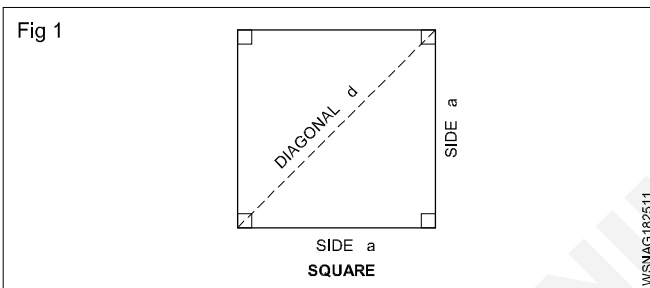
$A = a^2$ (or) unit^2

$P = 4a$ unit

$d = \sqrt{2}\ a$ unit

$a = \dfrac{d}{\sqrt{2}}$ unit where $\sqrt{2} = 1.414$

Find the area of a brass sheet in the form of a square whose perimeter is 31.2 cm.

Perimeter(P) = 4a = 31.2 cm

$\therefore a = \dfrac{31.2}{4} = 7.8$ cm

Area (A) = a^2

= 7.8 x 7.8 = 60.84 cm^2

Examples

1 Find out the circumference, diagonal and area of a square, whose side is 18 cm.

Side of the square (a)=   18 cm

Perimeter (P)   =   4a

                 =   4 x 18 = 72 cm

Diagonal (d)   = $\sqrt{2}$ x a

                 = $\sqrt{2}$ x 18 = 1.414 x 18

                 =   25.45 cm

Area (A)   = a^2

                =   18 x 18   = 324 cm^2

Perimeter of square   =   72 cm

Diagonal   =   25.45 cm ; Area = 324 cm^2

2 If the diagonal of a square measure 10 cm. Find area of the square.

Diagonal of the square (d)   = $\sqrt{2}\ a$ = 10 cm

Side (a)   = $\dfrac{d}{\sqrt{2}}$

Area (a^2) = $\dfrac{d}{\sqrt{2}}$ x $\dfrac{d}{\sqrt{2}}$ = $\dfrac{d^2}{2}$

            = $\dfrac{10^2}{2}$ = $\dfrac{100}{2}$

            = 50 cm^2

Area of the square   = 50 cm^2

3 The perimeter of one square is 748 cm and that of Another is 336 cm. Find the perimeter of a square and total area of the two squares.

Side of the square (a)   = $\dfrac{\text{Perimeter}}{4}$

1st square

Side (a)   = $\dfrac{\text{Perimeter of 1}^{st}\text{ square}}{4}$

           = $\dfrac{748}{4}$ = 187 cm

Area (A)   = a^2

          = 187 x 187

          = 34,969 cm^2

2nd square

Side (a)   = $\dfrac{\text{Perimeter of 2}^{nd}\text{ square}}{4}$

           = $\dfrac{336}{4}$ = 84 cm

Area (A)	= a²	

$$Area\ (A) = a^2$$
$$= 84 \times 84$$
$$= 7{,}056\ cm^2$$

Total area of two squares = 34,969 + 7,056
$$= 42{,}025\ cm^2$$

Assignment

1   Find the Area, Perimeter and diagonal of a square steel plate whose side measures 28.1 cm.

2   Find the area of a square whose diagonal is equal to 8.5 cm.

3   Find the area of the square if the side of the square is 28 cm.

4   Find its side if the area of the square field is 169 m².

5   Find the area of the square if the diagonal of the square is 20 cm.

6   Find the perimeter of a square whose diagonal is 144 m.

7   Find the area if the perimeter of a square plot is 48 m.

Rectangle

This is a four sided figure. Opposite sides are parallel. Angles between adjacent sides are 90°.

Fig 1
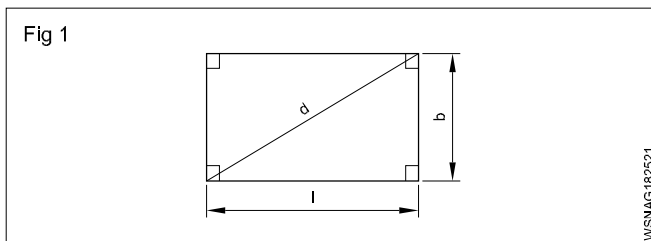
A = Area = length x breadth = l.b.unit²

P = Perimeter = 2 (l + b) unit

Diagonal = $\sqrt{l^2 + b^2}$ unit

Examples

1   Find the Area, Perimeter and diagonal of a rectangle whose length and breadth are 144 mm and 60 mm respectively.

Area = A $\quad = l \times b\ unit^2$

$\qquad = 144 \times 60 = 8640\ mm^2$

Perimeter = P $= 2\ (l + b)\ unit$

$\qquad = 2(144 + 60)$

$\qquad = 2 \times 204 = 408\ mm$

Diagonal = d $= \sqrt{l^2 + b^2}$ unit

$\qquad = \sqrt{144^2 + 60^2}$

$\qquad = \sqrt{20736 + 3600}$

$\qquad = \sqrt{24336} = 156\ mm$

2   The perimeter of a rectangle is equal to 42 cm. If its breadth is 9 cm. Find the length of the rectangle.

Perimeter $\quad$ = 42 cm

Breath $\qquad$ = 9 cm

Length $\qquad$ = ?

Perimeter $\quad$ = P = 2(l + b)

$\qquad$ 2(l + 9) = 42

$\qquad$ l + 9 $\quad$ = 42 ÷ 2

$\qquad$ l + 9 $\quad$ = 21

$\qquad$ l $\qquad$ = 21 - 9

$\qquad$ **l $\quad$ = 12 cm**

3   The perimeter of a rectangle is 48 cm and its length is 4 cm more than its width. Find the length and breadth of the rectangle.

Perimeter (P) = 48 cm

Breath (b) $\quad = x$

Length (l) $\quad = x + 4$

$\qquad$ 2(l + b) = Perimeter

$\qquad$ 2(x + 4 + x) $\quad$ = 48

$\qquad$ 2(2x + 4) $\qquad$ = 48

$\qquad$ 4x + 8 $\qquad$ = 48

$\qquad\qquad$ 4x $\quad$ = 48 - 8

$\qquad x \quad = \dfrac{40}{4} = 10$

$\qquad x \quad$ = breadth = 10 cm

length $\ = x + 4 = 10 + 4$ **= 14 cm**

4 How many rectangular pieces of 50 cm x 20 cm can be cut out from a sheet of 1000 cm x 500 cm.

   Sheet size = 1000 cm x 500 cm

 Size of the rectangular piece to be cut = 50 cm x 20 cm

No. of pieces to be cut in lengthwise = $\dfrac{1000}{50}$ = 20

No. of pieces to be cut in breadthwise = $\dfrac{500}{20}$ = 25

 Total no. of pieces to be cut out   = 20 x 25

                                   = 500

5 The perimeter of a rectangle is 320 metre. Its sides are in the ratio of 5:3. Find the area of the rectangle.

   Ratio   = 5:3 = l : b

length l   = $5x$

breadth b   = $3x$

2(l + b)   = Perimeter

2($5x + 3x$) = 320

2($8x$)   = 320

16x = 320

  x = $\dfrac{320}{16}$ = 20

  l = $5x$ = 5 x 20 = 100 m

  b = $3x$ = 3 x 20 = 60 m

Area   = l x b   (length = 100m, breath = 60m)

            = 100 x 60

Area   = 6000 m^2

Assignment

1 Find the area of a rectangular plot whose sides are 24 metres and 20 metres respectively. Also find the perimeter of the plot.

2 How many rectangular pieces of 5 cm x 4 cm will you get out of 65 cm x 30 cm brass sheet?

3 Find its breadth and area if the perimeter of a rectangle is 400 metre and its length is 140 m. .

4 Find its area, if the opposite sides of a rectangle are 64 cm and 25 cm respectively.

5 What is the width of the rectangle if a rectangle has an area of 224 cm^2 and length 16 cm.

6 What is the length of the diagonal of a rectangle with sides 16 cm and 12 cm?

7 Find the area of the rectangle if the perimeter of the rectangle is 100 cm and the ratio of its length and breadth is 3:2.

Parallelogram

This is also a four sided figure, opposite side being parallel to each other.
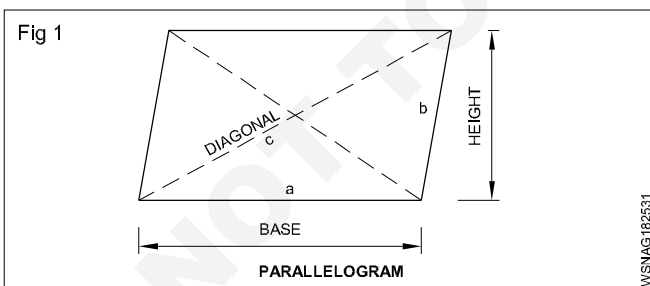
Area of parallelogram = base x height

   or = $2x\sqrt{s(s-a)(s-b)(s-c)}$

Where

   s = $\dfrac{a+b+c}{2}$

a and b are adjacent sides.

   P = 2(a+b)

Examples

1 The base and height of a parallelogram are 7.1 cm and 2.85 cm. Calculate its area.

      A = base x height units^2

         = 7.1 x 2.85

         = 20.235 cm^2

2 Find the height of a parallelogram whose area is 20 cm^2 and base is 10 cm.

      A = base x height units^2

      h = $\dfrac{area}{base}$

         = $\dfrac{20}{10}$

         = 2 cm

3. Two sides of a parallelogram are 12 cm and 8 cm. The diagonal is 10 cm long. Find the area of the parallelogram.

Area $\quad A \quad = 2x\sqrt{s(s-a)(s-b)(s-c)}$ units^2

$\quad s \quad = \dfrac{a+b+c}{2}$

$\qquad = \dfrac{12+8+10}{2}$

$\qquad = \dfrac{30}{2}$

$\qquad = 15$

$A \quad = 2x\sqrt{15(15-12)(15-8)(15-10)}$

$\quad = 2x\sqrt{15 \times 3 \times 7 \times 5}$

$\quad = 2x\sqrt{1575}$

$\quad = 2 \times 39.686$

Area $\quad A \quad = 79.37$ cm^2

Assignment

1 Find the area of a parallelogram, if its base and height are 8.1 cm and 30.8 cm respectively.

2 Find the area of a parallelogram, if the sides of a field in the shape of parallelogram are 12 m and 17 m and one of the diagonal is 25 m.

3 Find the base of a parallelogram whose height is 12 cm and area is 120 cm^2.

4 Find the height of a parallelogram whose base is 40 cm and area is 320 cm^2.

5 Find the area of the land if the sides of a land in the shape of a parallelogram are 24 m and 28 m respectively and one of the diagonal is 30 m.

6 What is the perimeter of parallelogram if base is 10 cm and other side is 5 cm?

7 Find the area of parallelogram if its base and height are 25 cm and 12 cm.

8 Find the base of a parallelogram if height is 15 cm and area is 150 cm^2.

9 Find the area of parallelogram if side is 5 cm, diagonal is 8 cm and diagonal bisects each other at right angles.

10 Find the height of a parallelogram if base is 80 cm and area is 640 cm^2.

11 Find the area of parallelogram if its base and height are 15 cm and 8 cm.

12 Calculate the perimeter and area of parallelogram if base, height are 12.7 cm, 5.5 cm and other side is 6.5 cm.

13 Find the height of parallelogram if the area is 20 cm^2 and base is 10 cm.

Mensuration - Surface area and volume of solids - cube, cuboid, cylinder, sphere and hollow cylinder

Cube

All sides of cube are same i.e length,breadth and height have same value. It is bounded by six equal square faces.

Volume of cube   = side x side x side

                       = a^3 unit^3

Lateral surface area = $4a^2$ unit^2

Total surface area   = 6 x side x side

                       = $6a^2$ unit^2 $\sqrt{3}$ = 1.732

Diagonal d   = $\sqrt{3}a$

CUBE
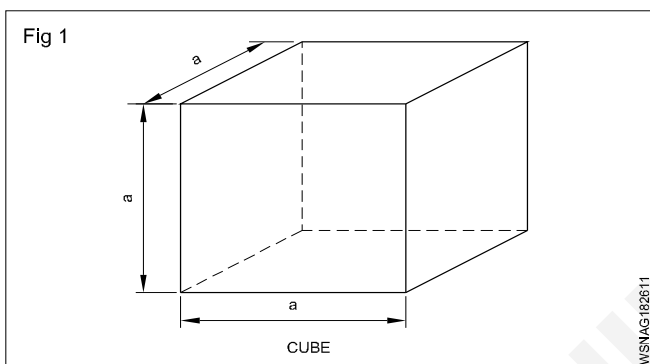
Rectangular solid (or) cuboid

Rectangular soild is bounded by six rectangular surfaces and opposite surfaces are equal and parallel to each other.

Volume of rectangular solid

                = Length x breadth x height

                = l . b . h unit^3

Lateral surface area = 2h(l+b) unit^2

Total surface area   = 2lb + 2bh + 2hl

                       = 2(lb+bh+hl) unit^2

RECTANGULAR SOLID (OR) CUBOLD
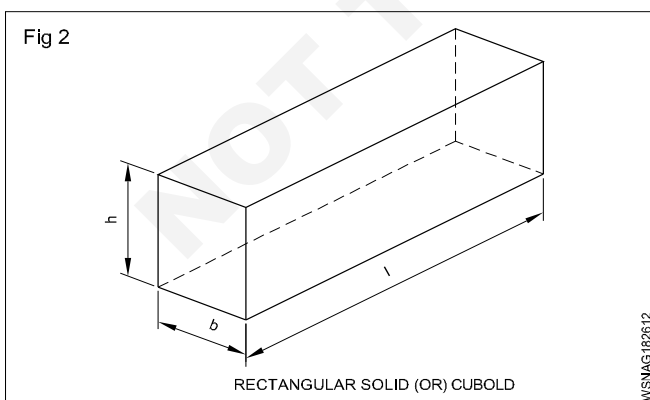
l = length, b = breadth and h = height

Cylinder

This is a prism whose top and bottom surfaces are equal and circular.

Volume of cylinder = $\pi r^2 h$ or $\dfrac{\pi}{4} d^2 h$
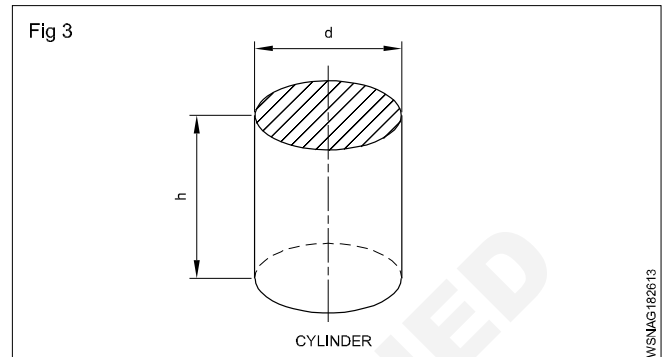
CYLINDER

Curved area of cylinder = 2πrh unit^2

Total surface area of cylinder = 2πr(h+r) unit^2

r = Radius of base , d = Diameter of base

h = Height of cylinder

Hollow cylinder

Hollow means empty space. In hollow cylinder there is an empty place. Water pipe is an example of hollow cylinder.
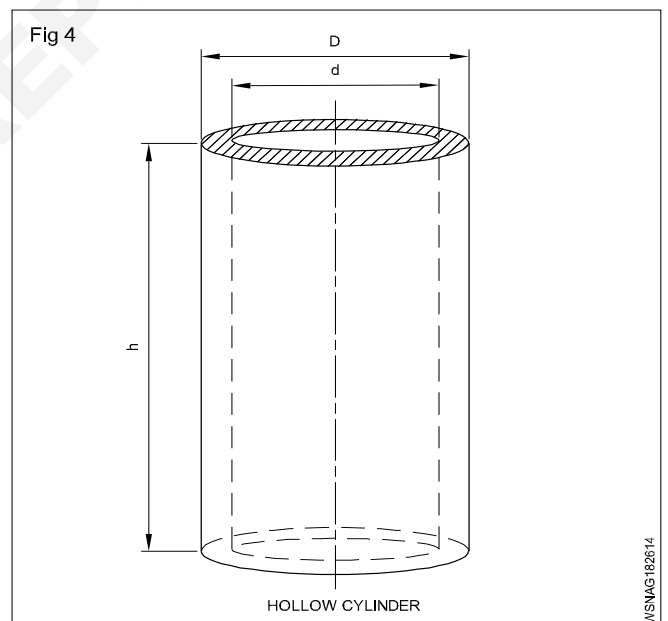
HOLLOW CYLINDER

Volume of hollow cylinder = $\pi (R^2 - r^2) h$ (or)

                              = $\pi (R + r) (R - r) h$ (or)

                              = $\dfrac{\pi}{4} (D^2 - d^2) h$ unit^3

                              = $\dfrac{\pi}{4} (D + d)(D - d) h$

Total surface area of hollow cylinder =

                    Inner + outer curved area + area of top and bottom circular part

∴ TSA : 2πRh + 2πrh + 2π(R^2 - r^2)

R = outer radius

r = inner radius

D = outer diameter

d = inner diameter

h = height of cylinder

t = thickness

Mean dia = $\dfrac{D - d}{2}$

If thickness given then:

Volume of hollow cylinder = π x mean dia x thickness x height

Finding out volumes of solids

The space occupied by a body is known its volume. The volume of a body indicates the capacity to hold substance in it.

The general form of Lateral surface area Total surface area and Volume is :

Lateral surface area = perimeter of the base x height

Total surface area = LSA + 2 (base area)

Volume = Area of base x height

Important and commonly used solids are described below one after another:

Cube

1 Find the diagonal, lateral surface area,, total surface area and volume of a cube of side 4.5 cm.

    side a = 4.5 cm

    diagonal d = $\sqrt{3}$a unit

              = 1.732 x 4.5

              = 7.794 cm

      L.S.A = $4a^2$ unit^2

              = 4 x 4.5 x 4.5

              = 81 cm^2

      T.S.A = $6a^2$ unit

              = 6 x 4.5 x 4.5

              = 121.5 cm^2

        V = a^3 unit^3

              = 4.5 x 4.5 x 4.5

      = 91.125 cc.

2 Calculate volume of a cube where side is 9 cm

        a = 9 cm

        V = ?

        V = a^3

          = 9 x 9 x 9

        = 729 cm^3

3 Find out side of the cube if a cube has volume of 3375cm^3.

      V = 3375 cm^3

      a = ?

      a^3 = 3375

      a = $\sqrt[3]{3375}$

        = $\sqrt{3 \times 3 \times 3 \times 5 \times 5 \times 5}$

        = 3 x 5

      = 15 cm

4 Find the side of a cube, if its surface area is 216 cm^2

    Surface area = T.S.A = 216 cm^2

      $6a^2$ = 216

      a^2 = $\dfrac{216}{6}$

        = 36

      a = $\sqrt{36}$

        = 6 cm

5 Find the side of the square tank, if its height is 2 metre and has the capacity to hold 50,000 litre of water.

    Height of square shape tank (h) = 2 m

      Capacity = 50,000 litre

      1000 litre = 1 m^3

      50,000 Litre = $\dfrac{50000}{1000}$

              = 50 m^3

    Capacity of tank = 50 m^3

      a^2 x h = 50

      a^2 x 2 = 50

      a^2 = $\dfrac{50}{2}$ = 25 m^2

      a = $\sqrt{25}$ = 5 m

Side of the square tank = 5 m

Rectangular Solid (or) Cuboid

1 Find its volume and T.S.A if a tank is 20 m long, 15 m broad and 12 m high.

      l = 20m

      b = 15 m

      h = 12 m

      v = ?

    T.S.A = ?

T.S.A = ?

Volume v = lbh unit^3

= 20 x 15 x 12

= 3600 m^3

T.S.A = 2(lb + bh + hl) unit^2

= 2((20 x 15) + (15 x 12) + (20 x 12))

= 2 (300 + 180 + 240)

= 1440 m^2

2 Find out its height if the cross section is 260 mm length and 180 mm wide rectangular and the capacity of a fuel tank is 10500 cm^3.

l = 260mm = 26 cm

b = 180 mm = 18 cm

v = 10500 cm^3

h = ?

l.b.h = volume

26 x 18 x h = 10500

$h = \dfrac{10500}{26 \times 18}$

= 22.44 cm

3 How many litres of water it can store if a water tank has the following dimensions length = 1 metre, width = 0.8 metre and height = 1.2 metre?

Volume = l x b x h unit^3

= 1 x 0.8 x 1.2

= 0.96 m^3 [1 m^3 = 1000 litres]

= 0.96 x 1000

= 960 litres of water can store in the tank.

4 Find its volume if the base of a prism is a rectangle having 5m length, 4m breadth and the height of the prism is 15m.

The base of prism is rectangle

Area of base = length x breadth

= 5 x 4

= 20 square m

Volume of prism = Area of base x Height

= 20 x 15

= 300 cm^3

Cylinder

1 Find the volume and total surface are of a cylinder having 9cm diameter and 15 cm height.

diameter = 9 cm

radius r = 4.5 cm

height h = 15 cm

Volume V = ?

T.S.A = ?

V = $\pi r^2 h$ unit^3

= $\dfrac{22}{7}$ x 4.5 x 4.5 x 15

= 954.4 cm^3

T.S.A = 2πr(h+r) unit^2

= 2 x $\dfrac{22}{7}$ x 4.5 (15 + 4.5)

= 2 x $\dfrac{22}{7}$ x 4.5 x 19.5

= 551.4 cm^2

2 Calculate the radius if the curved surface area of a cylindrical roller is 48π cm^2 and the roller is 10 cm long

C.S.A = 48π cm^2

length = 10 cm

radius = ?

2πrh = 48π

2 x π x r x 10 = 48π

$r = \dfrac{48 \times \pi}{2 \times \pi \times 10}$

= 2.4 cm

3 Find its radius if the volume of a cylinder is 5544 cm^3 and its height is 16 cm.

$\pi r^2 h$ = v

3.14 x r^2 x 16 = 5544

$r^2 = \dfrac{5544}{3.14 \times 16}$

$r^2 = \dfrac{5544}{50.24}$

= 110.35

r = $\sqrt{110.35}$

= 10.5 cm

4 Find the diameter of the tank if the volume of a circular tank is 68.46 m3, its height is 2 m.

$\pi r^2 h$ = 68.46

$r^2 = \dfrac{68.46}{3.14 \times 2}$

r^2 = 10.9

r = $\sqrt{10.9}$

= 3.3 m

diameter = 2r

= 2 x 3.3

= 6.6 m

5 A cylindrical vessel is to be made of 3 metre long and 1.9994 metre diameter. Calculate its surface area, if it is in a closed form on one end.

$$h = 3m$$
$$d = 1.9994 \text{ m}$$
$$r = 0.9997 \text{ m}$$

T.S.A = C.S.A + Base area

$$= 2\pi rh + \pi r^2$$

$$= (2 \times \frac{22}{7} \times 0.9997 \times 3) + (\frac{22}{7} \times 0.99997^2)$$

$$= 18.85 + 3.14$$

= 21.99 m²

6 How many litres of water a cylinder of radius 75 cm and height 100 cm can hold.

$$V = \pi r^2 h \text{ unit}^3$$
$$= 3.142 \times 75 \times 75 \times 100$$
$$= 1767375 \text{ cm}^3$$
$$= \frac{1767375}{1000} \quad [1000 \text{ cc} = 1 \text{ litre}]$$

= 1767.375 litres.

7 Calculate the height of cylindrical tin if a closed rectangular box 40 cm long, 30 cm wide and 25 cm deep has the same volume as that of cylinder tin of radius 17.5 cm.

Volume of cylinder = Volume of rectangular box

$$\pi r^2 h = l \times b \times h$$

$$\frac{22}{7} \times 17.5 \times 17.5 \times h = 40 \times 30 \times 25$$

$$h = \frac{40 \times 30 \times 25 \times 7}{22 \times 17.5 \times 17.5}$$

$$= \frac{210000}{6737.5}$$

= 31.17 cm

8 An oxygen cylinder is 15 cm in diameter and 100 cm in length. It is filled with gas under pressure so that every cm³ of the cylinder contains 120 cm³ of gas. How much cc of oxygen does this hold?

Volume of cylinder $= \pi r^2 h \text{ unit}^3$

$$= \frac{22}{7} \times 7.5 \times 7.5 \times 100$$

$$= 17678.57 \text{ cm}^3$$

Gas contain in 1 cm³ = 120 cm³ of gas

Gas contain in 17678.57 cm³ = 17678.57 x 120

$$= 2121428 \text{ cm}^3$$

Volume of oxygen = 2121428 cc.

Sphere

Sphere is a solid circular body.

Fig 5
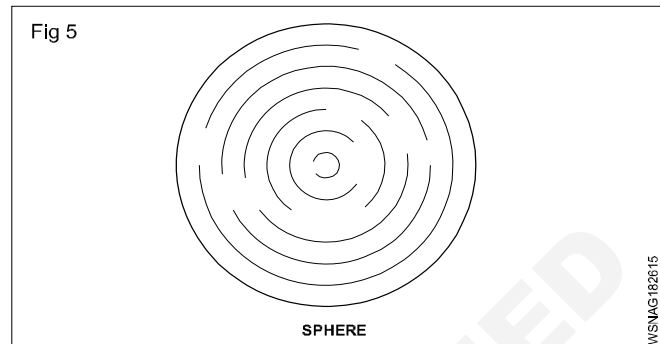
SPHERE

Volume of sphere $= \frac{4}{3}\pi r^3$ or

$$= \frac{\pi}{6}d^3 \text{ unit}^3$$

Total surface area of sphere $= 4\pi r^2 \text{ unit}^2$

Where r = Radius of sphere

d = Diametre of sphere

Radius $= \frac{1}{2}$ of diameter

1 Find the volume and surface area of a sphere of 3 cm radius.

$$V = \frac{4}{3}\pi r^3 \text{ unit}^3$$

$$= \frac{4 \times 22 \times 3 \times 3 \times 3}{3 \times 7}$$

$$= 113.1 \text{ cm}^3$$

Total Surface Area $= 4\pi r^2 \text{ unit}^2$

$$= 4 \times \frac{22}{7} \times 3 \times 3$$

= 113.1 cm²

2 Find the diameter of sphere having volume of 15625 cc.

$$\frac{4}{3}\pi r^3 = \text{Volume}$$

$$\frac{4}{3} \times \frac{22}{7} \times r^3 = 15625$$

$$r^3 = \frac{15625 \times 3 \times 7}{4 \times 22}$$

$$= \frac{328125}{88}$$

$$= 3728.69$$

$$r = \sqrt[3]{3728.69}$$

= 15.51 cm

diameter = 2 x radius

= 2 x 15.51

= 31.02 cm

3 How many spherical balls of 1 cm radius can be made from a sphere of 32 cm diameter.

No. of balls x volume of small sphere = Volume of bigger sphere

$$N \times \frac{4}{3} \times \pi r^3 = \frac{4}{3}\pi r^3$$

$$N \times \frac{\cancel{4}}{\cancel{3}} \times \cancel{\pi} \times 1^3 = \frac{\cancel{4}}{\cancel{3}} \times \cancel{\pi} \times r^3$$

N = 16 x 16 x 16

= 4096 balls

4 Three brass balls of diameters 3 cm, 4 cm and 5 cm are melted and make into one solid ball, if there is no wastage. Find the diameter of the solid ball.

1st ball d_1 = 3 cm,

r_1 = 1.5 cm

2nd ball d_2 = 4 cm,

r_2 = 2 cm

3rd ball d_3 = 5 cm,

r_1 = 2.5 cm

Diameter of new ball = ?

Volume of new ball = Volume of 3 spherical balls

$$\frac{4}{3}\pi r^3 = \frac{4}{3}\pi r_1^3 + \frac{4}{3}\pi r_2^3 + \frac{4}{3}\pi r_3^3$$

$$\frac{\cancel{4}}{\cancel{3}}\cancel{\pi} r^3 = \frac{\cancel{4}}{\cancel{3}}\cancel{\pi}(1.5^3 + 2^3 + 2.5)^3$$

$$r^3 = 3.375 + 8 + 15.625$$

$$r^3 = 27$$

$$r = \sqrt[3]{27}$$

$$r = \sqrt[3]{3 \times 3 \times 3}$$

$$r = 3 \text{ cm}$$

Diameter of the ball = 2 x r

= 2 x 3

= 6 cm

Assignment

Cube

1 Find the diagonal, lateral surface area, total surface area and volume of cube, whose side is 15 cm.

2 Find the volume of 10 cubes where each side is 5 cm.

3 Find its volume if a solid cube has each of its sides 60 mm long.

4 What is its side if the total surface area of a cube is 384 m².

Cuboid

1 Find the volume of the tank in m³, if the length is 60 m, breadth 40 m and height 20 m.

2 Find the volume of a C.I. casting of a rectangular block having 25 cm x 20 cm x 8 cm size.

3 Calculate the total surface area of a box whose length, width and height are 120 cm, 50 cm and 60 cm respectively.

4 Find the volume of the sheet if a brass sheet is of 25 cm square and 0.4 cm thick.

Cylinder

1 Find the curved surface area of cylinder whose diameter is 18 cm and height 34 cm?

2 Find the total surface area of cylinder whose diameter is 24 cm and height 40 cm?

3 Find out the volume of cylinder whose base is 10 cm radius and height is 40 cm?

Sphere

1 Find the volume of sphere having diameter 3.5cm?

2 Find the total surface area of a sphere having radius 1.75 cm?

3 How many spherical balls of 1 cm radius can be made from a sphere of 16 cm diameter.

4 Three balls of diameter 2m, 4cm and 6 cm are melted and made into one solid ball. If there is no wastage, find the diameter of solid ball.

Mensuration - Finding the lateral surface area, total surface area and capacity in litres of hexagonal, conical and cylindrical shaped vessels

Hexagonal bar

Volume of Hexagonal bar = Area of hexagonal x height

Lateral surface area of hexagonal bar

         = 6 x side of hexagon x length of the bar

or   = 3.464 x length of the bar x flat of hexagon

Total surface area of hexagonal bar

         = lateral surface area + (2 x area of hexagon)

Fig 1

TRIANGULAR PRISM   PENTAGONAL PRISM   HEXAGONAL PRISM

PRISM
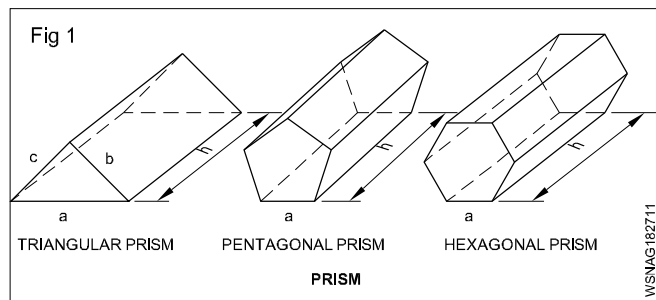
Cone

Cone is a pyramid with a circular base.

Fig 2
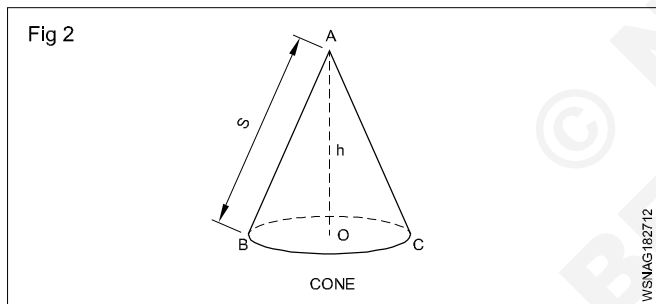
CONE

Volume of cone = $\frac{1}{3}\pi r^2 h$

or   = $\frac{\pi}{12}d^2 h$

Curved area = πrs

Total surface area = $\pi r(s+r)$

Where   r   = radius of base

       d   = diametre of base

       h   = vertical height of cone

       s   = slant height $\sqrt{r^2 + h^2}$

Frustum of a cone

When a cone is cut by a plane parallel to the base, and upper part is removed, the formation appears, is termed as frustum of a cone. Buckets, oil cans etc.are such frustums in shape.

L.S.A = $\pi l (R + r)$ unit^2

Fig 3

D = BASE DIA
d = UPPER DIA
ℓ = SLANT HEIGHT
h = VERTICAL HEIGHT
A_1 = TOP AREA (πr^2)
A_2 = BASE AREA (πR^2)
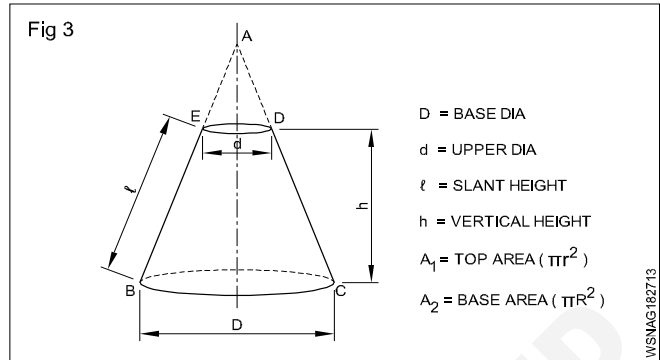
TSA = $\pi l (R + r) + A_1 + A_2$ unit^2

$V = \frac{\pi}{3}h (R^2 + Rr + r^2)$ unit^3

[A_1 = Top area ; A_2 = Bottom area]

Cylinder

This is a prism whose top and bottom surfaces are equal and circular.

Volume of cylinder = $\pi r^2 h$ or $\frac{\pi}{4}d^2 h$


Fig 4
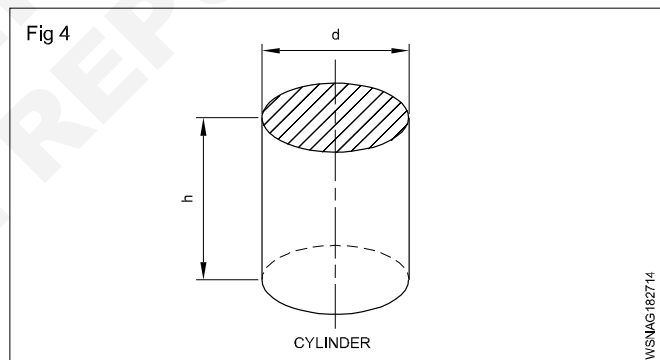
CYLINDER

Curved area of cylinder = $2\pi rh$

Total surface area of cylinder = $2\pi r(h+r)$

r = Radius of base, d = Diameter of base

h = Height of cylinder

Hollow cylinder

Hollow means empty space. In hollow cylinder there is an empty place. Water pipe is an example of hollow cylinder.

Volume of hollow cylinder = $\pi (R^2 - r^2)$ h (or)

                = $\pi (R + r) (R - r)$ h (or)

                = $\frac{\pi}{4} (D^2 - d^2)$ h

                = $\frac{\pi}{4}(D + d)(D - d)h$

Total surface area of hollow cylinder =

         Inner + outer curved area + area of top and bottom circular part

Fig 5
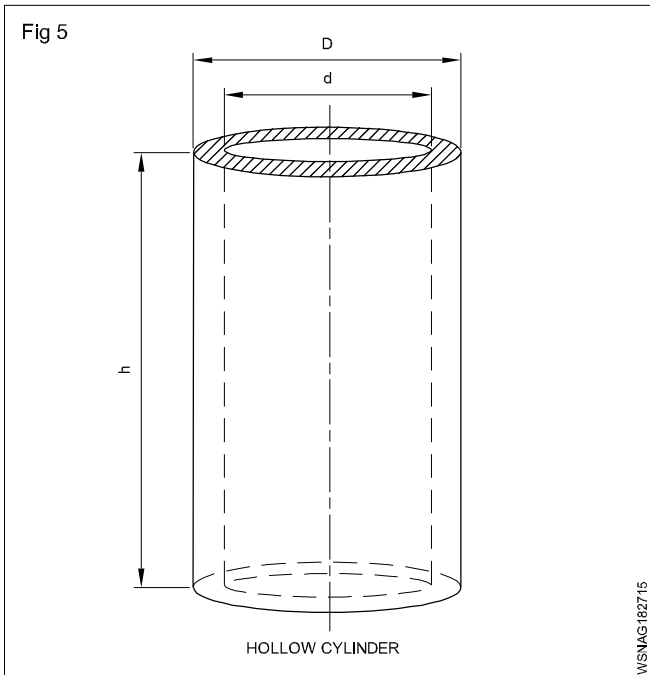
HOLLOW CYLINDER

$\therefore$ TSA : $2\pi Rh + 2\pi rh + 2\pi(R^2 - r^2)$

R = outer radius

r = inner radius

D = outer diameter

d = inner diameter

h = height of cylinder

t = thickness

Mean dia = $\dfrac{D - d}{2}$

If thickness given then:

Volume of hollow cylinder = π x mean dia x thickness x height

Example

1 Find the volume of an hexagonal prism having its side 20 cm and height 200 cm.

Side of hexagonal prism (a) = 20 cm

Height (h) = 200 cm

Volume (V) = Base side area x Height

= $6 \times \dfrac{\sqrt{3}}{4} \times a^2 \times h$

= $6 \times \dfrac{\sqrt{3}}{4} \times 20 \times 20 \times 200$

= $1,20,000 \times \sqrt{3}$

= $1,20,000 \times 1.732$

= **2,07,840 cm³**

Volume of the hexagonal prism = 2,07,840 cm³

2 Calculate the height. Also find the lateral surface area if a cone has a base diameter of 210 mm and its volume is 3056 cm3.

Fig 6
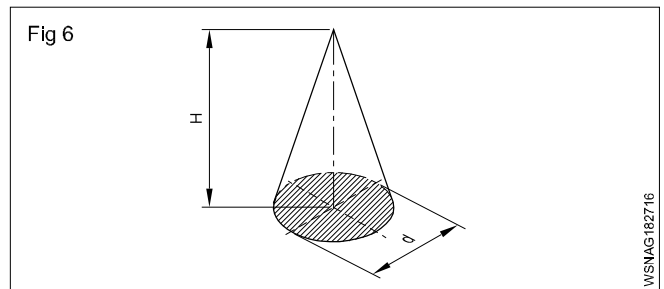
Volume of a cone = $\dfrac{1}{3}$ x Area of base x height

3056 cm³ = $\dfrac{1}{3}$ x 0.785 x 210²mm² x H

H = $\dfrac{3056 \times 3 \times 1000 mm^3}{0.785 \times 210^2 mm^2}$ = 264.82 mm

L = Slant height = $\sqrt{264.83^2 + 105^2}$ = 284.9mm

Lateral surface area = $\dfrac{1}{2} \pi$ X 210 X 284.9mm²

= 94017 mm² = 940.17 cm²

3 Determine its diameter in mm if the height of a rod of 1.6 metres and its volume is 1.017 metre³.

V = A x H

1.017 m³ = 0.785d² x 1.6 metres

0.785d² = $\dfrac{1.017}{1.6}$ m²

d² = $\dfrac{1.017}{1.6 \times 0.785}$ m²

= $\dfrac{1.017}{1.6 \times 785}$ m²

d = $\sqrt{\dfrac{10170}{16 \times 785}}$ metre

= $\sqrt{\dfrac{10170}{12560}}$

= $\sqrt{0.8097}$

= 0.8998

= 899.8mm

Levers & Simple machines - Effort and load, mechanical advantage, velocity ratio, efficiency of machine, relationship between efficiency, velocity ratio and mechanical advantage

Introduction

A machine is a tool containing one or more parts that uses energy to perform an intended action. Machines are usually powered by mechanical, chemical, thermal, or electrical means, and are often motorized. Historically, a power tool also required moving parts to classify as a machine. However, the advent of electronics has led to the development of power tools without moving parts that are considered machines.

A simple machine is a device that simply transforms the direction or magnitude of a force, but a large number of more complex machines exist. Examples include

1. Levers
2. Screw Jack
3. Wheel and axle
4. Pulleys
5. Inclined plane, etc.,

Load (or) Weight

The force overcome by the effort is called load or weight (W).

Effort (or) power

The force applied to lift the load is called effort or power (P).

Fulcurm

It is a fixed point in the machine around which the machine rotates (F).

Mechanical advantage

In a simple machine when the effort (P) balances a load (W) the ratio of the load to the effort is called the mechanical advantage of the machine. It is simply expressed in a number.

$$\text{Mechanical advantage (M.A)} \quad = \frac{\text{Load}}{\text{Effort}} = \frac{W}{P}$$

Velocity ratio

It is the ratio between the distances moved by the effort to the distance moved by the load. It is also expressed in a number.

$$\text{Velocity ratio} = \frac{\text{Distance moved by effort (dp)}}{\text{Distance moved by load (dw)}}$$

Efficiency of Machine

The ratio of output to the input of machine is known as efficiency. In simple machines, the ratio of mechanical advantage to the velocity ratio is also known as efficiency of machine. Efficiency is generally expressed in percentage.

$$\text{Efficiency} = \frac{\text{Output}}{\text{Input}} \times 100$$

$$\boxed{\text{\% Efficiency} = \frac{\text{Output}}{\text{Input}} \times 100}$$

Relation between M.A., V.R. and η

$$\text{Efficiency} = \frac{\text{Output}}{\text{Input}} = \frac{\text{Load} \times \text{Distance moved by load}}{\text{Effort} \times \text{Distance moved by effort}}$$

$$= \frac{\text{Load}}{\text{Effort}} \times \frac{\text{Distance moved by load}}{\text{Distance moved by effort}}$$

$$= \text{Mechanical advantage} \times \frac{1}{\text{Velocity ratio}}$$

$$\boxed{\text{Efficiency} (\eta) = \frac{\text{Mechanical advantage}}{\text{Velocity ratio}} = \frac{\text{M.A.}}{\text{V.R.}} \times 100}$$

Ideal Machine

In an ideal machine the mechanical advantage is equal to the velocity ratio. so, efficiency is 100% or unity.

Examples

1 Calculate the mechanical advantage, velocity ratio and efficiency if a machine mass of 120 kg is lifted to a height of 5 metre by a force of 60 kg. moving 15m.

Load (w) = 120 kg

Distance moved by load = (dw) = 5 m

Power (P) = 60 kg
Distance moved by power (dp) = 15 m

$$MA = \frac{W}{P} = \frac{120 \, \text{kg}}{60 \, \text{kg}} = 2$$

$$VR = \frac{dp}{dw} = \frac{15}{5} = 3$$

$$\text{Efficiency}(\eta) = \frac{MA}{VR} \times 100\%$$

$$= \frac{2}{3} \times 100$$

$$= 66.66 \, \%$$

2 Calculate the mechanical advantage and efficiency of machine, if effort applied 300 kg a load of 900 kg is lifted by a simple machine having a velocity ratio of 4.

Load (W)   =   900 kg

Effort (P)   =   300 kg

Velocity ratio (V.R)   =   4

Mechanical advantage (M.A.) $= \dfrac{\text{Load (W)}}{\text{Effort (P)}}$

$= \dfrac{900}{300}$

$= 3$

Efficiency $(\eta) = \dfrac{\text{M.A.}}{\text{V.R.}} \times 100\%$

$= \dfrac{3}{4} \times 100\%$

$= 75\%$

3 **Calculate Mechanical advantage, work done and horse power required if it is raised to a height of 6 m in 27 sec.and using a pulley block, a weight of 180 kg is raised with a force 15 kg.**

W	=	180 kg
P	=	15 kg
M.A.	=	?
Work done	=	?
HP	=	?
Height	=	6 m
t	=	27 second
M.A.	=	M.A.$= \dfrac{W}{P} = \dfrac{180 \text{ kg}}{15 \text{ kg}} = 12$
Work done	=	F x d (Force x Distance)
	=	15 kg x 6 m

Work done = **90 m - kg**

Power = Workdone / time

$= \dfrac{90 \text{ m kg}}{27 \text{ s}}$

$= \dfrac{90}{27}$ m kg/s [75m kg/sec=1HP]

$= 90/27 \times 1/75$ H.P.

$= 0.04444$ H.P.

4 **Calculate the applied force if a Load of 400 kg is lifted by a machine having an η of 72%. If velocity ratio = 6?**

W	=	400 kg
η	=	72 %
V.R.	=	6
η	=	$\dfrac{\text{M.A.}}{\text{V.R.}} \times 100$
72	=	$\dfrac{\text{M.A.}}{6} \times 100$
M.A.	=	$\dfrac{72 \times 6}{100}$
$\dfrac{W}{P}$	=	4.32
$\dfrac{400 \text{ kg}}{P}$	=	4.32
Applied Force P	=	$\dfrac{400}{4.32} = 92.59$ kg.

Assignment

1   Calculate the efficiency of a machine having velocity ratio 5 if a force of 275 kg applied to lift a weight of 1100kg with the help of simple machine.

2   Calculate (i) Mechanical advantage (ii) Efficiency of machine if the effort applied is 250 kg and a load of 1000 kg is lifted by a simple machine having a velocity ratio of 5.

3   What effort would be required and what would be the mechanical advantage if a lifting machine having a velocity ratio of 25, lifts a load of 40 Kg with an efficiency of 54.4% ?

4   Find out the effort required if the velocity ratio of a weight lifting machine is 20. If the efficiency of the machine is 40%.

5   Find the mechanical advantage if using a pulley block a load of 350 N is raised with a force of 25N.

6   Calculate M.A. η of the machine, if the effort applied is 250 kg and a load of 1000 kg is lifted by a simple machine having a velocity ratio 5.

7   Find out the η of the machine of effort applied is 300 kg if load of 1200 kg is lifted using simple machine having a velocity ratio of 5.

8   Calculate M.A. and efficiency if in a simple machine the velocity ratio is found to be 20. An effort of 20 kg is required to lift a load of 400 kg.

9   What is the velocity ratio, if its efficiency is 0.75 and in a lifting machine an effort of 31 kg just raises a load of 1000 kg?

Levers & Simple machines - Lever and its types

Lever

A lever is a rigid rod which rotates about a fixed point called the fulcrum.

E.g. : Cutting plier, A pair of scissors, Crow bar, Beam balance, Hand pump.

The distance of the load from the fulcrum is called the load arm. The distance of the effort from the fulcrum is called the effort arm.

Principle of Lever

*   All levers are functioning in the following principle

    Load x Load arm = Effort x Effort arm

*   **Classification of lever**

1   Straight lever

2   Curved lever

1   Straight lever

There are three types :

1   First order lever

2   Second order lever

3   Third order lever

First order lever

In this type the fulcrum lies between the load and the effort.

E.g : A pair of scissors, See-saw, Crow bar, Beam balance, Hand pump, etc.,
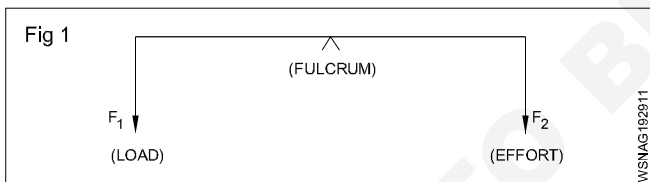
In this type of lever the mechanical advantage will be equal or less than or greater than 1 (M.A < = > 1)

Second order lever

In this type, the load lies between the fulcrum and the effort.

E.g : Nut cracker, Wheel barrow, Paper sheet cutter, Bottle openers, Lime squeezer, etc.,
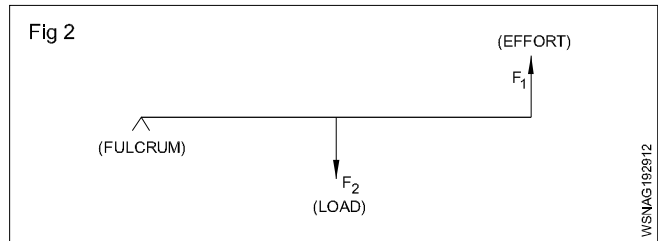
In this type of lever, the mechanical advantage will be greater than 1 (M.A. > 1). Less effort is used to lift more load.

Third order lever

In this type, the effort lies between the fulcrum and the load.

E.g. The human force arm, forceps, broom, fire tongs, fishing rod.
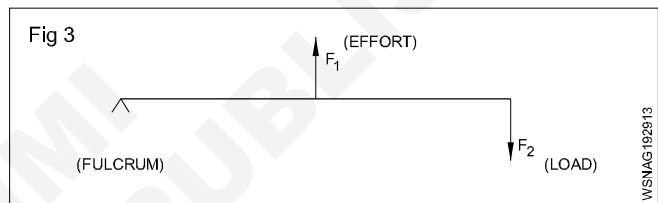
In this type of lever, the mechanical advantage will be less than 1 (M.A < 1) more effort is used to lift less load.

Bell cranked levers (Curved levers) (Fig 5)

In addition to the above types of levers, two rods may be joined together at an angle to increase leverage without utilising much space. Such levers are cranked levers and the special form in which included angle is 90°, is called the bell cranked lever.

E.g : Motor cycle breaks system clutch pedal.

BELL CRANKED LEVER
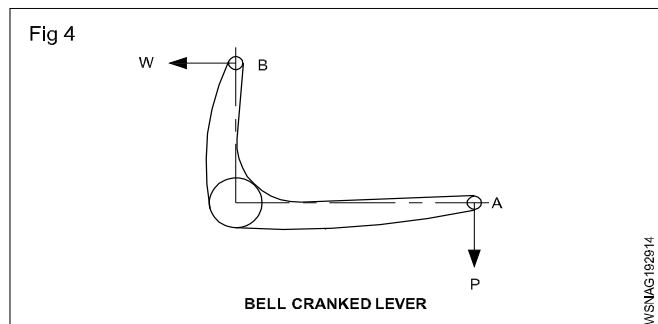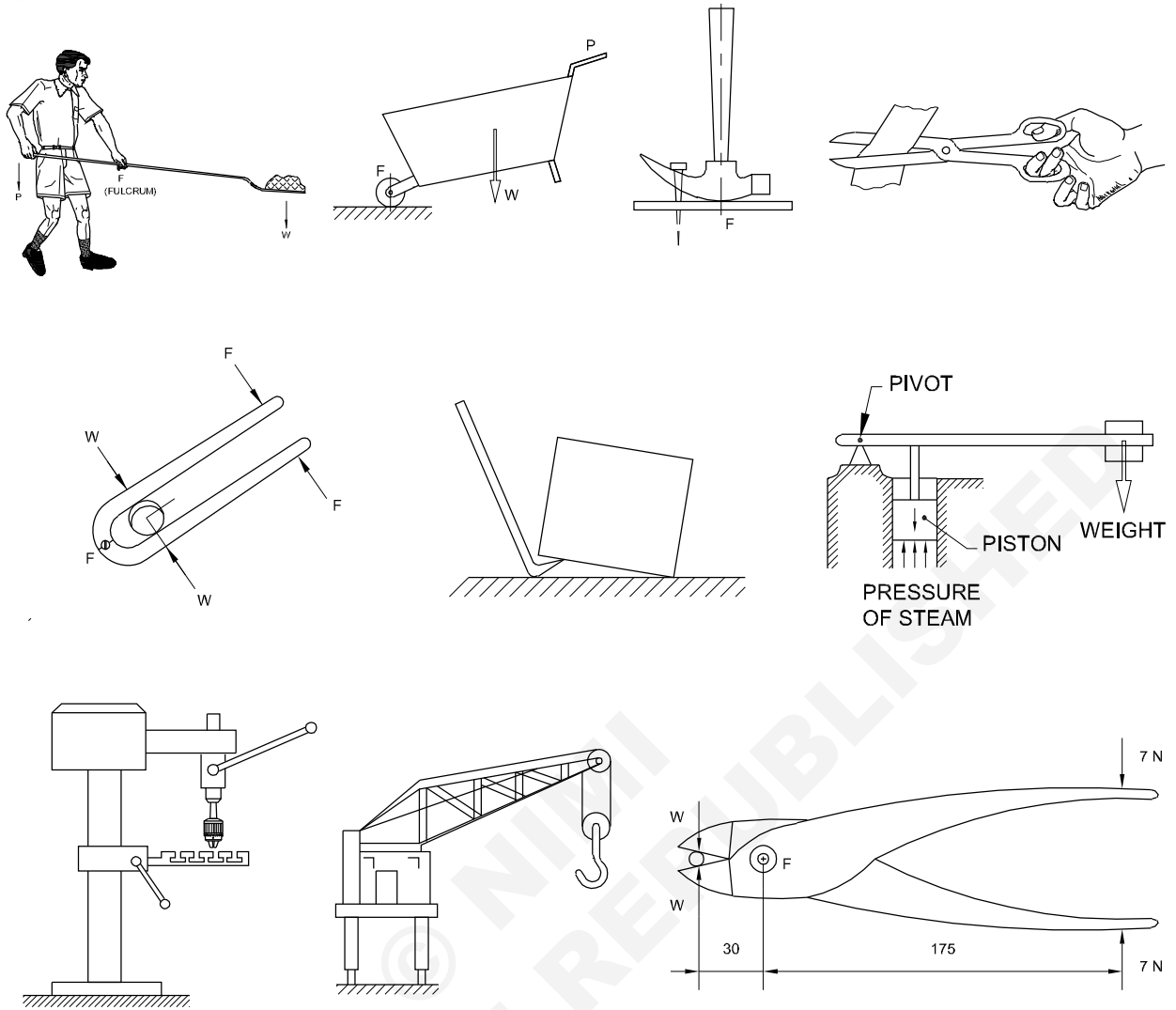
EXAMPLES OF SIMPLE LEVERS

WSNAG192915

Examples

1 **Calculate the load at B, if the load is in the balance condition if a rod AB is 8 metre long and has got a weight of 10 kg at A. The fulcrum is 3 metre from B.**

Load x Load arm = Effort x Effort arm

$$10 \times 5 = P \times 3$$
$$50 = 3P$$
$$P = 50/3$$
$$= 16.67 \text{ kg}$$

Fig 6
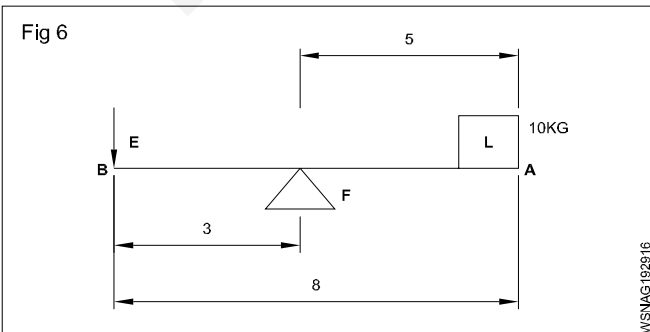
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When load and effort are not given separately in the sum consider which one having more weight is as a load.

2 **Find the effort required and mechanical advantage of the system if a weight of 3000 kg is to be lifted by a bar of length 3 metre. The load arm is 1 metre and the effort arm is 2 metre.**

Fig 7
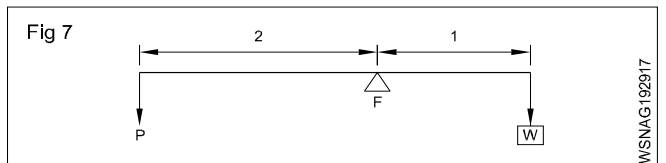
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As per lever principle

Load x Load arm = Effort x Effort arm

$$3000 \times 1 = P \times 2$$
$$3000 = P \times 2$$
$$P = 3000/2$$
$$= 1500 \text{ kg}$$

$$\text{Mechanical advantage} = \frac{\text{Load}}{\text{Effort}} = \frac{3000}{1500}$$

$$= 2$$

3 According to Fig. the lever has to support a 100 kg load with a 17 kg equivalent force supplied to it. Find the distance between the load and point of force.

Fig 8
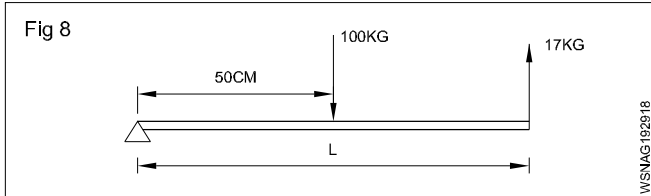
Solution.

Load = 100 kg; Effort = 17 kg.

Load arm = 50 cm

Let effort arm = x cm

As per principle of levers:

Effort x Effort arm = Load x Load arm

$$17x = 100 \times 50$$

$$x = \frac{100 \times 50}{17} = 294.1 \text{ cm}$$

$$x = 294.1 \text{ cm}$$

Distance between the load and point of force = 294.1 - 50

$$= 244.1 \text{ cm}$$

$$= 2.4410 \text{ m}$$

4 Find the tension of the string if an uniform bar of length 80 cm and weighing 2.1 kg is supported on a smooth peg at one end and by a vertical string at a distance of 15 cm from the other end.

Fig 9
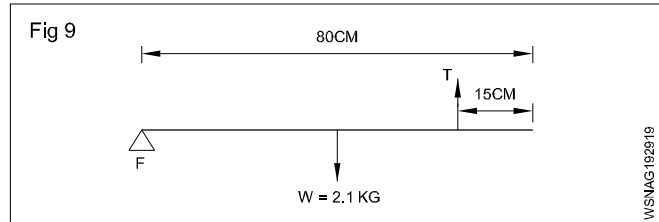
W = 2.1 kg

Tension = T kg

P x dp = 2.1 x dv

$$T \text{ kg} \times (80 - 15) \text{ cm} = 2.1 \text{ kg} \times \frac{80}{2} \text{ cm}$$

$$T \times 65 = 2.1 \times 40$$

$$T = \frac{2.1 \times 40}{65} \text{ kg.}$$

Tension = 1.292 kg

5 In the figure given below in bell cranked lever AFB on perpendicular AF the force P is 40 kg. Weight W is on perpendicular FB. Find the measure of W.

Fig 10
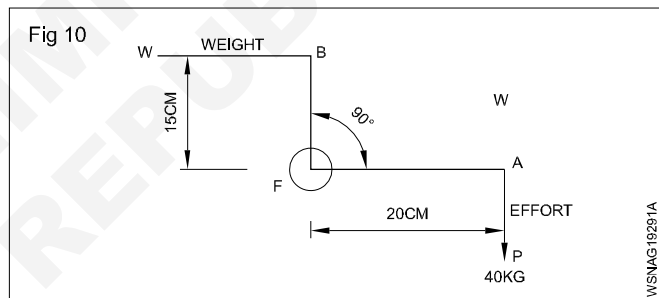
Solution. By principle of momentum

$$P \times AF = W \times BF$$

$$40 \times 20 = W \times 15$$

$$W = \frac{40 \times 20}{15} = \frac{160}{3} = 53.3 \text{ kg.}$$

Assignment

1 a Which order belongs to forearm of a human body.

b Which order belongs to a pair of sugar tongs.

c Which order belongs to carburetor Throttle Valve.

d Which order belongs to a common balance.

e Which order belongs to a pair of scissors.

f Which order belongs to a safety valve.

g Which order belongs to a Crow bar.

h Which order belongs to a Brake lever.

2 a What is the principle of levers?

b Write two examples of first order lever.

c Write two examples of second order lever.

d Write two examples of third order lever.

e Which order belongs to bell cranked lever.

f What is the Mechanical advantage?

g What is the Velocity ratio?

h What is the Efficiency?

Trigonometry - Measurement of angles

Introduction:

Trigonometry is the branch of mathematics which deals with the study of measurement and relationship of the three sides and three angles of a triangle.

Units:

Measurement of Angles

There are three systems of measuring the angle:

(i) Sexagesimal System

This is called British System. In this system, one right angle is divided into 90 equal parts which are called degrees. Each part is divided into 60 parts which are called minutes. Each minute is divided into 60 parts which are called seconds. The parts so divided respectively are called:

One degree (1°), one minute (1') and one second (1")

It means 1 right angle = 90° (90 degrees)

$\qquad$ 1 degree (1°) = 60' (60 minutes)

$\qquad$ 1 minute (1') = 60" (60 seconds)

In Trigonometry, mostly this system is used.

(ii) Centesimal System

This is called French System. In this system, the right angle is divided into 100 equal parts which are called grades. Each grade is divided into 100 minutes and each minute is divided into 100 seconds.

Parts so divided are respectively called:

One grade (1 g), one minute (1'), one second (1").

It means 1 right angle = 100 grades (100g)

$\qquad$ 1 grade (1 g) = 100 minutes (100')

$\qquad$ 1 minute (1') = 100 seconds (100")

$\qquad\qquad$ 90° = 100g (because each is a right angle)

This system is easier than Sexagesimal System. But to use this system many other systems will have to be devised that is why this system is not used.

(iii) Circular System

In this system, the unit of measuring angles is radian. It is that angle which is formed at the centre and is formed of an arc of length equal to radius in a circle.

There is one constant ratio between the circumference and dia of a circle. This is represented by π .

$$\frac{\text{Circumference}}{\text{Diameter}} = \text{constant point} = \pi$$

Circumference $= \pi$ x dia

$\qquad\qquad$ = 2πr (where r is radius of the circle)

$$\pi = \frac{22}{7}$$

Circumference makes an angle (2πr) = 360°

Radius of the circle makes an angle (r) = 1 Radian

$$\text{ie :} \quad \frac{C}{r} = \frac{360°}{1\,\text{Radian}}$$

$$\frac{2\pi r}{r} = \frac{360°}{1\,\text{Radian}}$$

$$2\pi = \frac{360°}{1\,\text{Radian}}$$

$$2\pi \text{ Radian} = 360°$$

$$\pi \text{ Radian} = 180°$$

$$1 \text{ Radian} = \frac{180°}{\pi}$$

$$1° = \frac{\pi}{180°} \text{ Radian}$$

Examples

1 Convert 45°36'20" into degree and decimal of degree.

$\qquad$ 60 second = 1 minute

$$20 \text{ second} = \frac{20}{60} = 0.333'$$

$\qquad$ 60 minute = 1 degree

$$36.333 \text{ minute} = \frac{36.333}{60} = 0.606°$$

$\qquad$ 45°36'20" = 45.606°

2 Convert 24.59° into degree, minute and second

$\qquad$ 1 degree = 60 minute

$\qquad$ 0.59 degree = 0.59 x 60 = 35.4'

$\qquad$ 1 minute = 60 second

$\qquad$ 0.4 minute = 60 sec x 0.4

$\qquad\qquad\qquad$ = 24"

$\qquad$ Therefore 24.59° = 24°35'24"

3 Change 50°37'30" into degrees

$\qquad$ By changing angle degrees into decimals

$$30" = \frac{30}{60} = 0.50'$$

$\qquad$ 37'30" = 37.5'

$$37.5' = \frac{37.5}{60} = 0.625°$$

$\qquad$ 50°37'30" = 50.625°

4 Convert $23^0 25' 32''$ into radians

We know $1^0 = 60' = 3600''$

Therefore $23^0 25' 32''$

$$= \left(23 + \frac{25}{60} + \frac{32}{3600}\right) degrees$$

$$= \frac{82800 + 1500 + 32}{3600}$$

$$= \frac{84332}{3600}$$

But $180^0 = \pi$ radians

Therefore 23.4255 degrees

$$= \frac{23.4255}{180} \pi \text{ radians}$$

$$= \frac{23.4255}{180} \times \frac{22}{7} \text{ radians}$$

= 0.4089 radians

5 Convert $87^0 19' 57''$ into Radian.

$$19'57'' = 19' + \frac{57'}{60}$$

$$= 19' + 0.95'$$

$$= 19.95'$$

$$87°19.95' = 87° + \frac{19.95°}{60}$$

$$= 87° + 0.332° = 87.33°$$

$$1° = \frac{\pi}{180} \text{ radian}$$

$$87.33° = \frac{\pi}{180} \times 87.33 \text{ radian}$$

$$= 1.524 \text{ radian}$$

6 Convert $67°11'43''$ into Radian

$$11'43'' = 11' + \frac{43'}{60}$$

$$= 11' + 0.716'$$

$$= 11.72'$$

$$67°11.72' = 67° + \frac{11.72°}{60}$$

$$= 67° + 0.195°$$

$$= 67.2°$$

$$1° = \frac{\pi}{180} \text{ radian}$$

$$67.2° = \frac{\pi}{180} \times 67.2 \text{ radian}$$

$$= 1.173 \text{ radian}$$

7 Convert $\frac{4}{7}\pi$ radian into degrees

$$1 \text{ radian} = \frac{180}{\pi} \text{ degree}$$

$$\frac{4}{7}\pi \text{ radian} = \frac{180}{\pi} \times \frac{4}{7}\pi \text{ degree}$$

$$= 102.9 \text{ degree}$$

$$= 102^0 \ 0.9 \times 60'$$

$$= 102^0 \ 54'$$

8 Convert 0.8357 radian into degrees

$$1 \text{ radian} = \frac{180}{\pi} \text{ degree}$$

$$0.8357 \text{ radian} = \frac{180}{\pi} \times 0.8357 \text{ degree}$$

$$= 47.88^0$$

$$= 47^0 \ 0.88 \times 60'$$

$$= 47^0 \ 52.80'$$

$$= 47^0 \ 52' 0.8 \times 60''$$

$$= 47^0 \ 52' 48''$$

9 Convert 2.752 radian into degrees

$$1 \text{ Radian} = \frac{180}{\pi} \text{ degree}$$

$$2.7520 \text{ radian} = \frac{180}{\pi} \times 2.752 \text{ degree}$$

$$= 157.7^0$$

$$= 157.7^0 \times 60'$$

$$= 157^0 \ 42'$$

10 Convent $\frac{3}{5}\pi$ radian into degrees

$$1 \text{ Radian} = \frac{180}{\pi} \text{ degree}$$

$$\frac{3}{5}\pi \text{ radian} = \frac{180}{\pi} \times \frac{3}{5}\pi \text{ degree}$$

$$= 108^0$$

Assignment

Convert into Degree

1 12 Radian

Convert into Radians

2 78°

3 47°20'

4 52° 36' 45"

5 25° 38"

Convert into degree, minute and seconds

6 46.723°

7 68.625°

8 0.1269 Radians

9 2.625 Radians

10 3/5 Radians

Trigonometry - Trigonometrical ratios

Dependency

The sides of a triangle bear constant ratios for a given definite value of the angle. That is, increase or decrease in the length of the sides will not affect the ratio between them unless the angle is changed. These ratios are trigonometrical ratios. For the given values of the angle a value of the ratios

$\dfrac{BC}{AB}, \dfrac{AC}{AB}, \dfrac{BC}{AC}, \dfrac{AB}{BC}, \dfrac{AB}{AC}$ and $\dfrac{AC}{BC}$ do not change even when

the sides AB, BC, AC are increased to AB', BC' and AC' or decreased to AB", BC" and AC".

For the angle

AC   is the hypotenuse

AB   is the adjacent side

BC   is the opposite side.

The ratios

Fig 1
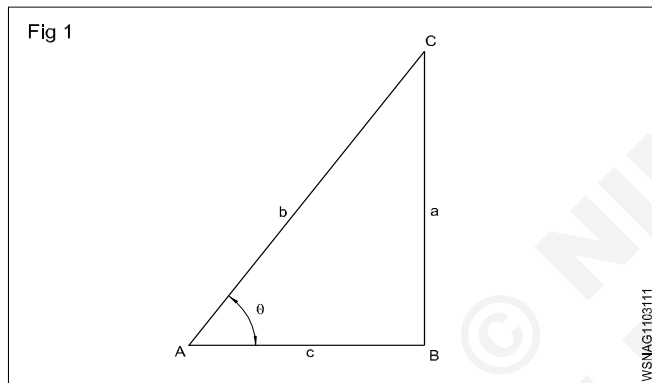
The six ratios between the sides have precise definitions.

$\text{Sine } \theta = \dfrac{BC}{AC} = \dfrac{\text{Opposite side}}{\text{Hypotenuse}} = \text{Sin }\theta$

$\text{Cosine } \theta = \dfrac{AB}{AC} = \dfrac{\text{Adjacent side}}{\text{Hypotenuse}} = \text{Cos }\theta$

$\text{Tangent } \theta = \dfrac{BC}{AB} = \dfrac{\text{Opposite side}}{\text{Adjacent side}} = \text{Tan }\theta$

$\text{Cosecant } \theta = \dfrac{AC}{BC} = \dfrac{\text{Hypotenuse}}{\text{Opposite side}} = \text{Cosec }\theta$

$\text{Secant } \theta = \dfrac{AC}{AB} = \dfrac{\text{Hypotenuse}}{\text{Adjacent side}} = \text{Sec }\theta$

$\text{Cotangent } \theta = \dfrac{AB}{BC} = \dfrac{\text{Adjacent side}}{\text{Opposite side}} = \text{Cot }\theta$

Relationship between the ratios

$\text{Cosec }\theta = \dfrac{AC}{BC} = \dfrac{1}{\dfrac{BC}{AC}} = \dfrac{1}{\sin\theta}$

$\sec\theta = \dfrac{AC}{AB} = \dfrac{1}{\dfrac{AB}{AC}} = \dfrac{1}{\cos\theta}$

$\cot\theta = \dfrac{AB}{BC} = \dfrac{1}{\dfrac{BC}{AB}} = \dfrac{1}{\tan\theta}$

$\sin\theta = \dfrac{\text{side}BC}{\text{side}AC} = \dfrac{a}{b}$

$\cos\theta = \dfrac{\text{side }AB}{\text{side}AC} = \dfrac{c}{b}$

$\dfrac{\sin\theta}{\cos\theta} = \dfrac{\dfrac{a}{b}}{\dfrac{c}{b}} = \dfrac{a}{b} \times \dfrac{b}{c} = \dfrac{a}{c}$

$= \dfrac{\text{side }BC}{\text{side }AB} = \tan\theta$

$\sin\theta = \dfrac{1}{\text{cosec }\theta}$ or cosec $\theta = \dfrac{1}{\sin\theta}$ or $\sin\theta.\text{cosec }\theta = 1$

$\cos\theta = \dfrac{1}{\sec\theta}$ or sec $\theta = \dfrac{1}{\cos\theta}$ or $\cos\theta.\sec\theta = 1$

$\tan\theta = \dfrac{1}{\cot\theta}$ or cot $\theta = \dfrac{1}{\tan\theta}$ or $\cot\theta.\tan\theta = 1$

By pythogoras theorem we have, $AC^2 = AB^2 + BC^2$

Fig 2
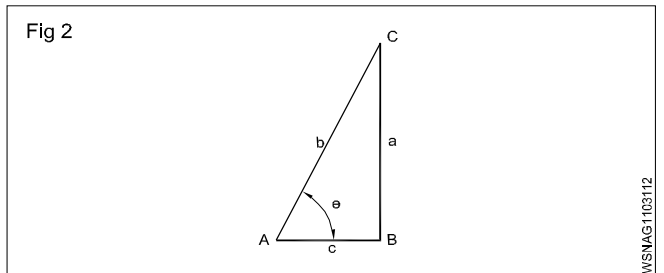
Dividing both sides of the equation by AC^2, we have

$\dfrac{AC^2}{AC^2} = \dfrac{AB^2}{AC^2} + \dfrac{BC^2}{AC^2}$

$= \left[\dfrac{AB}{AC}\right]^2 + \left[\dfrac{BC}{AC}\right]^2$

$1 = (\cos\theta)^2 + (\sin\theta)^2$

$\sin^2\theta + \cos^2\theta = 1$

Sine, Cosine, Tangent, Cosec, Sec and Cotangent are the six trigonometrical ratios

$\tan\theta = \dfrac{\text{Sin }\theta}{\text{Cos }\theta}$ **and $\sin^2\theta + \cos^2\theta = 1$**

$$\sin^2\theta + \cos^2\theta = 1$$

It can be transformed as

$$\sin^2\theta = 1 - \cos^2\theta$$

$$\sin\theta = \sqrt{1 - \cos^2\theta}$$

$$\text{or } \cos^2\theta = 1 - \sin^2\theta$$

$$\cos\theta = \sqrt{1 - \sin^2\theta}$$

$$\tan\theta = \frac{\sin\theta}{\cos\theta} = \frac{\sqrt{1 - \cos^2\theta}}{\cos\theta}$$

$$\tan\theta = \frac{\sin\theta}{\sqrt{1 - \sin^2\theta}}$$

We know $\sin^2\theta + \cos^2\theta = 1$

Dividing both sides by $\cos^2\theta$.

$$\frac{\sin^2\theta}{\cos^2\theta} + \frac{\cos^2\theta}{\cos^2\theta} = \frac{1}{\cos^2\theta}$$

$$\text{or } 1 + \tan^2\theta = \sec^2\theta$$

Using the same equation

$$\sin^2\theta + \cos^2\theta = 1.$$

Dividing both sides by $\sin^2\theta$,

$$1 + \frac{\cos^2\theta}{\sin^2\theta} = \frac{1}{\sin^2\theta}$$

$$1 + \cot^2\theta = \csc^2\theta$$

$$1 + \tan^2\theta = \sec^2\theta$$

Trigonometrical Tables

Ratio	0°	30°	45°	60°	90°
$\sin\theta$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
$\cos\theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
$\tan\theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	∞

When θ increases,

Sine value increases;

Cosine value decreases;

Tangent value increases to more than 1 when the angle is more than 45° (tan60° = 1.732)

Sine of an angle = Cosine of its complementary angle

Cosine of an angle = Sine of its complementary angle

Examples

If $\sin 30^0 = \frac{1}{2}$ find the value of $\sin 60^0$

By applying pythagores theorem

$$BC^2 = AC^2 - AB^2$$

Fig 3

$$BC^2 = 2^2 - 1^2$$

$$= 4 - 1$$

$$= 3$$

$$BC = \sqrt{3}$$
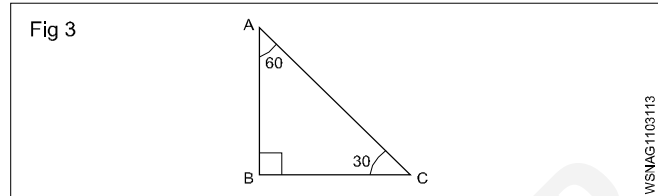
$$\sin 60^0 = \frac{\sqrt{3}}{2}$$

$\cos\theta = \frac{3}{5}$ Find the other trigonometrical ratios

By applying pythagores theorem

$$AB^2 = AC^2 - BC^2$$

$$= 5^2 - 3^2 \qquad = 25 - 9$$

$$= 16$$

Fig 4
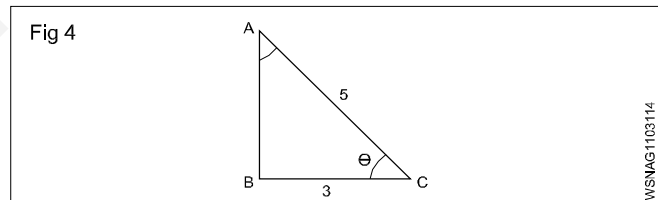
$$AB = \sqrt{16} = 4$$

Now $\sin\theta = \frac{4}{5}$

$$\tan\theta = \frac{4}{3}$$

$$\operatorname{Cosec}\theta = \frac{5}{4}$$

$$\sec\theta = \frac{5}{3}$$

$$\cot\theta = \frac{3}{4}$$

Signs of trigonometrical functions for angles more than 90⁰

Ratio	90 - θ	90 + θ	180 - θ	180 + θ	270 - θ	270 + θ	360 - θ	- θ
sin	cos	cos	sin	- sin	- cos	- cos	- sin	- sin
cos	sin	- sin	- cos	- cos	- sin	sin	cos	cos
tan	cot	- cot	- tan	tan	cot	- cot	- tan	- tan
cosec	sec	sec	cosec	- cosec	- sec	- sec	- cosec	- cosec
sec	cosec	- cosec	- sec	- sec	- cosec	cosec	sec	sec
cot	tan	- tan	- cot	cot	tan	- tan	- cot	- cot

Simplify :

cot θ + tan (180+θ) + tan(90-θ) + (tan 360 - θ)

$$= \cot θ + \tan θ - \cot θ - \tan θ$$

$$= 0$$

Simplify :

$$\frac{\cos\left(90+θ\right)\sec\left(-θ\right)\tan\left(180-θ\right)}{\sec\left(360-θ\right)\sin\left(180+θ\right)\cos\left(90-θ\right)}$$

$$= \frac{\left(-\sin θ\right) \times \left(\sec θ\right) \times \left(-\tan θ\right)}{\left(\sec θ\right) \times \left(-\sin θ\right) \times \left(-\sin θ\right)}$$

$$= \frac{\tan θ}{\sin θ} = \frac{1}{\cos θ} = \sec θ$$

simplify:

$$\frac{\cos\left(90°+θ\right)\sec\left(-θ\right)\tan\left(180°-θ\right)}{\sec\left(360°-θ\right)\sin\left(180°+θ\right)\cot\left(90°-θ\right)}$$

cos (90⁰ + θ) = - sin θ

sec (- θ) = sec θ

tan (180⁰ - θ) = - tan θ

sec (360⁰ - θ) = sec θ

sin (180⁰ + θ) = - sin θ

cot (90⁰ + θ) = - tan θ

$$\frac{\cos\left(90°+θ\right)\sec\left(-θ\right)\tan\left(180°-θ\right)}{\sec\left(360°-θ\right)\sin\left(180°+θ\right)\cot\left(90°-θ\right)}$$

$$= \frac{(-\sin θ)(\sec θ)(\tan θ)}{(\sec θ)(-\sin θ)(-\tan θ)}$$

$$= 1$$

Simplify:

Cot θ + tan (180⁰ + θ) + tan (90⁰ + θ) + tan (360⁰ - θ)

tan (180⁰ - θ) = tan θ

tan (90⁰ + θ) = - cot θ

tan (360⁰ - θ) = - tan θ

cot θ + tan (180⁰ + θ) + tan (90⁰ + θ) + tan (360⁰ - θ)

cot θ + tan θ - cot θ - tan θ = 0

Assignment

1 Given sin 30⁰ = 1/2, find the value of tan 60⁰

2 If cos θ = 4/5, find the other radios

3 If sin A = 3/5, find cos θ, tan θ & sec θ

4 If tan θ = 24/7, find sin θ and cos θ

5 Find the value of cos θ and tan θ, if sin θ = 1/2

6 If cos θ = 5/13, find the value of tan θ

7 If sin θ = 1/2, find the value of $\sin^2 θ - \cos^2 θ$

8 What is the value of

$$\frac{\sin^2 30°}{\cos^2 45°} + \frac{\tan 45°}{\sec 60°} - \frac{\sin 60°}{\cot 45°} - \frac{\cos 30°}{\sin 90°}$$

Simplify :

1 tan (90 + A) + (tan 180 + A) tan (90 + A)

2 $\dfrac{\cos\left(90+θ\right) \cdot \sec\left(-θ\right) \cdot \tan\left(180-θ\right)}{\sec\left(360+θ\right) \cdot \sin\left(180+θ\right) \cdot \cot\left(90+θ\right)}$

Trigonometry - Trigonometrical tables

Use of trigonometrical tables (Ref: Sin, Cos & Tan Table)

	Minutes from 0 to 4						Mean difference				
Deg.	0'	6'	12'	18'	24'	54'	1'	2'	3'	4'	5'
0				.				.			
1				.				.			
2				.				.			
3				.				.			
.				.				.			
.				.				.			
.				.				.			
26	..	..	..	x	..	..	..	5			
.				.							
.											
.											
89											

Sine value for 26°– 20'

Refer to Natural sine table.

Degrees column go up to 26° down

Minutes column 18' horizontal and under this note the value which is given as 0.4431.

Under mean difference for 2' in the same horizontal line 5 is given. Add this to the extreme right number noted for 26°– 18'.

Sine 26° – 20' = 0.4431 + .0005 = 0.4436

Cosine value for 43° – 41'

Referring to the Natural cosines table for 43° –36' it is given as 0.7242 and the mean difference for 5' minutes is given as 10.

cos 43°– 41' = value for cos 43°.36 '
  – the value given for
mean difference of 5 ' = 0.7242 – 0.0010
  = 0.7232

> **When reading sine value add the mean difference value. When reading cosine value subtract the mean difference value.**

Arrangement

Values of trigonometrical ratios can be taken from mathematical tables.

The left hand vertical column consists of degrees.

The top horizontal column is arranged in minutes in steps of 6' from 0' to 54'. In the extreme right horizontal columns the mean differences are written in minutes from 1' to 5' in steps of 1' to account for angles with minutes between the interval of 6'.

> - **The values of cosine, cosecant and cotangent decrease when the value of the angle increases.**
> - **For sine, secant and tangent, the value increases when the angle increases.**
> - **The value of sine and cosine will never be more than 1.**
> - **The value of secant and cosecant will never be less than 1.**
> - **The value of Tan and Cot ranges from 0 to ∞.**

EXAMPLE

From the tables obtain the cosine of 45°–20 '.

cos 45°–18 ' = 0.7108

mean difference for 2 ' = 0.0004

cos 45°– 20 ' = 0.7104

— — — — — — —

SINE TABLE

1   Sin 25⁰ = 0.4226

23   Sin 17⁰ 5'

$$\sin 17° = 0.2924$$
$$\underline{\text{Difference 5'} = 14}$$
$$\sin 17° 5' = 0.2938 \quad \text{Ans}$$

3 **sin 17° 45' 13"**

$$\sin 17° 46' = 0.3051$$
$$\underline{\sin 17° 45' = 0.3048}$$
$$\text{Difference 1'} = 0.0003$$

$$1'(\text{or})\,60'' = 0.0003$$

$$13'' = \frac{0.0003}{60} \times 13$$

$$= \frac{0.0039}{60}$$

$$= \frac{0.00039}{6}$$

$$= 0.000065$$

$$\sin 17^0 45' = 0.3048$$

$$\underline{\qquad\qquad 13'' = 0.000065 \qquad}$$

$$\sin 17^0 45'13'' = 0.304865 \quad \text{Ans.}$$

4 sin82° 14'18"

$$\sin 82^0\ 15' = 0.9908$$

$$\underline{\sin 82^0\ 14' = 0.9908}$$

Difference 1' = 0

$$1'(\text{or})\,60'' = 0$$

$$\sin 18'' = 0$$

$$\sin 82^0\ 14' = 0.9908$$

$$\underline{\qquad\quad 18'' = 0.0000}$$

$$\sin 82^0 41'18'' = 0.9908 \quad \text{Ans.}$$

Finding the corresponding angles when sine values are given:

1. Sin θ = 0.9925

$$\theta = 83^0$$

2. Sin θ = 0.8791

$$0.8788 = \sin 61^0\ 30'$$

$$0.0003 = \qquad\qquad 2'$$

$$\overline{\qquad\qquad\qquad\qquad\qquad}$$

$$0.8791 = \sin 61^0\ 32'$$

3. sin θ = 0.68015

$$0.6794 = \sin 42^0 48'$$

$$0.0006 = \qquad\qquad 3'$$

$$\overline{\qquad\qquad\qquad\qquad\qquad}$$

$$0.6800 = \sin 42^0 51'$$

$$0.6803 = \sin 42^0 52'$$

$$\overline{\qquad\qquad\qquad\qquad\qquad}$$

Difference 0.0003 = 1' (or) 60"

$$0.00015 = \frac{60}{0.0003} \times 0.00015$$

$$= \frac{60 \times 15}{30}$$

$$= 30''$$

$$0.6800 = \sin 42^0 51'$$

$$0.00015 = \qquad\qquad 30''$$

$$\overline{\qquad\qquad\qquad\qquad\qquad}$$

$$0.68015 = \sin 42^0 51'30''$$

$$\overline{\qquad\qquad\qquad\qquad\qquad}$$

$$\boldsymbol{\theta = 42^0\ 51'30''}$$

Calculations involving tapers

D - Big diameter of the taper

d - small diameter of the taper

C - Taper Ratio - 1:x

Fig 1

Fig 2

Fig 3
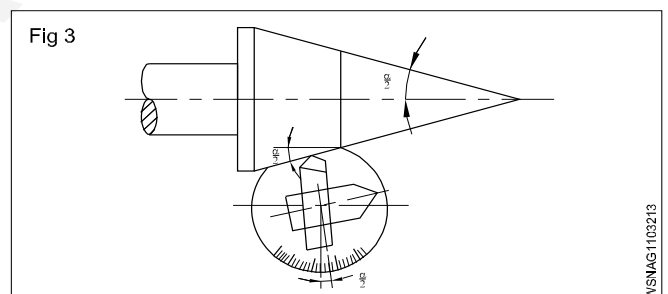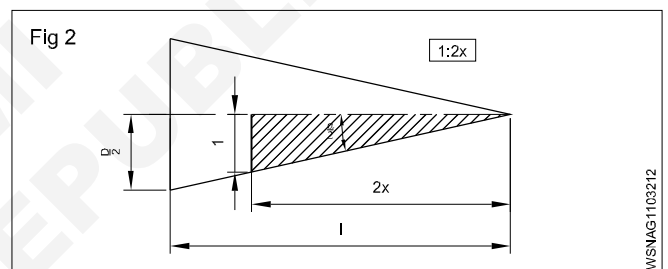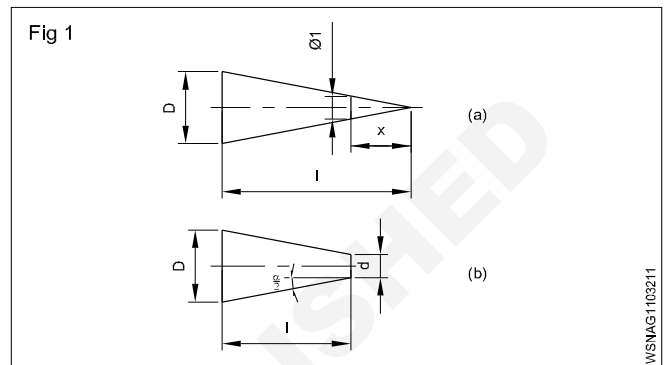
$\dfrac{C}{2}$ Ratio of inclination - 1:2 **x**

l - length of taper

a - included angle of taper

$\dfrac{\alpha}{2}$ - setting angle

Taper ratio = Ratio of inclination (for wedges).

Taper ratio

The ratio between the difference in diameter to the length of the taper is known as taper ratio. *D* is the difference in larger diameter shown in the sketch as the small diameter of taper is 0. Taper ratio is *D : l*. In the sectioned portion the difference in diameter is 1 and the length of taper is shown as *x* .

C = D: d = 1 : x as per Fig 1 (a), C = $\dfrac{D-d}{l}$ as per Fig 1 (b)

Ratio of inclination

Taking half of the taper, $\dfrac{D}{2}$ is the difference in diameter for a taper length of l, if d = 0.

$\therefore \dfrac{C}{2} = \dfrac{D}{2l}$ if the small diameter is 0

or $\dfrac{C}{2} = \dfrac{D-d}{2l}$

1 Ratio of inclination = $\dfrac{1}{2}$ of the taper ratio.

Setting angle

One of the methods of turning taper is by swivelling the compound slide to an angle known as setting angle and feeding the tool at an angle to the axis of work.

$\tan \dfrac{\alpha}{2} = \dfrac{C}{2} = \dfrac{D-d}{2l}$

$\tan \dfrac{\alpha}{2} = \dfrac{\text{taper ratio}}{2}$

$= \dfrac{\text{difference in diameter}}{2 \times \text{taper length}}$

NOTE: $\dfrac{\alpha}{2}$ is the setting angle which is equal to half of the included angle of the taper.

Taper Ratio $C = 1 : x$ or $D : l$ or $(D-d) : l$

Ratio of inclination $\dfrac{C}{2} = 1 : 2x = \dfrac{D}{2} : l$ or $\left(\dfrac{D-d}{2}\right) : l$

Setting angle determination is by the formula

$\tan \dfrac{\alpha}{2} = \dfrac{D-d}{2l} = \dfrac{C}{2}$

Fig 4
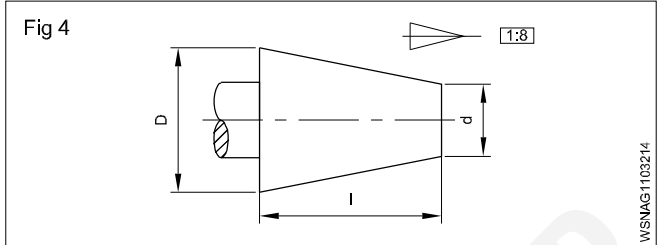
EXAMPLE

A pivot in the form of a frustum of a cone has a taper ratio 1:8. If the small diameter is 30 mm and length of taper is 80 mm, find its large diameter.

$C = 1:8 = \dfrac{1}{8}$

$\therefore \dfrac{D-d}{l} = \dfrac{1}{8}$

$\therefore D - d = \dfrac{1}{8} = \dfrac{80}{8} = 10\,\text{mm}.$

D – 30 mm = 10 mm

D = 10 mm + 30 mm = 40 mm

Large diameter D = 40 mm

— — — — — — —

Cos Table

1 **Cos 38°**

Cos 38°   =   0.7880

2 **Cos 83°12'**

Cos 83°12' = 0.1184

3 **Cos 26°40'**

Cos 26°36' = 0.8942

        4' =   5 (-)

Cos 26°40' = 0.8937

---

4 **Cos 31°20'**

Cos 31°18' = 0.8545

        2' =   3 (-)

Cos 31°20' = 0.8542

Find the corresponding angles when cos values are given:

1 **Cos θ** = **0.5150**

        θ = 59°

2 **Cos θ** = **0.0192**

        θ = 88°54'

3 **Cos θ** = **0.9682**

    0.9686 = cos 14°24'

(-)   4 =   5'

    0.9682 = cos 14° 29'

        θ = 14° 29'

4 **Cos θ**   **=**   **0.8476**

0.8480   =   cos 32° 0'

(-) 0.0003   =   2'

0.8477   =   cos 32° 2'

0.8475   =   cos 32° 3'

0.0002   =   1' (or) 60"

$$0.0001 = \frac{60}{0.0002} \times 0.0001$$

$$= \frac{60}{2} \times 1$$

=   30"

0.8477   =   Cos 32° 2'

(-) 0.0001   =   30" (+)

0.8476   **=**   **Cos 32° 2' 30"**

----

tan Table

1 **tan 35° 37'**

tan 35° 36'   =   0.7159

1'   =   0.0004

----

tan 35° 37'   =   0.7163

----

2 **tan 50° 5'**

Tan 50° 0'   =   1.1918

5'   =   0.0036

Tan 50° 5'   =   1.1954

Find the corresponding angles when tan values are given

1   tan θ   = 0.3972

0.3959   =   tan 21° 36'

0.0013   =   4'

0.3972   =   tan 21° 40'

----

2   tan θ   = 1.0065

1.0035   =   tan 45° 6'

0.0030   =   5'

1.0065   =   tan 45° 11'

Problems Related with Trigonometrical tables

1 **A 250 mm Sine bar is used to measure an angle. If the difference in height is 5 cm, find the angle.**

$$Sin\,\theta = \frac{Opp.side}{Hyp.} = \frac{h}{l}$$

$$= \frac{5\ cm}{250\ mm}$$

$$= \frac{50\ mm}{250\ mm}$$

$$= 0.2000$$

θ   = 11° 32'

2 **Find the height of the slip gauge if a Sine bar with plugs of 10" centre is set up to inspect a taper having an included angle of 9° 56".**

$$Sin\,\theta = \frac{Opp.side}{Hyp.} = \frac{h}{l}$$

$$Sin\ 9°56" = \frac{h}{10}$$

$$\therefore h = 10 \times sin\ 9°56"$$

Fig 5
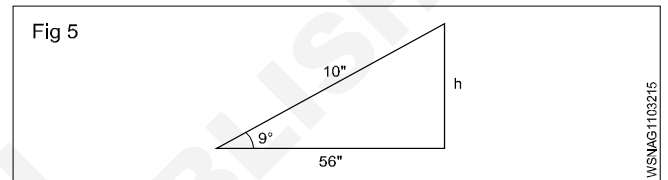
Sin 9° 0"   =   0.1564

Sin 9° 1"   =   0.1567

1' (or) 60"   =   0.0003

$$56" = \frac{0.0003}{60} \times 56$$

$$= \frac{0.0168}{60}$$

$$= \frac{0.00168}{6}$$

$$= 0.00028$$

sin 9° 0' 00"   = 0.1564

56"   = 0.00028

----

sin 9° 0' 56"   = 0.15668

----

h   = 10 x sin 9° 56"

= 10 x 0.15668

= 1.5668 cm

Height of slip gauge = 1.5668"

3 **Find the angle which the ladder makes with the ground if the foot of a 4.5 m long ladder is placed at 1 m away from the wall.**

In Right angled D

$$Cos\ C \quad = \frac{BC}{AC}$$

$$\cos\theta = \frac{1\,m}{4.5\,m} = 0.2222$$

Cos	=	0.2222
0.2233	=	cos 77° 6'
(-) 0.0011	=	4' (+)

0.2222	=	cos 77° 10'

$$\theta = 77°10'$$

Fig 6
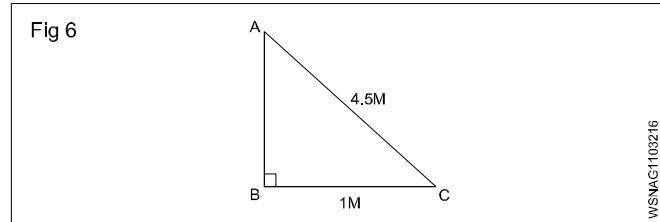
Assignment

I Find the values of the given angles

1 Sin 65°

2 Sin 42° 23'

3 Sin 66° 35' 32"

4 Sin 7° 15' 41"

5 Sin 27° 27"

6 Cos 47° 39'

7 Cos 47° 39'

8 Cos 79° 31' 53"

9 Tan 28° 45'

10 Tan 67° 27' 36"

II Find corresponding angles for given values

1 Sin θ = 0.3062

2 Sin θ = 0.6002

3 Sin θ = 0.22453

4 Sin θ = 0.04802

5 Cos θ = 0.6446

6 Cos θ = 0.8926

7 Cos θ = 0.11773

8 Cos θ = 0.21646

9 Tan θ = 0.3411

10 Tan θ = 2.3868

III

1 Calculate its base. if the slant height of a cone is 12.25 cm and the vertex angle is 110°.

2 A ladder 2.5 m long makes an angle of 60° with the ground. Find the height of the wall where the ladder touches the wall.

3 A sine bar of 200 mm is to be set at an angle of 15° 15' 3". Select the slip gauge block to built up the required height.

4 In a right angled triangle ABC, ∠C = 90°, If AB = 50 mm and ∠B = 75°, Find the remaining sides.

5 Calculate the required length of the bar for this point if a centre point having an included angle of 60° is to be turned at the end of a 50 mm dia bar.

Natural Sines

°	0' 0.0°	6' 0.1°	12' 0.2°	18' 0.3°	24' 0.4°	30' 0.5°	36' 0.6°	42' 0.7°	48' 0.8°	54' 0.9°	1'	2'	3'	4'	5'
0	0.0000	0.0017	0.0035	0.0052	0.0070	0.0087	0.0105	0.0122	0.0140	0.0157	3	6	9	12	15
1	0.0175	0.0192	0.0209	0.0227	0.0244	0.0262	0.0279	0.0297	0.0314	0.0332	3	6	9	12	15
2	0.0349	0.0366	0.0384	0.0401	0.0419	0.0436	0.0454	0.0471	0.0488	0.0506	3	6	9	12	15
3	0.0523	0.0541	0.0558	0.0576	0.0593	0.0610	0.0628	0.0645	0.0663	0.0680	3	6	9	12	15
4	0.0698	0.0715	0.0732	0.0750	0.0767	0.0785	0.0802	0.0819	0.0837	0.0854	3	6	9	12	14
5	0.0872	0.0899	0.0906	0.0924	0.0941	0.0958	0.0976	0.0993	0.1011	0.1028	3	6	9	12	14
6	0.1045	0.1063	0.1080	0.1097	0.1115	0.1132	0.1149	0.1167	0.1184	0.1201	3	6	9	12	14
7	0.1219	0.1236	0.1253	0.1271	0.1288	0.1305	0.1323	0.1340	0.1357	0.1374	3	6	9	12	14
8	0.1392	0.1409	0.1426	0.1444	0.1461	0.1478	0.1495	0.1513	0.1530	0.1547	3	6	9	11	14
9	0.1564	0.1582	0.1599	0.1616	0.1633	0.1650	0.1668	0.1685	0.1702	0.1719	3	6	9	11	14
10	0.1736	0.1754	0.1771	0.1788	0.1805	0.1822	0.1840	0.1857	0.1874	0.1891	3	6	9	11	14
11	0.1908	0.1925	0.1942	0.1959	0.1977	0.1994	0.2011	0.2028	0.2045	0.2062	3	6	9	12	14
12	0.2079	0.2096	0.2113	0.2130	0.2147	0.2164	0.2181	0.2198	0.2215	0.2232	3	6	9	11	14
13	0.2250	0.2267	0.2284	0.2300	0.2317	0.2334	0.2351	0.2368	0.2385	0.2402	3	6	8	11	14
14	0.2419	0.2436	0.2453	0.2470	0.2487	0.2504	0.2521	0.2538	0.2554	0.2571	3	6	8	11	14
15	0.2558	0.2605	0.2622	0.2639	0.2656	0.2672	0.2689	0.2706	0.2723	0.2740	3	6	8	11	14
16	0.2756	0.2773	0.2790	0.2807	0.2823	0.2840	0.2857	0.2874	0.2890	0.2907	3	6	8	11	14
17	0.2924	0.2940	0.2957	0.2974	0.2990	0.3007	0.3024	0.3040	0.3057	0.3074	3	6	8	11	14
18	0.3090	0.3107	0.3123	0.3140	0.3156	0.3173	0.3190	0.3206	0.3223	0.3239	3	6	8	11	14
19	0.3256	0.3272	0.3289	0.3305	0.3322	0.3338	0.3355	0.3371	0.3387	0.3404	3	5	8	11	14
20	0.3420	0.3437	0.3453	0.3469	0.3486	0.3502	0.3518	0.3535	0.3551	0.3567	3	5	8	11	14
21	0.3584	0.3600	0.3616	0.3633	0.3649	0.3665	0.3681	0.3697	0.3714	0.3730	3	5	8	11	14
22	0.3746	0.3762	0.3778	0.3795	0.3811	0.3827	0.3843	0.3859	0.3875	0.3891	3	5	8	11	13
23	0.3907	0.3923	0.3939	0.3955	0.3971	0.3987	0.4003	0.4019	0.4035	0.4051	3	5	8	11	13
24	0.4067	0.4083	0.4099	0.4115	0.4131	0.4147	0.4163	0.4179	0.4195	0.4210	3	5	8	11	13
25	0.4226	0.4242	0.4258	0.4274	0.4289	0.4305	0.4321	0.4337	0.4352	0.4368	3	5	8	11	13
26	0.4384	0.4399	0.4415	0.4431	0.4446	0.4462	0.4478	0.4493	0.4509	0.4524	3	5	8	10	13
27	0.4540	0.4555	0.4571	0.4586	0.4602	0.4617	0.4633	0.4648	0.4664	0.4679	3	5	8	10	13
28	0.4695	0.4710	0.4726	0.4741	0.4756	0.4772	0.4787	0.4802	0.4818	0.4833	3	5	8	10	13
29	0.4848	0.4863	0.4879	0.4894	0.4909	0.4924	0.4939	0.4955	0.4970	0.4985	3	5	8	10	13
30	0.500	0.5015	0.5030	0.5045	0.5060	0.5075	0.5090	0.5105	0.5120	0.5135	3	5	8	10	13
31	0.5150	0.5165	0.5180	0.5195	0.5210	0.5225	0.5240	0.5255	0.5270	0.5284	2	5	7	10	12
32	0.5299	0.5314	0.5329	0.5344	0.5358	0.5373	0.5388	0.5402	0.5417	0.5432	2	5	7	10	12
33	0.5446	0.5461	0.5476	0.5490	0.5505	0.5519	0.5534	0.5548	0.5563	0.5577	2	5	7	10	12
34	0.5592	0.5606	0.5621	0.5635	0.5650	0.5664	0.5678	0.5693	0.5707	0.5721	2	5	7	10	12
35	0.5736	0.5750	0.5764	0.5779	0.5793	0.5807	0.5821	0.5835	0.5850	0.5864	2	5	7	9	12
36	0.5878	0.5892	0.5906	0.5920	0.5934	0.5948	0.5962	0.5976	0.5990	0.6004	2	5	7	9	12
37	0.6018	0.6032	0.6046	0.6060	0.6074	0.6088	0.6101	0.6115	0.6129	0.6143	2	5	7	9	12
38	0.6157	0.6170	0.6184	0.6198	0.6211	0.6225	0.6239	0.6252	0.6266	0.6280	2	5	7	9	11
39	0.6293	0.6307	0.6320	0.6334	0.6347	0.6361	0.6374	0.6388	0.6401	0.6414	2	4	7	9	11
40	0.6428	0.6441	0.6455	0.6468	0.6481	0.6494	0.6508	0.6521	0.6534	0.6547	2	4	7	9	11
41	0.6561	0.6574	0.6587	0.6600	0.6613	0.6626	0.6639	0.6652	0.6665	0.6678	2	4	7	9	11
42	0.6691	0.6704	0.6717	0.6730	0.6743	0.6756	0.6769	0.6782	0.6794	0.6807	2	4	6	9	11
43	0.6820	0.6833	0.6845	0.6858	0.6871	0.6884	0.6896	0.6909	0,6921	0.6934	2	4	6	8	11
44	0.6947	0.6959	0.6972	0.6984	0.6997	0.7009	0.7022	0.7034	0.7046	0.7059	2	4	6	8	10
45	0.7071	0.7083	0.7096	0.7108	0.7120	0.7133	0.7145	0.7157	0.7169	0.7181	2	4	6	8	10
46	0.7193	0.7206	0.7218	0.7230	0.7242	0.7254	0.7266	0.7278	0.7290	0.7302	2	4	6	8	10
47	0.7314	0.7325	0.7337	0.7349	0.7361	0.7373	0.7385	0.7396	0.7408	0.7420	2	4	6	8	10
48	0.7431	0.7443	0.7455	0.7466	0.7478	0.7490	0.7501	0.7513	0.7524	0.7536	2	4	6	8	10
49	0.7547	0.7558	0.7570	0.7581	0.7593	0.7604	0.7615	0.7627	0.7638	0.7649	2	4	6	8	9
50	0.7660	0.7672	0.7683	0.7694	0.7705	0.7716	0.7727	0.7738	0.7749	0.7760	2	4	6	7	9
51	0.7771	0.7782	0.7793	0.7804	0.7815	0.7826	0.7837	0.7848	0.7859	0.7869	2	4	5	7	9
52	0.7880	0.7891	0.7902	0.7912	0.7923	0.7934	0.7944	0.7955	0.7965	0.7976	2	4	5	7	9
53	0.7986	0.7997	0.8007	0.8018	0.8028	0.8039	0.8049	0.8059	0.8070	0.8080	2	3	5	7	9
54	0.8090	0.8100	0.8111	0.8121	0.8131	0.8141	0.8151	0.8161	0.8171	0.8181	2	3	5	7	8
55	0.8192	0.8202	0.8211	0.8221	0.8231	0.8241	0.8251	0.8261	0.8271	0.8281	2	3	5	7	8
56	0.8290	0.8300	0.8310	0.8320	0.8329	0.8339	0.8348	0.8358	0.8368	0.8377	2	3	5	6	8
57	0.8387	0.8396	0.8406	0.8415	0.8425	0.8434	0.8443	0.8453	0.8462	0.8471	2	3	5	6	8
58	0.8480	0.8490	0.8499	0.8508	0.8517	0.8526	0.8536	0.8545	0.8554	0.8563	2	3	5	6	8
59	0.8572	0.8581	0.8590	0.8599	0.8607	0.8616	0.8625	0.8634	0.8643	0.8652	1	3	4	6	7

Natural Sines

°	0' 0.0°	6' 0.1°	12' 0.2°	18' 0.3°	24' 0.4°	30' 0.5°	36' 0.6°	42' 0.7°	48' 0.8°	54' 0.9°	1'	2'	3'	4'	5'
60	0.8660	0.8669	0.8678	0.8686	0.8695	0.8704	0.8712	0.8721	0.8729	0.8738	1	3	4	6	7
61	0.8746	0.8755	0.8763	0.8771	0.8780	0.8788	0.8796	0.8805	0.8813	0.8821	1	3	4	6	7
62	0.8829	0.8838	0.8846	0.8854	0.8862	0.8870	0.8878	0.8886	0.8894	0.8902	1	3	4	5	7
63	0.8910	0.8918	0.8926	0.8934	0.8942	0.8949	0.8957	0.8965	0.8973	0.8980	1	3	4	5	6
64	0.8988	0.8996	0.9003	0.9011	0.9018	0.9026	0.9033	0.9041	0.9048	0.9056	1	3	4	5	6
65	0.9063	0.9070	0.9078	0.9085	0.9092	0.9100	0.9107	0.9114	0.9121	0.9128	1	2	4	5	6
66	0.9135	0.9143	0.9150	0.9157	0.9164	0.9171	0.9178	0.9184	0.9191	0.9198	1	2	3	5	6
67	0.9205	0.9212	0.9219	0.9225	0.9232	0.9239	0.9245	0.9252	0.9259	0.9265	1	2	3	4	6
68	0.9272	0.9278	0.9285	0.9291	0.9298	0.9304	0.9311	0.9317	0.9323	0.9330	1	2	3	4	5
69	0.9336	0.9342	0.9348	0.9354	0.9361	0.9367	0.9373	0.9379	0.9385	0.9391	1	2	3	4	5
70	0.9397	0.9403	0.9409	0.9415	0.9421	0.9426	0.9432	0.9438	0.9444	0.9449	1	2	3	4	5
71	0.9455	0.9461	0.9466	0.9472	0.9478	0.9483	0.9489	0.9494	0.9500	0.9505	1	2	3	4	5
72	0.9511	0.9516	0.9521	0.9527	0.9532	0.9537	0.9542	0.9548	0.9553	0.9558	1	2	3	3	4
73	0.9563	0.9568	0.9573	0.9578	0.9583	0.9588	0.9593	0.9598	0.9603	0.9608	1	2	2	3	4
74	0.9613	0.9617	0.9622	0.9627	0.9632	0.9636	0.9641	0.9646	0.9650	0.9655	1	2	2	3	4
75	0.9659	0.9664	0.9668	0.9673	0.9677	0.9681	0.9686	0.9690	0.9694	0.9699	1	1	2	3	4
76	0.9703	0.9707	0.9711	0.9715	0.9720	0.9724	0.9728	0.9732	0.9736	0.9740	1	1	2	3	3
77	0.9744	0.9748	0.9751	0.9755	0.9759	0.9763	0.9767	0.9770	0.9774	0.9778	1	1	2	2	3
78	0.9781	0.9785	0.9789	0.9792	0.9796	0.9799	0.9803	0.9806	0.9810	0.9813	1	1	2	2	3
79	0.9816	0.9820	0.9823	0.9826	0.9829	0.9833	0.9836	0.9839	0.9842	0.9845	1	1	2	2	3
80	0.9848	0.9851	0.9854	0.9857	0.9860	0.9863	0.9866	0.9869	0.9871	0.9874	0	1	1	2	2
81	0.9877	0.9880	0.9882	0.9885	0.9888	0.9890	0.9893	0.9895	0.9898	0.9900	0	1	1	2	2
82	0.9903	0.9905	0.9907	0.9910	0.9912	0.9914	0.9917	0.9919	0.9921	0.9923	0	1	1	1	2
83	0.9925	0.9928	0.9930	0.9932	0.9934	0.9936	0.9938	0.9940	0.9942	0.9943	0	1	1	1	2
84	0.9945	0.9947	0.9949	0.9951	0.9952	0.9954	0.9956	0.9957	0.9959	0.9960	0	1	1	1	1
85	0.9962	0.9963	0.9965	0.9966	0.9968	0.9969	0.9971	0.9972	0.9973	0.9974	0	0	1	1	1
86	0.9976	0.9977	0.9978	0.9979	0.9980	0.9981	0.9982	0.9983	0.9984	0.9985	0	0	1	1	1
87	0.9986	0.9987	0.9988	0.9989	0.9990	0.9990	0.9991	0.9992	0.9993	0.9993	0	0	0	1	1
88	0.9994	0.9995	0.9995	0.9996	0.9996	0.9997	0.9997	0.9997	0.9998	0.9998	0	0	0	0	0
89	0.9998	0.9999	0.9999	0.9999	0.9999	1.0000	1.0000	1.0000	1.0000	1.0000	0	0	0	0	0
90	1.0000														

Fig 1

SINE CURVE
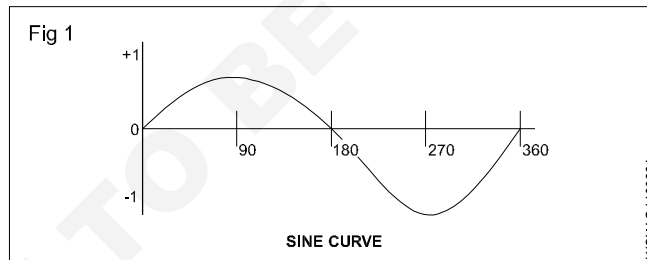
Quadrant	Angle	sinA =	Examples
First	0 to 90°	sin A	sin 34°38' = 0.5683
Second	90° to 180°	sin(180° − A)	sin 145°22' = sin(180° − 145° 22') = sin 34°38' = 0.5683
Third	180° to 270°	−sin(A − 180°)	sin 214°38' = −sin(214°38' − 180°) = −sin34°38' = −0.5683
Fourth	270° to 360°	−sin(360° − A)	sin 325°22' = −sin(360° − 325°22') = − sin 34°38' = −0.5683

Natural Cosines

Numbers in different columns to be subtracted, not added

| °	0' 0.0°	6' 0.1°	12' 0.2°	18' 0.3°	24' 0.4°	30' 0.5°	36' 0.6°	42' 0.7°	48' 0.8°	54' 0.9°	1'	2'	3'	4'	5'
0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9999	0.9999	0	0	0	0	0
1	0.9998	0.9998	0.9998	0.9997	0.9997	0.9997	0.9996	0.9996	0.9995	0.9995	0	0	0	0	0
2	0.9994	0.9993	0.9993	0.9992	0.9991	0.9990	0.9990	0.9989	0.9988	0.9987	0	0	0	1	1
3	0.9986	0.9985	0.9984	0.9983	0.9982	0.9981	0.9980	0.9979	0.9978	0.9977	0	0	1	1	1
4	0.9976	0.9974	0.9973	0.9972	0.9971	0.9969	0.9968	0.9966	0.9965	0.9963	0	0	1	1	1
5	0.9962	0.9960	0.9959	0.9957	0.9956	0.9954	0.9952	0.9951	0.9949	0.9947	0	1	1	1	1
6	0.9945	0.9943	0.9942	0.9940	0.9938	0.9936	0.9934	0.9932	0.9930	0.9928	0	1	1	1	2
7	0.9925	0.9923	0.9921	0.9919	0.9917	0.9914	0.9912	0.9910	0.9907	0.9905	0	1	1	1	2
8	0.9903	0.9900	0.9898	0.9895	0.9893	0.9890	0.9888	0.9885	0.9882	0.9880	0	1	1	2	2
9	0.9877	0.9874	0.9871	0.9869	0.9866	0.9863	0.9860	0.9857	0.9854	0.9851	0	1	1	2	2
10	0.9848	0.9845	0.9842	0.9839	0.9836	0.9833	0.9829	0.9826	0.9823	0.9820	1	1	2	2	3
11	0.9816	0.9813	0.9810	0.9806	0.9803	0.9799	0.9796	0.9792	0.9789	0.9785	1	1	2	2	3
12	0.9781	0.9778	0.9774	0.9770	0.9767	0.9763	0.9759	0.9755	0.9751	0.9748	1	1	2	2	3
13	0.9744	0.9740	0.9736	0.9732	0.9728	0.9724	0.9720	0.9715	0.9711	0.9707	1	1	2	3	3
14	0.9703	0.9699	0.9694	0.9690	0.9686	0.9681	0.9677	0.9673	0.9668	0.9664	1	1	2	3	4
15	0.9659	0.9655	0.9650	0.9646	0.9641	0.9636	0.9632	0.9627	0.9622	0.9617	1	2	2	3	4
16	0.9613	0.9608	0.9603	0.9598	0.9593	0.9588	0.9583	0.9578	0.9573	0.9568	1	2	2	3	4
17	0.9563	0.9558	0.9553	0.9548	0.9542	0.9537	0.9532	0.9527	0.9521	0.9516	1	2	3	3	4
18	0.9511	0.9505	0.9500	0.9494	0.9489	0.9483	0.9478	0.9472	0.9466	0.9461	1	2	3	4	5
19	0.9455	0.9449	0.9444	0.9438	0.9432	0.9426	0.9421	0.9415	0.9409	0.9403	1	2	3	4	5
20	0.9397	0.9391	0.9385	0.9379	0.9373	0.9367	0.9361	0.9354	0.9348	0.9342	1	2	3	4	5
21	0.9336	0.9330	0.9323	0.9317	0.9311	0.9304	0.9298	0.9291	0.9285	0.9278	1	2	3	4	5
22	0.9272	0.9625	0.9259	0.9252	0.9245	0.9239	0.9232	0.9225	0.9219	0.9212	1	2	3	4	6
23	0.9205	0.9198	0.9191	0.9184	0.9178	0.9171	0.9164	0.9157	0.9150	0.9143	1	2	3	5	6
24	0.9135	0.9128	0.9121	0.9114	0.9107	0.9100	0.9092	0.9085	0.9078	0.9070	1	2	4	5	6
25	0.9063	0.9056	0.9048	0.9041	0.9033	0.9026	0.9018	0.9011	0.9003	0.8996	1	3	4	5	6
26	0.8988	0.8980	0.8973	0.8965	0.8957	0.8949	0.8942	0.8934	0.8926	0.8918	1	3	4	5	6
27	0.8910	0.8902	0.8894	0.8886	0.8878	0.8870	0.8862	0.8854	0.8846	0.8838	1	3	4	5	7
28	0.8829	0.8821	0.8813	0.8805	0.8796	0.8788	0.8780	0.8771	0.8763	0.8755	1	3	4	6	7
29	0.8746	0.8738	0.8729	0.8721	0.8712	0.8704	0.8695	0.8686	0.8678	0.8669	1	3	4	6	7
30	0.8660	0.8652	0.8643	0.8634	0.8625	0.8616	0.8607	0.8599	0.8590	0.8581	1	3	4	6	7
31	0.8572	0.8563	0.8554	0.8545	0.8536	0.8526	0.8517	0.8508	0.8499	0.8490	2	3	5	6	8
32	0.8480	0.8471	0.8462	0.8453	0.8443	0.8434	0.8425	0.8415	0.8406	0.8396	2	3	5	6	8
33	0.8387	0.8377	0.8368	0.8358	0.8348	0.8339	0.8329	0.8320	0.8310	0.8300	2	3	5	6	8
34	0.8290	0.8281	0.8271	0.8261	0.8251	0.8241	0.8231	0.8221	0.8211	0.8202	2	3	5	7	8
35	0.8192	0.8181	0.8171	0.8161	0.8151	0.8141	0.8131	0.8121	0.8111	0.8100	2	3	5	7	8
36	0.8090	0.8080	0.8070	0.8059	0.8049	0.8039	0.8028	0.8018	0.8007	0.7997	2	3	5	7	9
37	0.7986	0.7976	0.7965	0.7955	0.7944	0.7934	0.7923	0.7912	0.7902	0.7891	2	4	5	7	9
38	0.7880	0.7869	0.7859	0.7848	0.7837	0.7826	0.7815	0.7804	0.7793	0.7782	2	4	5	7	9
39	0.7771	0.7760	0.7749	0.7738	0.7727	0.7716	0.7705	0.7694	0.7683	0.7672	2	4	6	7	9
40	0.7660	0.7649	0.7638	0.7627	0.7615	0.7604	0.7593	0.7581	0.7570	0.7559	2	4	6	8	9
41	0.7547	0.7536	0.7524	0.7513	0.7501	0.7490	0.7478	0.7466	0.7455	0.7443	2	4	6	8	10
42	0.7431	0.7420	0.7408	0.7396	0.7385	0.7373	0.7361	0.7349	0.7337	0.7325	2	4	6	8	10
43	0.7314	0.7302	0.7290	0.7278	0.7266	0.7254	0.7242	0.7230	0.7218	0.7206	2	4	6	8	10
44	0.7193	0.7181	0.7169	0.7157	0.7145	0.7133	0.7120	0.7108	0.7096	0.7083	2	4	6	8	10
45	0.7071	0.7059	0.7046	0,7034	0.7022	0.7009	0.6997	0.6984	0.6972	0.6959	2	4	6	8	10
46	0.6947	0.6934	0.6921	0.6909	0.6896	0.6884	0.6871	0.6858	0.6845	0.6833	2	4	6	8	11
47	0.6820	0.6807	0.6794	0.6782	0.6769	0.6756	0.6743	0.6730	0.6717	0.6704	2	4	6	9	11
48	0.6691	0.6678	0.6665	0.6652	0.6639	0.6626	0.6613	0.6600	0.6587	0.6574	2	4	7	9	11
49	0.6561	0.6547	0.6534	0.6521	0.6508	0.6494	0.6481	0.6468	0.6455	0.6441	2	4	7	9	11
50	0.6428	0.6414	0.6401	0.6388	0.6374	0.6361	0.6347	0.6334	0.6320	0.6307	2	4	7	9	11
51	0.6293	0.6280	0.6266	0.6252	0.6239	0.6255	0.6211	0.6198	0.6184	0.6170	2	5	7	9	11
52	0.6157	0.6143	0.6129	0.6115	0.6101	0.6088	0.6404	0.6060	0.6046	0.6032	2	5	7	9	12
53	0.6018	0.6004	0.5990	0.5976	0.5962	0.5948	0.5934	0.5920	0.5906	0.5892	2	5	7	9	12
54	0.5878	0.5864	0.5850	0.5835	0.5821	0.5807	0.5793	0.5779	0.5764	0.5750	2	5	7	9	12
55	0.5736	0.5721	0.5707	0.5693	0.5678	0.5664	0.5650	0.5635	0.5621	0.5606	2	5	7	10	12
56	0.5592	0.5577	0.5563	0.5548	0.5534	0.5519	0.5505	0.5490	0.5476	0.5461	2	5	7	10	12
57	0.5446	0.5432	0.5417	0.5402	0.5388	0.5373	0.5358	0.5344	0.5329	0.5314	2	5	7	10	12
58	0.5299	0.5284	0.5270	0.5255	0.5240	0.5225	0.5210	0.5195	0.5180	0.5165	2	5	7	10	12
59	0.5150	0.5135	0.5120	0.5105	0.5090	0.5075	0.5060	0.5045	0.5030	0.5015	3	5	8	10	13

Natural Cosines

Numbers in different columns to be subtracted, not added

°	0' 0.0°	6' 0.1°	12' 0.2°	18' 0.3°	24' 0.4°	30' 0.5°	36' 0.6°	42' 0.7°	48' 0.8°	54' 0.9°	1'	2'	3'	4'	5'
60	0.5000	0.4985	0.4970	0.4955	0.4939	0.4924	0.4909	0.4894	0.4879	0.4863	3	5	8	10	13
61	0.4848	0.4833	0.4818	0.4802	0.4787	0.4772	0.4756	0.4741	0.4726	0.4710	3	5	8	10	13
62	0.4695	0.4679	0.4664	0.4648	0.4633	0.4617	0.4602	0.4586	0.4571	0.4555	3	5	8	10	13
63	0.4540	0.4524	0.4509	0.4493	0.4478	0.4462	0.4446	0.4431	0.4415	0.4399	3	5	8	10	13
64	0.4384	0.4368	0.4352	0.4337	0.4321	0.4305	0.4289	0.4274	0.4258	0.4242	3	5	8	11	13
65	0.4226	0.4210	0.4195	0.4179	0.4163	0.4147	0.4131	0.4115	0.4099	0.4083	3	5	8	11	13
66	0.4067	0.4051	0.4035	0.4019	0.4003	0.3987	0.3971	0.3955	0.3939	0.3923	3	5	8	11	13
67	0.3907	0.3891	0.3875	0.3859	0.3843	0.3827	0.3811	0.3795	0.3778	0.3762	3	5	8	11	13
68	0.3746	0.3730	0.3714	0.3697	0.3681	0.3665	0.3649	0.3633	0.3616	0.3600	3	5	8	11	14
69	0.3584	0.3567	0.3551	0.3535	0.3518	0.3502	0.3486	0.3469	0.3453	0.3437	3	5	8	11	14
70	0.3420	0.3404	0.3387	0.3371	0.3355	0.3338	0.3322	0.3305	0.3289	0.3272	3	5	8	11	14
71	0.3256	0.3239	0.3223	0.3206	0.3190	0.3173	0.3156	0.3140	0.3123	0.3107	3	6	8	11	14
72	0.3090	0.3074	0.3057	0.3040	0.3024	0.3007	0.2990	0.2974	0.2957	0.2940	3	6	8	11	14
73	0.2924	0.2907	0.2890	0.2874	0.2857	0.2840	0.2823	0.2807	0.2790	0.2773	3	6	8	11	14
74	0.2756	0.2740	0.2723	0.2706	0.2689	0.2672	0.2656	0.2639	0.2622	0.2605	3	6	8	11	14
75	0.2588	0.2571	0.2554	0.2538	0.2521	0.2504	0.2487	0.2470	0.2453	0.2436	3	6	8	11	14
76	0.2419	0.2402	0.2385	0.2368	0.2351	0.2334	0.2317	0.2300	0.2284	0.2267	3	6	8	11	14
77	0.2250	0.2233	0.2215	0.2198	0.2181	0.2164	0.2147	0.2130	0.2113	0.2096	3	6	9	11	14
78	0.2079	0.2062	0.2045	0.2028	0.2011	0.1994	0.1977	0.1959	0.1942	0.1925	3	6	9	11	14
79	0.1908	0.1891	0.1874	0.1857	0.1840	0.1822	0.1805	0.1788	0.1771	0.1754	3	6	9	11	14
80	0.1736	0.1719	0.1702	0.1685	0.1668	0.1650	0.1633	0.1616	0.1599	0.1582	3	6	9	11	14
81	0.1564	0.1547	0.1530	0.1513	0.1495	0.1478	0.1461	0.1444	0.1426	0.1409	3	6	9	11	14
82	0.1392	0.1374	0.1357	0.1340	0.1323	0.1305	0.1288	0.1271	0.1253	0.1236	3	6	9	12	14
83	0.1219	0.1201	0.1184	0.1167	0.1149	0.1132	0.1115	0.1097	0.1080	0.1063	3	6	9	12	14
84	0.1045	0.1028	0.1011	0.0993	0.0976	0.0958	0.0941	0.0924	0.0906	0.0889	3	6	9	12	14
85	0.0872	0.0854	0.0837	0.0819	0.0802	0.0785	0.0767	0.0750	0.0732	0.0715	3	6	9	12	14
86	0.0698	0.0680	0.0663	0.0645	0.0628	0.0610	0.0593	0.0576	0.0558	0.0541	3	6	9	12	15
87	0.0523	0.0506	0.0488	0.0471	0.0454	0.0436	0.0419	0.0401	0.0384	0.0366	3	6	9	12	15
88	0.0349	0.0332	0.0314	0.0297	0.0279	0.0262	0.0244	0.0227	0.0209	0.0192	3	6	9	12	15
89	0.0175	0.0157	0.0140	0.0122	0.0105	0.0087	0.0070	0.0052	0.0035	0.0017	3	6	9	12	15
90	0.0000														

Fig 2

COSINE CURVE
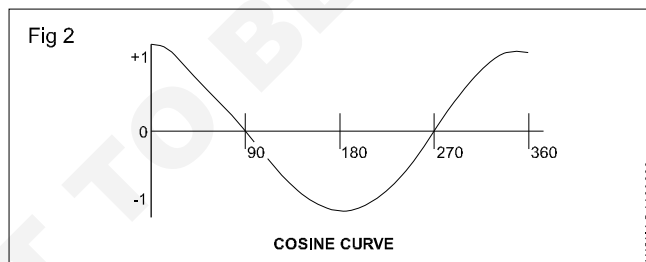
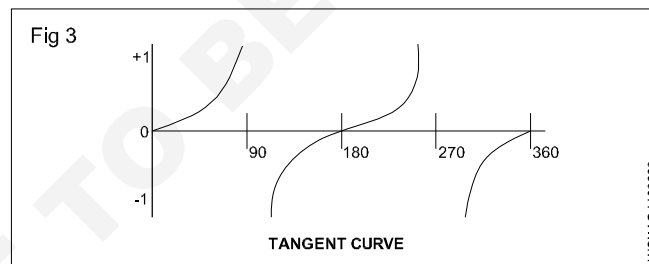| Quadrant	Angle	cos A =	Examples
First	0 to 90°	cos A	cos 33°26' = 0.8345
Second	90° to 180°	−cos(180° − A)	sin 146°34' = −cos(180° − 146o 34') = −cos 33o26' = −0.8345
Third	180° to 270°	cos(A − 180°)	cos 213°26' = −cos(213°26' − 180°) = −cos 33°26' = −0.8345
Fourth	270° to 360°	cos(360° − A)	cos 326°34' = cos(360° − 326°34') = cos 33°26' = 0.8345

Natural Tangents

°	0' 0.0°	6' 0.1°	12' 0.2°	18' 0.3°	24' 0.4°	30' 0.5°	36' 0.6°	42' 0.7°	48' 0.8°	54' 0.9°	1'	2'	3'	4'	5'
0	0.0000	0.0017	0.0035	0.0052	0.0070	0.0087	0.0105	0.0122	0.0140	0.0157	3	6	9	12	15
1	0.0175	0.0192	0.0209	0.0227	0.0244	0.0262	0.0279	0.0297	0.0314	0.0332	3	6	9	12	15
2	0.0349	0.0367	0.0384	0.0402	0.0419	0.0437	0.0454	0.0472	0.0489	0.0507	3	6	9	12	15
3	0.0524	0.0542	0.0559	0.0577	0.0594	0.0612	0.0629	0.0647	0.0664	0.0682	3	6	9	12	15
4	0.0699	0.0717	0.0734	0.0752	0.0769	0.0787	0.0805	0.0822	0.0840	0.0857	3	6	9	12	15
5	0.0875	0.0892	0.0910	0.0928	0.0945	0.0963	0.0981	0.0998	0.1016	0.1033	3	6	9	12	15
6	0.1051	0.1069	0.1086	0.1104	0.1122	0.1139	0.1157	0.1175	0.1192	0.1210	3	6	9	12	15
7	0.1228	0.1246	0.1263	0.1281	0.1299	0.1317	0.1334	0.1352	0.1370	0.1388	3	6	9	12	15
8	0.1405	0.1423	0.1441	0.1459	0.1477	0.1495	0.1512	0.1530	0.1548	0.1566	3	6	9	12	15
9	0.1584	0.1602	0.1620	0.1638	0.1655	0.1673	0.1691	0.1709	0.1727	0.1745	3	6	9	12	15
10	0.1763	0.1781	0.1799	0.1817	0.1835	0.1853	0.1871	0.1890	0.1908	0.1926	3	6	9	12	15
11	0.1944	0.1962	0.1980	0.1998	0.2016	0.2035	0.2053	0.2071	0.2089	0.2107	3	6	9	12	15
12	0.2126	0.2144	0.2162	0.2180	0.2199	0.2217	0.2235	0.2254	0.2272	0.2290	3	6	9	12	15
13	0.2309	0.2327	0.2345	0.2364	0.2382	0.2401	0.2419	0.2438	0.2456	0.2475	3	6	9	12	15
14	0.2493	0.2512	0.2530	0.2549	0.2568	0.2586	0.2605	0.2623	0.2642	0.2661	3	6	9	12	16
15	0.2679	0.2698	0.2717	0.2736	0.2754	0.2773	0.2792	0.2811	0.2830	0.2849	3	6	9	13	16
16	0.2867	0.2886	0.2905	0.2924	0.2943	0.2962	0.2981	0.3000	0.3019	0.3038	3	6	9	13	16
17	0.3057	0.3076	0.3096	0.3115	0.3134	0.3153	0.3172	0.3191	0.3211	0.3230	3	6	10	13	16
18	0.3249	0.3269	0.3288	0.3307	0.3327	0.3346	0.3365	0.3385	0.3404	0.3424	3	6	10	13	16
19	0.3443	0.3463	0.3482	0.3502	0.3522	0.3541	0.3561	0.3581	0.3600	0.3620	3	7	10	13	16
20	0.3640	0.3659	0.3679	0.3699	0.3719	0.3739	0.3759	0.3779	0.3799	0.3819	3	7	10	13	17
21	0.3839	0.3859	0.3879	0.3899	0.3919	0.3939	0.3959	0.3979	0.4000	0.4020	3	7	10	13	17
22	0.4040	0.4061	0.4081	0.4101	0.4122	0.4142	0.4163	0.4183	0.4204	0.4224	3	7	10	14	17
23	0.4245	0.4265	0.4286	0.4307	0.4327	0.4348	0.4369	0.4390	0.4411	0.4431	3	7	10	14	17
24	0.4452	0.4473	0.4494	0.4515	0.4536	0.4557	0.4578	0.4599	0.4621	0.4642	4	7	11	14	18
25	0.4663	0.4684	0.4706	0.4727	0.4748	0.4770	0.4791	0.4813	0.4834	0.4856	4	7	11	14	18
26	0.4877	0.4899	0.4921	0.4942	0.4964	0.4986	0.5008	0.5029	0.5051	0.5073	4	7	11	15	18
27	0.5095	0.5117	0.5139	0.5161	0.5184	0.5206	0.5228	0.5250	0.5272	0.5295	4	7	11	15	18
28	0.5317	0.5340	0.5362	0.5384	0.5407	0.5430	0.5452	0.5475	0.5498	0.5520	4	8	11	15	19
29	0.5543	0.5566	0.5589	0.5612	0.5635	0.5658	0.5681	0.5704	0.5727	0.5750	4	8	12	15	19
30	0.5774	0.5797	0.5820	0.5844	0.5867	0.5890	0.5914	0.5938	0.5961	0.5985	4	8	12	16	20
31	0.6009	0.6032	0.6056	0.6080	0.6104	0.6128	0.6152	0.6176	0.6200	0.6224	4	8	12	16	20
32	0.6249	0.6273	0.6297	0.6322	0.6346	0.6371	0.6395	0.6420	0.6445	0.6469	4	8	12	16	20
33	0.6494	0.6519	0.6544	0.6569	0.6594	0.6619	0.6644	0.6669	0.6694	0.6720	4	8	13	17	21
34	0.6745	0.6771	0.6796	0.6822	0.6847	0.6873	0.6899	0.6924	0.6950	0.6976	4	9	13	17	21
35	0.7002	0.7028	0.7054	0.7080	0.7107	0.7133	0.7159	0.7186	0.7212	0.7239	4	9	13	17	22
36	0.7265	0.7292	0.7319	0.7346	0.7373	0.7400	0.7427	0.7454	0.7481	0.7508	5	9	14	18	23
37	0.7536	0.7563	0.7590	0.7618	0.7646	0.7673	0.7701	0.7729	0.7757	0.7785	5	9	14	18	23
38	0.7813	0.7841	0.7869	0.7898	0.7926	0.7954	0.7983	0.8012	0.8040	0.8069	5	9	14	19	24
39	0.8098	0.8127	0.8156	0.8185	0.8214	0.8243	0.8273	0.8302	0.8332	0.8361	5	10	15	20	24
40	0.8391	0.8421	0.8451	0.8481	0.8511	0.8541	0.8571	0.8601	0.8632	0.8662	5	10	15	20	25
41	0.8693	0.8724	0.8754	0.8785	0.8816	0.8847	0.8878	0.8910	0.8941	0.8972	5	10	16	21	26
42	0.9004	0.9036	0.9067	0.9099	0.9131	0.9163	0.9195	0.9228	0.9260	0.9293	5	11	16	21	27
43	0.9325	0.9358	0.9391	0.9424	0.9457	0.9490	0.9523	0.9556	0.9590	0.9623	6	11	17	22	28
44	0.9657	0.9691	0.9725	0.9759	0.9793	0.9827	0.9861	0.9896	0.9930	0.9965	6	11	17	23	28
45	1.0000	1.0035	1.0070	1.0105	1.0141	1.0176	1.0212	1.0247	1.0283	1.0319	6	12	18	24	30
46	1.0355	1.0392	1.0428	1.0464	1.0501	1.0538	1.0575	1.0612	1.0649	1.0686	6	12	18	25	31
47	1.0724	1.0761	1.0799	1.0837	1.0875	1.0913	1.0951	1.0990	1.1028	1.1067	6	13	19	25	32
48	1.1106	1.1145	1.1184	1.1224	1.1263	1.1303	1.1343	1.1383	1.1423	1.1463	7	13	20	27	33
49	1.1504	1.1544	1.1585	1.1626	1.1667	1.1708	1.1750	1.1792	1.1833	1.1875	7	14	21	28	34
50	1.1918	1.1960	1.2002	1.2045	1.2088	1.2131	1.2174	1.2218	1.2261	1.2305	7	14	22	29	36
51	1.2349	1.2393	1.2437	1.2482	1.2527	1.2572	1.2617	1.2662	1.2708	1.2753	8	15	23	30	38
52	1.2799	1.2846	1.2892	1.2938	1.2985	1.3032	1.3079	1.3127	1.3175	1.3222	8	16	24	31	39
53	1.3270	1.3319	1.3367	1.3416	1.3465	1.3514	1.3564	1.3613	1.3663	1.3713	8	16	25	33	41
54	1.3764	1.3814	1.3865	1.3916	1.3968	1.4019	1.4071	1.4124	1.4176	1.4229	9	17	26	34	43
55	1.4281	1.4335	1.4388	1.4442	1.4496	1.4550	1.4605	1.4659	1.4715	1.4770	9	18	27	36	45
56	1.4826	1.4882	1.4938	1.4994	1.5051	1.5108	1.5166	1.5224	1.5282	1.5340	10	19	29	38	48
57	1.5399	1.5458	1.5517	1.5577	1.5637	1.5697	1.5757	1.5818	1.5880	1.5941	10	20	30	40	50
58	1.6003	1.6066	1.6128	1.6191	1.6255	1.6319	1.6383	1.6447	1.6512	1.6577	11	21	32	43	53
59	1.6643	1.6709	1.6775	1.6842	1.6909	1.6977	1.7045	1.7113	1.7182	1.7251	11	23	34	45	56

Natural Tangents

°	0' 0.0°	6' 0.1°	12' 0.2°	18' 0.3°	24' 0.4°	30' 0.5°	36' 0.6°	42' 0.7°	48' 0.8°	54' 0.9°	1'	2'	3'	4'	5'
60	1.7321	1.7391	1.7461	1.7532	1.7603	1.7675	1.7747	1.7820	1.7893	1.7966	12	24	36	48	60
61	1.8040	1.8115	1.8190	1.8265	1.8341	1.8418	1.8495	1.8572	1.8650	1.8728	13	26	38	51	64
62	1.8807	1.8887	1.8967	1.9047	1.9128	1.9210	1.9292	1.9375	1.9458	1.9542	14	27	41	55	68
63	1.9626	1.9711	1.9797	1.9883	1.9970	2.0057	2.0145	2.0233	2.0323	2.0413	15	29	44	58	73
64	2.0503	2.0594	2.0686	2.0778	2.0872	2.0965	2.1060	2.1155	2.1251	2.1348	16	31	47	63	78
65	2.1445	2.1543	2.1642	2.1742	2.1842	2.1943	2.2045	2.2148	2.2251	2.2355	17	34	51	68	85
66	2.2460	2.2566	2.2673	2.2781	2.2889	2.2998	2.3109	2.3220	2.3332	2.3445	18	37	55	73	92
67	2.3559	2.3673	2.3789	2.3906	2.4023	2.4142	2.4262	2.4383	2.4504	2.4627	20	40	60	79	99
68	2.4751	2.4876	2.5002	2.5129	2.5257	2.5386	2.5517	2.5649	2.5782	2.5916	22	43	65	87	108
69	2.6051	2.6187	2.6325	2.6464	2.6605	2.6746	2.6889	2.7034	2.7179	2.7326	24	47	71	95	119
70	2.7475	2.7625	2.7776	2.7929	2.8083	2.8239	2.8397	2.8556	2.8716	2.8878	26	52	78	104	131
71	2.9042	2.9208	2.9375	2.9544	2.9714	2.9887	3.0061	3.0237	3.0415	3.0595	29	58	87	116	145
72	3.0777	3.0961	3.1146	3.1334	3.1524	3.1716	3.1910	3.2106	3.2305	3.2506	32	64	96	129	161
73	3.2709	3.2914	3.3122	3.3332	3.3544	3.3759	3.3977	3.4197	3.4420	3.4646	36	72	108	144	180
74	3.4874	3.5105	3.5339	3.5576	3.5816	3.6059	3.6305	3.6554	3.6806	3.7062	41	81	122	163	204
75	3.7321	3.7583	3.7848	3.8118	3.8391	3.8667	3.8947	3.9232	3.9520	3.9812	46	93	139	186	232
76	4.0108	4.0408	4.0713	4.1022	4.1335	4.1653	4.1976	4.2303	4.2635	4.2972	53	107	160	213	267
77	4.3315	4.3662	4.4015	4.4374	4.4737	4.5107	4.5483	4.5864	4.6252	4.6646					
78	4.7046	4.7453	4.7867	4.8288	4.8716	4.9152	4.9594	5.0045	5.0504	5.0970					
79	5.1446	5.1929	5.2422	5.2924	5.3435	5.3955	5.4486	5.5026	5.5578	5.6140					
80	5.6713	5.7297	5.7894	5.8502	5.9124	5.9758	6.0405	6.1066	6.1742	6.2432		DIFFERENCES			
81	6.3138	6.3859	6.4596	6.5350	6.6122	6.6912	6.7720	6.8548	6.9395	7.0264		UNTRUSTWORTHY			
82	7.1154	7.2066	7.3002	6.3962	7.4947	7.5958	7.6996	7.8062	7.9158	8.0285		HERE			
83	8.1443	8.2636	8.3863	8.5126	8.6427	8.7769	8.9152	9.0579	9.2052	9.3572					
84	9.5144	9.677	9.845	10.02	10.20	10.39	10.58	10.78	10.99	11.20					
85	11.43	11.66	11.91	12.16	12.43	12.71	13.00	13.30	13.62	13.95					
86	14.30	14.67	15.06	15.46	15.89	16.35	16.83	17.34	17.89	18.46					
87	19.08	19.74	20.45	21.20	22.02	22.90	23.86	24.90	26.03	27.27					
88	28.64	30.14	31.82	33.69	35.80	38.19	40.92	44.07	47.74	52.08					
89	57.29	63.66	71.62	81.85	95.49	114.6	143.2	191.0	286.5	573.0					
90	×														

Fig 3

TANGENT CURVE

Quadrant	Angle	tan A =	Examples
First	0 to 90°	tan A	tan 56°17' = 1.4986
Second	90° to 180°	–tan(180° – A)	tan 123°43' = –tan(180° – 123° 43') = –tan 56°17' = –1.4986
Third	180° to 270°	tan(A – 180°)	tan 236°17' = tan(236°17' – 180°) = tan 56°17' = 1.4986
Fourth	270° to 360°	–tan(360° – A)	tan 303°43' = –tan(360° – 303°43') = – tan 56°17' = –1.4986